Issued: 10/2006

PSP 102.1

The PSP model is a joint development of Arizona State University and NXP Semiconductors Research

G.D.J. Smit, A.J. Scholten, and D.B.M. Klaassen (NXP Semiconductors)

R. van Langevelde (Philips Research Europe)

G. Gildenblat, X. Li, and W. Wu (Arizona State University)

Unclassified Report

© NXP Semiconductors 2006

Concerns:

Period of Work: 2005-2006

Notebooks: None

PSP developers

- At NXP semiconductors Research (formerly Philips Research Europe)
 - Geert D.J. Smit
 - Andries J. Scholten
 - Dirk B.M. Klaassen
- At Philips Research Europe
 - Ronald van Langevelde
- At Arizona State University (formerly at The Pennsylvania State University)
 - Gennady Gildenblat
 - Hailing Wang (until 2005)
 - Xin Li
 - Weimin Wu

Authors' address G.D.J. Smit

A.J. Scholten D.B.M. Klaassen G. Gildenblat Gert-Jan.Smit@nxp.com Andries.Scholten@nxp.com D.B.M.Klaassen@nxp.com Gennady.Gildenblat@asu.edu

© NXP SEMICONDUCTORS 2006

All rights reserved. Reproduction or dissemination in whole or in part is prohibited without the prior written consent of the copyright holder.

Title: PSP 102.1

Author(s): G.D.J. Smit, A.J. Scholten, and D.B.M. Klaassen (NXP Research)

Ronald van Langevelde (Philips Research Europe)

G. Gildenblat, X. Li, and W. Wu (Arizona State University)

Reviewer(s):

Technical Note: TN-

Additional Numbers:

Subcategory:

Project: Compact modeling

Customer: NXP Semiconductors

Keywords: PSP Model, compact modeling, MOSFET, CMOS, circuit simulation, integrated circuits

Abstract: The PSP model is a compact MOSFET model intended for digital, analogue, and RF-

design, which is jointly developed by NXP Semiconductors (formerly part of Philips) and Arizona State University (formerly at The Pennsylvania State University). The roots of PSP lie in both MOS Model 11 (developed by Philips Research) and SP (developed by Penn State University). PSP is a surface-potential based MOS Model, containing all relevant physical effects (mobility reduction, velocity saturation, DIBL, gate current, lateral doping gradient effects, STI stress, etc.) to model present-day and upcoming deepsubmicron bulk CMOS technologies. A source/drain junction model, c.q. the JUNCAP2 model, is an integrated part of PSP. This report contains a full description of the PSP model, including parameter sets, scaling rules, model equations, and a description of the

parameter extraction procedure.

In December 2005, the Compact Model Council (CMC) has elected PSP as the new industrial standard model for compact MOSFET modeling.

History of model and documentation

History of the model

April 2005 Release of PSP 100.0 (which includes JUNCAP2 200.0) as part of SiMKit 2.1. A Verilog-A implementation of the PSP-model is made available as well. The PSP-NQS model is released as Verilog-A code only.

August 2005 Release of PSP 100.1 (which includes JUNCAP2 200.1) as part of SiMKit 2.2. Similar to the previous version, a Verilog-A implementation of the PSP-model is made available as well and the PSP-NQS model is released as Verilog-A code only. Focus of this release was mainly on the optimization of the evaluation speed of PSP. Moreover, the PSP implementation has been extended with operating point output (SiMKit-version only).

March 2006 Release of PSP 101.0 (which includes JUNCAP2 200.1) as part of SiMKit 2.3. PSP 101.0 is *not* backward compatible with PSP 100.1. Similar to the previous version, a Verilog-A implementation of the PSP-model is made available as well and the PSP-NQS model is released as Verilog-A code only. Focus of this release was on the implementation of requirements for CMC standardization, especially those which could not preserve backward compatibility.

June 2006 Release of PSP 102.0 (which includes JUNCAP2 200.1) as part of SiMKit 2.3.2. PSP 102.0 is backward compatible with PSP 101.0 in all practical cases, provided a simple transformation to the parameter set is applied (see description below). Similar to the previous version, a Verilog-A implementation of the PSP-model is made available as well and the PSP-NQS model is released as Verilog-A code only.

Global parameter sets for PSP 101.0 can be transformed to PSP 102.0 by replacing **DPHIBL** (in 102.0 parameter set) by **DPHIBO** · **DPHIBL** (from 101.0 parameter set). After this transformation, the simulation results of PSP 102.0 are identical to those of PSP 101.0 in all practical situations.

October 2006 Release of PSP 102.1 (which includes JUNCAP2 200.2) as part of SiMKit 2.4. PSP 102.1 is backward compatible with PSP 102.0. SiMKit 2.4 includes a preliminary implementation of the PSP-NQS model. Similar to the previous version, a Verilog-A implementation of the PSP-model is available as well. The main changes are:

- Added clipping boundaries for SWNQS
- Several minor changes and improvements in model implementation
- Solved bug in stress model
- Solved bug in JUNCAP2
- Included preliminary implementation of PSP-NQS in SiMKit. This implementation thereby circumvents the problem of the Verilog-A code being too large to compile in Spectre. Moreover, it is computationally more efficient as it uses less rows in the simulator matrix. On the other hand, this implementation has some known limitations. For more details, please contact one of the authors. Further improvements are expected in future releases.

History of the documentation

April 2005 First release of PSP (PSP 100.0) documentation.

August 2005 Documentation updated for PSP 100.1, errors corrected and new items added.

March 2006 Documentation adapted to PSP 101.0. Added more details on noise-model implementation and a full description of the NQS-model.

June 2006 Documentation adapted to PSP 102.0 and some errors corrected.

October 2006 Documentation adapted to PSP 102.1 and some errors corrected.

Contents

1	Intr	oductio	n	1
	1.1	Origin	and purpose	1
	1.2	Structu	ure of PSP	1
	1.3	Availa	bility	2
		1.3.1	SiMKit	3
2	Con	stants a	and Parameters	4
	2.1	Nome	nclature	4
	2.2	Param	eter clipping	4
	2.3	Circuit	t simulator variables	4
	2.4	Model	constants	5
	2.5	Model	parameters	5
		2.5.1	Instance parameters at global level	6
		2.5.2	Instance parameters at local level	7
		2.5.3	Parameters for physical geometrical scaling rules (global model)	9
		2.5.4	Parameters for binning model	15
		2.5.5	Parameters for stress model	25
		2.5.6	Parameters for local model	27
		2.5.7	Parameters for source-bulk and drain-bulk junction model	30
3	Geo	metry a	and Stress dependence	33
	3.1	Introdu	uction	33
	3.2	Geome	etrical scaling rules	33
	3.3	Binnin	ng equations	40
	3.4	Param	eter modification due to stress effects	47
		3.4.1	Layout effects for regular shapes	47
		3.4.2	Layout effects for irregular shapes	47
		3.4.3	Calculation of parameter modifications	47
4	PSP	Model	Equations	51
	4.1	Interna	al Parameters (including Temperature Scaling)	51
	4.2	Model	Equations	55
		4.2.1	Conditioning of Terminal Voltages	55

		4.2.2	Bias-Dependent Body Factor	55
		4.2.3	Surface Potential at Source Side and Related Variables	55
		4.2.4	Drain Saturation Voltage	57
		4.2.5	Surface Potential at Drain Side and Related Variables	58
		4.2.6	Mid-Point Surface Potential and Related Variables	59
		4.2.7	Polysilicon Depletion	60
		4.2.8	Potential Mid-Point Inversion Charge and Related Variables	61
		4.2.9	Drain-Source Channel Current	61
		4.2.10	Auxiliary Variables for Calculation of Intrinsic Charges and Gate Current	62
		4.2.11	Impact Ionization or Weak-Avalanche	62
		4.2.12	Surface Potential in Gate Overlap Regions	63
		4.2.13	Gate Current	64
		4.2.14	Gate-Induced Drain/Source Leakage Current	65
		4.2.15	Total Terminal Currents	66
		4.2.16	Quantum-Mechanical Corrections	67
			Intrinsic Charge Model	67
		4.2.18	Extrinsic Charge Model	67
			Total Terminal Charges	68
			Noise Model	69
5		•	tatic RF model	71
	5.1		action	71
	5.2	-	ffects	71
	5.3		ics circuit	71
	5.4	-	nd RF parameters	72
		5.4.1	Additional Parameters for global NQS model	73
		5.4.2	Additional Parameters for local NQS model	73
		5.4.3	Geometrical Scaling Rules	73
	5.5	NQS M	Model Equations	74
		5.5.1	Internal constants	74
		5.5.2	Position independent quantities	75
		5.5.3	Position dependent surface potential and charge	75
		5.5.4	Cubic spline interpolation	77
		5.5.5	Continuity equation	77
		5.5.6	Non-quasi-static terminal charges	78
6	Emb	edding		80
-	6.1	_	selection	80
	6.2		f parameters	80
	6.3		ding PSP in a Circuit Simulator	80
	6.4		tion of JUNCAP2 in PSP	81
	6.5	_	g-A versus C	84
	0.0	, 51110 g	,	0-1

A	Aux	iliary E	quations	102
8	DC	Operati	ing Point Output	97
	7.6	Extrac	tion of Binning Parameters	. 95
	7.5	Summ	ary – Geometrical scaling	. 95
	7.4	Extrac	tion of Geometry Scaling Parameters	. 93
	7.3	Extrac	tion of Temperature Scaling Parameters	. 91
	7.2	Extrac	tion of local parameters at room temperature	. 88
	7.1	Measu	rements	. 87
7	Para	meter (extraction	87
		6.5.2	Implementation of the noise-equations	. 84
		6.5.1	Implementation of GMIN	. 84

Section 1

Introduction

1.1 Origin and purpose

The PSP model is a compact MOSFET model intended for digital, analogue, and RF-design, which is jointly developed by NXP Semiconductors Research (formerly part of Philips) and Arizona State University (formerly at The Pennsylvania State University). The roots of PSP lie in both *MOS Model 11* (developed by Philips) and *SP* (developed by Penn State University). PSP is a surface-potential based MOS Model, containing all relevant physical effects (mobility reduction, velocity saturation, DIBL, gate current, lateral doping gradient effects, STI stress, etc.) to model present-day and upcoming deep-submicron bulk CMOS technologies. The source/drain junction model, c.q. the JUNCAP2 model, is fully integrated in PSP.

PSP not only gives an accurate description of currents, charges, and their first order derivatives (i.e. transconductance, conductance and capacitances), but also of the higher order derivatives, resulting in an accurate description of electrical distortion behavior. The latter is especially important for analog and RF circuit design. The model furthermore gives an accurate description of the noise behavior of MOSFETs. Finally, PSP has an option for simulation of non-quasi-static (NQS) effects.

The source code of PSP and the most recent version of this documentation are available on the PSP model web site pspmodel.asu.edu and the NXP Semiconductors web site: www.nxp.com/philips_models.

1.2 Structure of PSP

The PSP model has a hierarchical structure, similar to that of MOS Model 11 and SP. This means that there is a strict separation of the geometry scaling in the global model and the model equations in the local model.

As a consequence, PSP can be used at either one of two levels.

- Global level One uses a global parameter set, which describes a whole geometry range. Combined with instance parameters (such as L and W), a local parameter set is internally generated and further processed at the local level in exactly the same way as a custom-made local parameter set.
- Local level One uses a custom-made local parameter set to simulate a transistor with a specific geometry. Temperature scaling is included at this level.

The set of parameters which occur in the equations for the various electrical quantities is called the *local* parameter set. In PSP, temperature scaling parameters are included in the local parameter set. An overview of the local parameters in PSP is given in Section 2.5.6. Each of these parameters can be determined by purely electrical measurements. As a consequence, a local parameter set gives a complete description of the electrical properties of a device of *one* particular geometry.

Since most of these (local) parameters scale with geometry, all transistors of a particular process can be described by a (larger) set of parameters, called the *global* parameter set. An overview of the global parameters

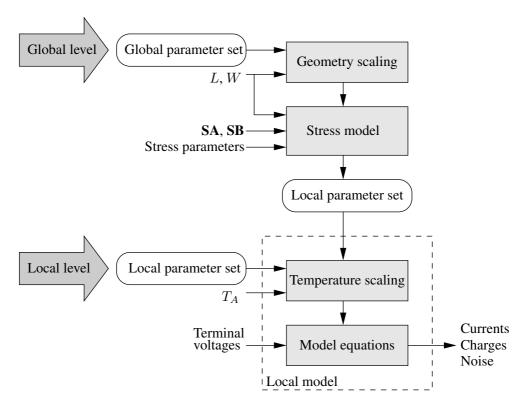


Figure 1.1: Simplified schematic overview of PSP's hierarchical structure.

in PSP is given in Section 2.5.3. Roughly speaking, this set contains all local parameters for a long/wide device plus a number of sensitivity coefficients. From the global parameter set, one can obtain a local parameter set for a specific device by applying a set of scaling rules (see Section 3.2). The geometric properties of that specific device (such as its length and width) enter these scaling rules as *instance parameters*.

From PSP 101.0 onwards it is possible to use a set of binning rules (see Section 3.3) as an alternative to the geometrical (physics based) scaling rules. These binning rules come with their own set of parameters (see Section 2.5.4). Similar to the geometrical scaling rules, the binning rules yield a local parameter set which is used as input for the local model.

PSP is preferably used at global level when designing a circuit in a specific technology for which a global parameter set is available. On the other hand, using PSP at local level can be advantageous during parameter extraction.

As an option, it is possible to deal with the modification of transistor properties due to stress. In PSP, this is implemented by an additional set of transformation rules, which are optionally applied to the intermediate local parameter set generated at the global level. The parameters associated with the stress model are consequently part of the global parameter set (both geometrical and binning).

The model structure described above is schematically depicted in Fig. 1.1.

The JUNCAP2 model is implemented in such a way that the same set of JUNCAP2 parameters can be used at both the global and the local level. This is further explained in Section 6.4.

1.3 Availability

The PSP model developers (The Arizona State University and NXP Semiconductors Research) distribute the PSP code in two formats:

1. Verilog-A code

2. C-code (as part of SiMKit)

The C-version is automatically generated from the Verilog-A version by a software package called ADMS [1]. This procedure guarantees the two implementations to contain identical equations. Nevertheless—due to some specific limitations/capabilities of the two formats—there are a few minor differences, which are described in Section 6.5.

1.3.1 SiMKit

SiMKit is a simulator-independent compact transistor model library. Simulator-specific connections are handled through so-called adapters that provide the correct interfacing to the circuit simulator of choice. Currently, adapters to the following circuit simulators are provided:

- 1. Spectre (Cadence)
- 2. Pstar (Philips/NXP)
- 3. ADS (Agilent)

Section 2

Constants and Parameters

2.1 Nomenclature

The nomenclature of the quantities listed in the following sections has been chosen to express their purpose and their relation to other quantities and to preclude ambiguity and inconsistency. Throughout this document, all PSP parameter names are printed in boldface capitals. Parameters which refer to the long transistor limit and/or the reference temperature have a name containing an 'O', while the names of scaling parameters end with the letter 'L' and/or 'W' for length or width scaling, respectively. Parameters for temperature scaling start with 'ST', followed by the name of the parameter to which the temperature scaling applies. Parameters used for the binning model start with 'PO', 'PL', 'PW', or 'PLW', followed by the name of the local parameter they refer to.

2.2 Parameter clipping

For most parameters, a maximum and/or minimum value is given in the tables below. In PSP, all parameters are limited (clipped) to this pre-specified range in order to prevent difficulties in the numerical evaluation of the model, such as division by zero.

N.B. After computation of the scaling rules (either physical or binning) and stress equations, the resulting local parameters are subjected to the clipping values as given in Section 2.5.6.

2.3 Circuit simulator variables

External electrical variables

The definitions of the external electrical variables are illustrated in Fig. 2.1. The relationship between these external variables and the internal variables used in Chapter 4 is given in Fig. 6.1.

Symbol	Unit	Description				
$V_{ m D}^e$	V	Potential applied to drain node				
$V_{ m G}^e$	V	Potential applied to gate node				
$V_{ m S}^e$	V	Potential applied to source node				
$V_{ m B}^e$	V	Potential applied to bulk node				
$I_{ m D}^e$	A	DC current into drain node				
$I_{ m G}^e$	A	DC current into gate node				

... continued from previous page

Symbol	Unit	Description			
$I_{ m S}^e$	A	DC current into source node			
$I_{ m B}^e$	A	DC current into bulk node			
S_{fl}^{e}	A^2s	Spectral density of flicker noise current in the channel			
S_{id}^e	A^2s	Spectral density of thermal noise current in the channel			
$S_{ig,S}^e$	A^2s	Spectral density of induced gate noise at source side			
$S_{ m ig,D}^e$	A^2s	Spectral density of induced gate noise at drain side			
$S_{ m igs}^e$	A^2s	Spectral density of gate current shot noise at source side			
$S_{ m igd}^e$	A^2s	Spectral density of gate current shot noise at drain side			
$S_{ m j,S}^e$	A^2s	Spectral density of source junction shot noise			
$S_{\mathrm{j,D}}^{e}$	A^2s	Spectral density of drain junction shot noise			
S_{igid}^{e}	A^2s	Cross spectral density between S_{id}^e and $(S_{igS}^e$ or $S_{igD}^e)$			

Other circuit simulator variables

Next to the electrical variables described above, the quantities in the table below are also provided to the model by the circuit simulator.

Symbol	Unit	Description			
$T_{ m A}$	°C	Ambient circuit temperature			
f_{op}	Hz	Operation frequency			

2.4 Model constants

In the following table the symbolic representation, the value and the description of the various physical constants used in the PSP model are given.

No.	Symbol	Unit	Value	Description		
1	T_0	K	273.15	Offset between Celsius and Kelvin tempera-		
				ture scale		
2	$k_{ m B}$	J/K	$1.3806505 \cdot 10^{-23}$	Boltzmann constant		
3	\hbar	J s	$1.05457168 \cdot 10^{-34}$	Reduced Planck constant		
4	q	C	$1.6021918 \cdot 10^{-19}$	Elementary unit charge		
5	m_0	kg	$9.1093826 \cdot 10^{-31}$	Electron rest mass		
6	$\epsilon_{ m ox}$	F/m	$3.453 \cdot 10^{-11}$	Absolute permittivity of oxide		
7	ϵ_{Si}	F/m	$1.045 \cdot 10^{-10}$	Absolute permittivity of silicon		
8	$QM_{ m N}$	$V m^{\frac{4}{3}} C^{-\frac{2}{3}}$	5.951993	Constant of quantum-mechanical behavior of		
				electrons		
9	$QM_{ m P}$	$V m^{\frac{4}{3}} C^{-\frac{2}{3}}$	7.448711	Constant of quantum-mechanical behavior of		
				holes		

2.5 Model parameters

In this section all parameters of the PSP-model are described. The parameters for the intrinsic MOS model, the stress model and the junction model are given in separate tables. The complete parameter list for each of the

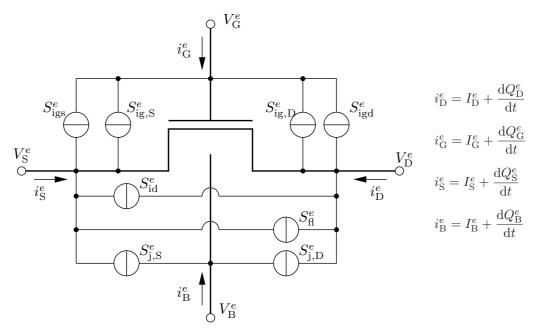


Figure 2.1: Definition of external electrical quantities.

model entry levels is composed of several parts, as indicated in the table below.

Entry level	Sections
Global (geometrical)	2.5.1 (instance parameters)
	2.5.3 (intrinsic MOS)
	2.5.5 (stress)
	2.5.7 (junctions)
Global (binning)	2.5.1 (instance parameters)
	2.5.4 (intrinsic MOS)
	2.5.5 (stress)
	2.5.7 (junctions)
Local	2.5.2 (instance parameters)
	2.5.6 (intrinsic MOS)
	2.5.7 (junctions)

2.5.1 Instance parameters at global level

No.	Name	Unit	Default	Min.	Max.	Description	
0	L	m	$1 \cdot 10^{-6}$	$1 \cdot 10^{-9}$	_	Drawn channel length	
1	W	m	$1 \cdot 10^{-6}$	$1 \cdot 10^{-9}$	_	Drawn channel width	
2	SA	m	0	_	_	Distance between OD-edge and poly at source side	
3	SB	m	0	_	_	Distance between OD-edge and poly at drain side	
4	ABSOURCE	m^2	$1\cdot 10^{-12}$	0	_	Source junction area	

... continued from previous page

No.	Name	Unit	Default	Min.	Max.	Description		
	- 1111-11			1,111	11200120			
5	LSSOURCE	m	$1 \cdot 10^{-6}$	0	_	STI-edge part of source junction perimeter		
6	LGSOURCE	m	$1 \cdot 10^{-6}$	0	_	Gate-edge part of source junction perime-		
						ter		
7	ABDRAIN	m^2	$1 \cdot 10^{-12}$	0	_	Drain junction area		
8	LSDRAIN	m	$1 \cdot 10^{-6}$	0	_	STI-edge part of drain junction perimeter		
9	LGDRAIN	m	$1 \cdot 10^{-6}$	0	_	Gate-edge part of drain junction perimeter		
10	AS	m^2	$1 \cdot 10^{-12}$	0	_	Source junction area (alternative spec.)		
11	PS	m	$1 \cdot 10^{-6}$	0	_	Source STI-edge perimeter (alternative		
						spec.)		
12	AD	m^2	$1 \cdot 10^{-12}$	0	_	Drain junction area (alternative spec.)		
13	PD	m	$1 \cdot 10^{-6}$	0	_	Drain STI-edge perimeter (alternative		
						spec.)		
14	MULT	_	1	0	_	Number of devices in parallel		

Note that if both **SA** and **SB** are set to 0, the stress-equations are not computed.

The switching parameter **SWJUNCAP** is used to determine the meaning and usage of the junction instance parameters, where **AB** (junction area), **LS** (STI-edge part of junction perimeter), and **LG** (gate-edge part of junction perimeter) are the instance parameters of a single instance (source or drain) of the JUNCAP2 model.

	source drain					
SWJUNCAP	AB	LS	LG	AB	LS	LG
0	0	0	0	0	0	0
1	ABSOURCE	LSSOURCE	LGSOURCE	ABDRAIN	LSDRAIN	LGDRAIN
2	AS	PS	$W_{ m E}$	AD	PD	$W_{ m E}$
3	AS	$\mathbf{PS}-W_{\mathrm{E}}$	$W_{ m E}$	AD	$PD - W_{\rm E}$	$W_{ m E}$

2.5.2 Instance parameters at local level

As explained in Section 6.4, the instance parameters for the JUNCAP2 model are used at the local level as well.

No.	Name	Unit	Default	Min.	Max.	Description
0	ABSOURCE	m^2	$1 \cdot 10^{-12}$	0	_	Source junction area
1	LSSOURCE	m	$1 \cdot 10^{-6}$	0	_	STI-edge part of source junction perimeter
2	LGSOURCE	m	$1 \cdot 10^{-6}$	0	_	Gate-edge part of source junction perime-
						ter
3	ABDRAIN	m^2	$1 \cdot 10^{-12}$	0	_	Drain junction area
4	LSDRAIN	m	$1 \cdot 10^{-6}$	0	_	STI-edge part of drain junction perimeter
5	LGDRAIN	m	$1 \cdot 10^{-6}$	0	_	Gate-edge part of drain junction perimeter
6	AS	m^2	$1 \cdot 10^{-12}$	0	_	Source junction area (alternative spec.)
7	PS	m	$1 \cdot 10^{-6}$	0	_	Source STI-edge perimeter (alternative spec.)

... continued from previous page

	1-6-										
No.	Name	Unit	Default	Min.	Max.	Description					
8	AD	m^2	$1\cdot 10^{-12}$	0	_	Drain junction area (alternative spec.)					
9	PD	m	$1 \cdot 10^{-6}$	0	_	Drain STI-edge perimeter (alternative spec.)					
10	JW	m	$1 \cdot 10^{-6}$	0	_	Junction width					
11	MULT	_	1	0	_	Number of devices in parallel					

Also at the local level, the switching parameter $\mathbf{SWJUNCAP}$ is used to determine the meaning and usage of the junction instance parameters, where \mathbf{AB} (junction area), \mathbf{LS} (STI-edge part of junction perimeter), and \mathbf{LG} (gate-edge part of junction perimeter) are the instance parameters of a single instance (source or drain) of the JUNCAP2 model. Because the transistor width W is not available at the local level, an additional instance parameter \mathbf{JW} (junction width) is required when $\mathbf{SWJUNCAP} = 2$ or 3.

		source		drain			
SWJUNCAP	AB	LS	LG	AB	LS	LG	
0	0	0	0	0	0	0	
1	ABSOURCE	LSSOURCE	LGSOURCE	ABDRAIN	LSDRAIN	LGDRAIN	
2	AS	PS	$W_{ m E}$	AD	PD	$W_{ m E}$	
3	AS	PS – JW	JW	AD	PD - JW	JW	

2.5.3 Parameters for physical geometrical scaling rules (global model)

The physical geometry scaling rules of PSP (see Section 3.2) have been developed to give a good description over the whole geometry range of CMOS technologies.

No.	Name	Unit	Default	Min.	Max.	Description					
0	LEVEL	_	1020	_	_	Model selection parameter; see Sec. 6.1					
1	ТҮРЕ	_	1	-1	1	Channel type parameter; $1 \leftrightarrow \text{NMOS}, -1 \leftrightarrow \text{PMOS}^1$					
2	TR	°C	21	-273	_	Reference temperature					
	Switch Parameters										
3	SWIGATE	_	0	0	1	Flag for gate current $(0 \leftrightarrow \text{``off''})$					
4	SWIMPACT	_	0	0	1	Flag for impact ionization current (0 \leftrightarrow "off")					
5	SWGIDL	_	0	0	1	Flag for GIDL/GISL current $(0 \leftrightarrow \text{``off''})$					
6	SWJUNCAP	_	0	0	3	Flag for JUNCAP (0 \leftrightarrow "off"); see Sec. 2.5.1					
7	QMC	_	1	0	_	Quantum-mechanical correction factor					
	Process Parameters										
8	LVARO	m	0	_	_	Geometry independent difference between actual and programmed poly-silicon gate length					
9	LVARL	_	0	_	_	Length dependence of ΔL_{PS}					
10	LVARW	_	0	_	_	Width dependence of ΔL_{PS}					
11	LAP	m	0	_	_	Effective channel length reduction per side due to lateral diffusion of source/drain dopant ions					
12	WVARO	m	0	_	_	Geometry independent difference between actual and programmed field-oxide opening					
13	WVARL	_	0	_	_	Length dependence of $\Delta W_{ m OD}$					
14	WVARW	_	0	_	_	Width dependence of $\Delta W_{ m OD}$					
15	WOT	m	0	_	_	Effective reduction of channel width per side due to lateral diffusion of channel-stop dopant ions					
16	DLQ	m	0	_	_	Effective channel length offset for CV					
17	DWQ	m	0	_	_	Effective channel width offset for CV					
18	VFBO	V	-1	_	_	Geometry-independent flat-band voltage at TR					
19	VFBL	_	0	_	_	Length dependence VFB					
20	VFBW	_	0	_	_	Width dependence of VFB					
21	VFBLW	_	0	_	_	Area dependence of VFB					

 $^{^{1}}$ Note: In the SiMKit-based and built-in version of PSP in *Spectre* one should use type=n and type=p. Similarly, in the SiMKit-based and built-in version of PSP in *ADS* one should use gender=1 and gender=-1.

... continued from previous page

	ntinued from previous Name	Unit	Default	Min.	Mov	Description
No.				IVIIII.	Max.	Description
22	STVFBO	V/K	$5 \cdot 10^{-4}$	_	_	Geometry-independent temperature dependence of VFB
23	STVFBL	_	0	_	_	Length dependence of STVFB
24	STVFBW	_	0	_	_	Width dependence of STVFB
25	STVFBLW	_	0	_	_	Area dependence of STVFB
26	TOXO	m	$2 \cdot 10^{-9}$	10^{-10}	_	Gate oxide thickness
27	NSUBO	m^{-3}	$3 \cdot 10^{23}$	10^{20}	_	Geometry independent substrate doping
28	NSUBW	_	0	_	_	Width dependence of substrate doping due to segregation
29	WSEG	m	10^{-8}	10^{-10}	_	Characteristic length for segregation of substrate doping
30	NPCK	${\rm m}^{-3}$	10^{24}	0	_	Pocket doping level
31	NPCKW	_	0	_	_	Width dependence of NPCK due to segregation
32	WSEGP	m	10^{-8}	10^{-10}	_	Characteristic length for segregation of pocket doping
33	LPCK	m	10^{-8}	10^{-10}	_	Characteristic length for lateral doping profile
34	LPCKW	_	0	_	_	Width dependence of LPCK due to segregation
35	FOL1	_	0	_	_	First order length dependence of short channel body-effect
36	FOL2	_	0			Second order length dependence of short channel body-effect
37	VNSUBO	V	0	_		Effective doping bias-dependence parameter
38	NSLPO	V	0.05	_	_	Effective doping bias-dependence parameter
39	DNSUBO	V^{-1}	0		_,	Effective doping bias-dependence parameter
40	DPHIBO	V	0	_	_	Geometry independent offset of $arphi_{ m B}$
41	DPHIBL	V	0	_	_	Length dependence of DPHIB
42	DPHIBLEXP	_	1	_	_	Exponent for length dependence of DPHIB
43	DPHIBW	_	0	_	_	Width dependence of DPHIB
44	DPHIBLW	_	0	_	_	Area dependence of DPHIB
45	NPO	m^{-3}	10^{26}	_	_	Geometry-independent gate poly-silicon doping
46	NPL	_	0	_	_	Length dependence of NP
47	СТО	_	0	_	_	Geometry-independent part of interface states factor CT
48	CTL	_	0	_	_	Length dependence of CT

 $continued\ on\ next\ page.\dots$

... continued from previous page

	tinued from previous			T		
No.	Name	Unit	Default	Min.	Max.	Description
49	CTLEXP	_	1	_	_	Exponent describing length dependence of CT
50	CTW	_	0	_	_	Width dependence of CT
51	CTLW	_	0	_	_	Area dependence of CT
52	TOXOVO	m	$2 \cdot 10^{-9}$	10^{-10}	-	Overlap oxide thickness
53	LOV	m	0	0	_	Overlap length for gate/drain and gate/source overlap capacitance
54	NOVO	m^{-3}	$5\cdot 10^{25}$	_	_	Effective doping of overlap region
			DI	BL-Para	meters	
55	CFL	V^{-1}	0	_	_	Length dependence of DIBL-parameter
56	CFLEXP	_	2	_	_	Exponent for length dependence of CF
57	CFW	_	0	_	_	Width dependence of CF
58	CFBO	V^{-1}	0	_	_	Back-bias dependence of CF
		1		oility Par	ameters	
59	UO	m ² /V/s	$5 \cdot 10^{-2}$	_	_	Zero-field mobility at TR
60	FBET1	_	0	_	_	Relative mobility decrease due to first lateral profile
61	FBET1W	_	0	_	_	Width dependence of FBET1
62	LP1	m	10^{-8}	10^{-10}	_	Mobility-related characteristic length of first lateral profile
63	LP1W	_	0	_	_	Width dependence of LP1
64	FBET2	_	0	_	_	Relative mobility decrease due to second lateral profile
65	LP2	m	10^{-8}	10^{-10}	_	Mobility-related characteristic length of second lateral profile
66	BETW1	_	0	_	_	First higher-order width scaling coefficient of BETN
67	BETW2	_	0	_		Second higher-order width scaling coefficient of BETN
68	WBET	m	10^{-9}	10^{-10}	_	Characteristic width for width scaling of BETN
69	STBETO	_	1	_	_	Geometry independent temperature dependence of BETN
70	STBETL	-	0	_	ı	Length dependence of STBET
71	STBETW	_	0	_		Width dependence of STBET
72	STBETLW	-	0	_		Area dependence of STBET
73	MUEO	m/V	0.5	_	_	Geometry independent mobility reduction coefficient at TR
74	MUEW	-	0	_	ı	Width dependence of MUE
75	STMUEO	-	0	_		Temperature dependence of MUE
76	ТНЕМИО	-	1.5	0	_	Mobility reduction exponent at TR
77	STTHEMUO	_	1.5	_	_	Temperature dependence of THEMU

... continued from previous page

	tinued from previous p	_	D.C. L	14.	M	D		
No.	Name	Unit	Default	Min.	Max.	Description		
78	CSO	_	0	ı	_	Geometry independent Coulomb scattering parameter at TR		
79	CSL	-	0	_	_	Length dependence of CS		
80	CSLEXP	_	0	_	_	Exponent for length dependence of CS		
81	CSW	_	0	_	_	Width dependence of CS		
82	CSLW	-	0		_	Area dependence of CS		
83	STCSO	_	0	_	_	Temperature dependence of CS		
84	XCORO	V^{-1}	0	_	_	Geometry independent non-universality parameter		
85	XCORL	_	0	1	_	Length dependence of XCOR		
86	XCORW	_	0		_	Width dependence of XCOR		
87	XCORLW	_	0	_	_	Area dependence of XCOR		
88	STXCORO	_	0		_	Temperature dependence of XCOR		
89	FETAO	_	1	-	_	Effective field parameter		
Series Resistance Parameters								
90	RSW1	Ω	2500	_	_	Source/drain series resistance for channel width $W_{\rm EN}$ at ${\bf TR}$		
91	RSW2	-	0	_	_	Higher-order width scaling of source/drain series resistance		
92	STRSO	_	1	_	_	Temperature dependence of RS		
93	RSBO	V^{-1}	0	_	_	Back-bias dependence of RS		
94	RSGO	V^{-1}	0	_	_	Gate-bias dependence of RS		
			Velocity S	Saturatio	n Paran	neters		
95	THESATO	V^{-1}	0	_	_	Geometry independent velocity saturation parameter at TR		
96	THESATL	V^{-1}	0.05	_	_	Length dependence of THESAT		
97	THESATLEXP	_	1	_	_	Exponent for length dependence of THE-SAT		
98	THESATW	_	0	_	_	Width dependence of THESAT		
99	THESATLW	_	0		_	Area dependence THESAT		
100	STTHESATO	_	1	_	_	Geometry independent temperature dependence of THESAT		
101	STTHESATL	_	0	_	_	Length dependence of STTHESAT		
102	STTHESATW	_	0	_	_	Width dependence of STTHESAT		
103	STTHESATLW	_	0	_	_	Area dependence of STTHESAT		
104	THESATBO	V^{-1}	0	_	_	Back-bias dependence of THESAT		
105	THESATGO	V^{-1}	0	_	_	Gate-bias dependence of THESAT		
			Saturatio	n Voltag	e Param	neters		
106	AXO	_	18	_	_	Geometry independent linear/saturation transition factor		
			0.4	0	t	Length dependence of AX		

... continued from previous page

No.	tinued from previous Name	Unit Unit	Default	Min.	Max.	Description				
110.	Name									
100	Channel Length Modulation (CLM) Parameters 108 ALBI Length dependence of CLM profestor									
108	ALPL	_	$5 \cdot 10^{-4}$	_	_	Length dependence of CLM pre-factor ALP				
109	ALPLEXP	_	1	_	_	Exponent for length dependence of ALP				
110	ALPW	_	0	_	_	Width dependence of ALP				
111	ALP1L1	V	0	_	_	Length dependence of CLM enhancement factor above threshold				
112	ALP1LEXP	-	0.5	_	_	Exponent describing the length dependence of ALP1				
113	ALP1L2	_	0	0	_	Second order length dependence of ALP1				
114	ALP1W	_	0	_	_	Width dependence of ALP1				
115	ALP2L1	V	0	_	_	Length dependence of CLM enhancement factor below threshold				
116	ALP2LEXP	-	0.5	_	_	Exponent describing the length dependence ALP2				
117	ALP2L2	_	0	0	_	Second order length dependence of ALP2				
118	ALP2W	_	0	_	_	Width dependence of ALP2				
119	VPO	V	0.05	_	_	CLM logarithmic dependence parameter				
Impact Ionization (II) Parameters										
120	A10	_	1	_	_	Geometry independent part of impactionization pre-factor A1				
121	A1L	_	0	_	_	Length dependence of A1				
122	A1W	_	0	_	_	Width dependence of A1				
123	A2O	V	10	_	_	Impact-ionization exponent at TR				
124	STA2O	V	0	_	_	Temperature dependence of A2				
125	A3O	_	1.0	_	_	Geometry independent saturation-voltage dependence of II				
126	A3L	_	0	-	_	Length dependence of A3				
127	A3W	_	0	_	_	Width dependence of A3				
128	A4O	$V^{-\frac{1}{2}}$	0	_	_	Geometry independent back-bias dependence of II				
129	A4L	_	0	_	_	Length dependence of A4				
130	A4W	_	0	_	_	Width dependence of A4				
			Gate C	Current l	Paramete	ers				
131	GCOO	_	0	_	_	Gate tunneling energy adjustment				
132	IGINVLW	A	0	_	_	Gate channel current pre-factor for a channel area of $W_{\mathrm{EN}} \cdot L_{\mathrm{EN}}$				
133	IGOVW	A	0	_	_	Gate overlap current pre-factor for a channel width of $W_{\mathrm{EN}} \cdot L_{\mathrm{EN}}$				
134	STIGO	_	2	_	_	Temperature dependence of gate current				
135	GC2O	_	0.375	_	_	Gate current slope factor				
136	GC3O	_	0.063	_	_	Gate current curvature factor				

... continued from previous page

No.	Name	Unit	Default	Min.	Max.	Description				
137	СНІВО	V	3.1	_	_	Tunneling barrier height				
	Gate-Induced Drain Leakage (GIDL) Parameters									
138	AGIDLW	A/V ³	0	_	_	Width dependence of GIDL pre-factor				
139	BGIDLO	V	41	_	_	GIDL probability factor at TR				
140	STBGIDLO	V/K	0	_	_	Temperature dependence of BGIDL				
141	CGIDLO	_	0	_	_	Back-bias dependence of GIDL				
			Charge	e Model l	Paramet	ers				
142	CGBOVL	F	0	_	_	Oxide capacitance for gate–bulk overlap for an area of $W_{\mathrm{EN}} \cdot L_{\mathrm{EN}}$				
143	CFRW	F	0	_	_	Outer fringe capacitance for a channel width of W_{EN}				
			Noise	Model P	aramete	rs				
144	FNTO	_	1.0	_	_	Thermal noise coefficient				
145	NFALW	V^{-1} /m ⁴	$8 \cdot 10^{22}$	_	_	First coefficient of flicker noise for a channel area of $W_{\rm EN} \cdot L_{\rm EN}$				
146	NFBLW	V^{-1} /m ²	$3 \cdot 10^7$	_	_	Second coefficient of flicker noise for a channel area of $W_{\rm EN} \cdot L_{\rm EN}$				
147	NFCLW	V^{-1}	0	_	_	Third coefficient of flicker noise for a channel area of $W_{\mathrm{EN}} \cdot L_{\mathrm{EN}}$				
			Ot	her Para	meters					
148	DTA	K	0	_	_	Temperature offset w.r.t. ambient circuit temperature				

2.5.4 Parameters for binning model

The binning scaling rules of PSP (see Section 3.3) have been developed as a flexible but phenomenological alternative to the geometrical scaling rules.

No.	Name	Unit	Default	Min.	Max.	Description					
0	LEVEL	_	1021	_	_	Model selection parameter; see Sec. 6.1					
1	ТҮРЕ	_	1	-1	1	Channel type parameter; $1 \leftrightarrow NMOS, -1 \leftrightarrow PMOS^2$					
2	TR	°C	21	-273	_	reference temperature					
	Switch Parameters										
3	SWIGATE	_	0	0	1	Flag for gate current $(0 \leftrightarrow \text{``off''})$					
4	SWIMPACT	_	0	0	1	Flag for impact ionization current (0 \leftrightarrow "off")					
5	SWGIDL	_	0	0	1	Flag for GIDL/GISL current $(0 \leftrightarrow \text{``off''})$					
6	SWJUNCAP	_	0	0	3	Flag for JUNCAP (0 \leftrightarrow "off"); see Sec. 2.5.2					
7	QMC	_	1	0	_	Quantum-mechanical correction factor					
			Proce	ss Parar	neters						
8	LVARO	m	0	_	_	Geometry independent difference between actual and programmed poly-silicon gate length					
9	LVARL	_	0	_	_	Length dependence of difference between actual and programmed poly-silicon gate length					
10	LAP	m	0	_	_	Effective channel length reduction per side due to lateral diffusion of source/drain dopant ions					
11	WVARO	m	0	_	_	Geometry independent difference between actual and programmed field-oxide opening					
12	WVARW	_	0	_	_	Width dependence of difference between actual and programmed field-oxide opening					
13	WOT	m	0	_	_	Effective reduction of channel width per side due to lateral diffusion of channel-stop dopant ions					
14	DLQ	m	0	_	-	Effective channel length reduction for CV					
15	DWQ	m	0	_	_	Effective channel width reduction for CV					
16	POVFB	V	-1	_	_	Coefficient for the geometry independent part of flat-band voltage at TR					
17	PLVFB	V	0	_	_	Coefficient for the length dependence of flat-band voltage at TR					
18	PWVFB	V	0	_	_	Coefficient for the width dependence of flat-band voltage at TR					

 $^{^2}$ Note: In the SiMKit-based and built-in version of PSP in *Spectre* one should use type=n and type=p. Similarly, in the SiMKit-based and built-in version of PSP in *ADS* one should use gender=1 and gender=-1.

... continued from previous page

	continued from previous page										
No.	Name	Unit	Default	Min.	Max.	Description					
19	PLWVFB	V	0	_	_	Coefficient for the length times width dependence of flat-band voltage at TR					
20	POSTVFB	V/K	$5 \cdot 10^{-4}$	_	_	Coefficient for the geometry independent part of temperature dependence of VFB					
21	PLSTVFB	V/K	0	_	_	Coefficient for the length dependence of temperature dependence of VFB					
22	PWSTVFB	V/K	0	_	_	Coefficient for the width dependence of temperature dependence of VFB					
23	PLWSTVFB	V/K	0	_	_	Coefficient for the length times width dependence of temperature dependence of VFB					
24	POTOX	m	$2 \cdot 10^{-9}$	_	_	Coefficient for the geometry independent part of gate oxide thickness					
25	PONEFF	m^{-3}	$5 \cdot 10^{23}$	_	_	Coefficient for the geometry independent part of substrate doping					
26	PLNEFF	m^{-3}	0	_	_	Coefficient for the length dependence of substrate doping					
27	PWNEFF	m^{-3}	0	_	_	Coefficient for the width dependence of substrate doping					
28	PLWNEFF	m^{-3}	0	_	_	Coefficient for the length times width dependence of substrate doping					
29	POVNSUB	V	0	_	_	Coefficient for the geometry independent part of effective doping bias-dependence parameter					
30	PONSLP	V	$5 \cdot 10^{-2}$	_	_	Coefficient for the geometry independent part of effective doping bias-dependence parameter					
31	PODNSUB	V ⁻¹	0	_	_	Coefficient for the geometry independent part of effective doping bias-dependence parameter					
32	PODPHIB	V	0	_	_	Coefficient for the geometry independent part of offset of $\phi_{\rm B}$					
33	PLDPHIB	V	0	_	_	Coefficient for the length dependence of offset of $\phi_{\rm B}$					
34	PWDPHIB	V	0	_	_	Coefficient for the width dependence of offset of $\phi_{\rm B}$					
35	PLWDPHIB	V	0	_	_	Coefficient for the length times width dependence of offset of $\phi_{\rm B}$					
36	PONP	m^{-3}	10^{26}	_	_	Coefficient for the geometry independent part of gate poly-silicon doping					
37	PLNP	m^{-3}	0	_	_	Coefficient for the length dependence of gate poly-silicon doping					
38	PWNP	m^{-3}	0	_	_	Coefficient for the width dependence of gate poly-silicon doping					

... continued from previous page

	ntinued from previous				1	I				
No.	Name	Unit	Default	Min.	Max.	Description				
39	PLWNP	m^{-3}	0	_	_	Coefficient for the length times width dependence of gate poly-silicon doping				
40	POCT	_	0	_	_	Coefficient for the geometry independent part of interface states factor				
41	PLCT	_	0	_	_	Coefficient for the length dependence of interface states factor				
42	PWCT	_	0	_	_	Coefficient for the width dependence of interface states factor				
43	PLWCT	_	0	_	_	Coefficient for the length times width dependence of interface states factor				
44	POTOXOV	m	$2\cdot 10^{-9}$	_	_	Coefficient for the geometry independent part of overlap oxide thickness				
45	PONOV	m^{-3}	$5\cdot 10^{25}$	_	_	Coefficient for the geometry independent part of effective doping of overlap region				
46	PLNOV	m^{-3}	0	_	_	Coefficient for the length dependence of effective doping of overlap region				
47	PWNOV	m^{-3}	0	_	_	Coefficient for the width dependence of effective doping of overlap region				
48	PLWNOV	m ⁻³	0	_	_	Coefficient for the length times width dependence of effective doping of overlap region				
	DIBL Parameters									
49	POCF	V ⁻¹	0	_	_	Coefficient for the geometry independent part of DIBL parameter				
50	PLCF	V^{-1}	0	_	_	Coefficient for the length dependence of DIBL parameter				
51	PWCF	V^{-1}	0	_	_	Coefficient for the width dependence of DIBL parameter				
52	PLWCF	V^{-1}	0	_	_	Coefficient for the length times width dependence of DIBL parameter				
53	POCFB	V^{-1}	0	_	_	Coefficient for the geometry independent part of back-bias dependence of CF				
			Mobil	ity Para	meters					
54	POBETN	m ² /V/s	$7 \cdot 10^{-2}$	_	_	Coefficient for the geometry independent part of product of channel aspect ratio and zero-field mobility at TR				
55	PLBETN	m ² /V/s	0	_	_	Coefficient for the length dependence of product of channel aspect ratio and zero-field mobility at TR				
56	PWBETN	m ² /V/s	0	_	_	Coefficient for the width dependence of product of channel aspect ratio and zero-field mobility at TR				
57	PLWBETN	m ² /V/s	0	_	_	Coefficient for the length times width dependence of product of channel aspect ratio and zero-field mobility at TR				

... continued from previous page

No.	ntinued from previous pa	Unit	Description			
		Unit	Default	Min.	Max.	<u> </u>
58	POSTBET	_	1	_	_	Coefficient for the geometry independent part of temperature dependence of BETN
59	PLSTBET	_	0	_	_	Coefficient for the length dependence of temperature dependence of BETN
60	PWSTBET	_	0	_	_	Coefficient for the width dependence of temperature dependence of BETN
61	PLWSTBET	_	0	_	_	Coefficient for the length times width dependence of temperature dependence of BETN
62	POMUE	m/V	$5 \cdot 10^{-1}$	_	_	Coefficient for the geometry independent part of mobility reduction coefficient at TR
63	PLMUE	m/V	0	_	_	Coefficient for the length dependence of mobility reduction coefficient at TR
64	PWMUE	m/V	0	_	_	Coefficient for the width dependence of mobility reduction coefficient at TR
65	PLWMUE	m/V	0	_	_	Coefficient for the length times width dependence of mobility reduction coefficient at TR
66	POSTMUE	_	0	_	_	Coefficient for the geometry independent part of temperature dependence of MUE
67	POTHEMU	-	1.5	_	_	Coefficient for the geometry independent part of mobility reduction exponent at TR
68	POSTTHEMU	_	1.5	_	_	Coefficient for the geometry independent part of temperature dependence of THEMU
69	POCS	_	0	_	_	Coefficient for the geometry independent part of Coulomb scattering parameter at TR
70	PLCS	_	0	_	_	Coefficient for the length dependence of Coulomb scattering parameter at TR
71	PWCS	_	0	_	_	Coefficient for the width dependence of Coulomb scattering parameter at TR
72	PLWCS	_	0	_	_	Coefficient for the length times width dependence of Coulomb scattering parameter at TR
73	POSTCS	_	0	_	_	Coefficient for the geometry independent part of temperature dependence of CS
74	POXCOR	V^{-1}	0	_	_	Coefficient for the geometry independent part of non-universality parameter
75	PLXCOR	V^{-1}	0	_	_	Coefficient for the length dependence of non-universality parameter
76	PWXCOR	V^{-1}	0	_	_	Coefficient for the width dependence of non-universality parameter

... continued from previous page

	continued from previous page										
No.	Name	Unit	Default	Min.	Max.	Description					
77	PLWXCOR	V^{-1}	0	_	_	Coefficient for the length times width dependence of non-universality parameter					
78	POSTXCOR	-	0	_	_	Coefficient for the geometry independent part of temperature dependence of XCOR					
79	POFETA	-	1	_	_	Coefficient for the geometry independent part of effective field parameter					
	Series Resistance Parameters										
80	80 PORS Ω 30 $-$ Coefficient for the geometry independ part of source/drain series resistance at Ω										
81	PLRS	Ω	0	_	_	Coefficient for the length dependence of source/drain series resistance at TR					
82	PWRS	Ω	0	_	_	Coefficient for the width dependence of source/drain series resistance at TR					
83	PLWRS	Ω	0	_	_	Coefficient for the length times width dependence of source/drain series resistance at TR					
84	POSTRS	_	1	_	_	Coefficient for the geometry independent part of temperature dependence of RS					
85	PORSB	V^{-1}	0	_	_	Coefficient for the geometry independent part of back-bias dependence of RS					
86	PORSG	V^{-1}	0	_	_	Coefficient for the geometry independent part of gate-bias dependence of RS					
			Velocity Sa	turation	Parame	ters					
87	POTHESAT	V^{-1}	1	_	_	Coefficient for the geometry independent part of velocity saturation parameter at TR					
88	PLTHESAT	V^{-1}	0	_	_	Coefficient for the length dependence of velocity saturation parameter at TR					
89	PWTHESAT	V^{-1}	0	_	_	Coefficient for the width dependence of velocity saturation parameter at TR					
90	PLWTHESAT	V^{-1}	0	_	_	Coefficient for the length times width dependence of velocity saturation parameter at TR					
91	POSTTHESAT	-	1	_	_	Coefficient for the geometry independent part of temperature dependence of THE-SAT					
92	PLSTTHESAT	_	0	_	_	Coefficient for the length dependence of temperature dependence of THESAT					
93	PWSTTHESAT	_	0	_	_	Coefficient for the width dependence of temperature dependence of THESAT					
94	PLWSTTHESAT	_	0	_	_	Coefficient for the length times width dependence of temperature dependence of THESAT					

... continued from previous page

	continued from previous page								
No.	Name	Unit	Default	Min.	Max.	Description			
95	POTHESATB	V^{-1}	0	_	_	Coefficient for the geometry independent part of back-bias dependence of velocity saturation			
96	PLTHESATB	V^{-1}	0	_	_	Coefficient for the length dependence of back-bias dependence of velocity saturation			
97	PWTHESATB	V^{-1}	0	_	_	Coefficient for the width dependence of back-bias dependence of velocity saturation			
98	PLWTHESATB	V^{-1}	0	_	_	Coefficient for the length times width dependence of back-bias dependence of velocity saturation			
99	POTHESATG	V^{-1}	0	_	_	Coefficient for the geometry independent part of gate-bias dependence of velocity saturation			
100	PLTHESATG	V^{-1}	0	_	_	Coefficient for the length dependence of gate-bias dependence of velocity saturation			
101	PWTHESATG	V^{-1}	0	_	_	Coefficient for the width dependence of gate-bias dependence of velocity saturation			
102	PLWTHESATG	V^{-1}	0	_	_	Coefficient for the length times width dependence of gate-bias dependence of velocity saturation			
			Saturation	Voltage	Paramet	ters			
103	POAX	_	3	_	_	Coefficient for the geometry independent part of linear/saturation transition factor			
104	PLAX	_	0	_	_	Coefficient for the length dependence of linear/saturation transition factor			
105	PWAX	_	0	_	_	Coefficient for the width dependence of linear/saturation transition factor			
106	PLWAX	_	0	_	_	Coefficient for the length times width dependence of linear/saturation transition factor			
		Chanr	el Length Mo	dulation	(CLM)	Parameters			
107	POALP	_	10^{-2}	_	_	Coefficient for the geometry independent part of CLM pre-factor			
108	PLALP	_	0	_	_	Coefficient for the length dependence of CLM pre-factor			
109	PWALP	_	0	_	_	Coefficient for the width dependence of CLM pre-factor			
110	PLWALP	_	0	_	_	Coefficient for the length times width dependence of CLM pre-factor			
111	POALP1	V	0	_	_	Coefficient for the geometry independent part of CLM enhancement factor above threshold			

... continued from previous page

coi	continued from previous page									
No.	Name	Unit	Default	Min.	Max.	Description				
112	PLALP1	V	0	_	_	Coefficient for the length dependence of CLM enhancement factor above threshold				
113	PWALP1	V	0	_	_	Coefficient for the width dependence of CLM enhancement factor above threshold				
114	PLWALP1	V	0	_	_	Coefficient for the length times width dependence of CLM enhancement factor above threshold				
115	POALP2	V ⁻¹	0	_	_	Coefficient for the geometry independent part of CLM enhancement factor below threshold				
116	PLALP2	V ⁻¹	0	_	_	Coefficient for the length dependence of CLM enhancement factor below threshold				
117	PWALP2	V ⁻¹	0	_	_	Coefficient for the width dependence of CLM enhancement factor below threshold				
118	PLWALP2	V ⁻¹	0	_	_	Coefficient for the length times width dependence of CLM enhancement factor below threshold				
119	POVP	V	$5 \cdot 10^{-2}$	_	_	Coefficient for the geometry independent part of CLM logarithmic dependence parameter				
			Impact Ioniz	ation (II) Param	eters				
120	POA1	_	1	_	_	Coefficient for the geometry independent part of impact-ionization pre-factor				
121	PLA1	_	0	_	_	Coefficient for the length dependence of impact-ionization pre-factor				
122	PWA1	_	0	_	_	Coefficient for the width dependence of impact-ionization pre-factor				
123	PLWA1	_	0	_	_	Coefficient for the length times width dependence of impact-ionization pre-factor				
124	POA2	V	10	_	_	Coefficient for the geometry independent part of impact-ionization exponent at TR				
125	POSTA2	V	0	_	_	Coefficient for the geometry independent part of temperature dependence of A2				
126	POA3	_	1	_	_	Coefficient for the geometry independent part of saturation-voltage dependence of II				
127	PLA3	-	0	_	_	Coefficient for the length dependence of saturation-voltage dependence of II				
128	PWA3	_	0	_	_	Coefficient for the width dependence of saturation-voltage dependence of II				
129	PLWA3	_	0	_	_	Coefficient for the length times width dependence of saturation-voltage dependence of II				
130	POA4	$V^{-0.5}$	0	_	_	Coefficient for the geometry independent part of back-bias dependence of II				

... continued from previous page

coi	continued from previous page									
No.	Name	Unit	Default	Min.	Max.	Description				
131	PLA4	V ^{-0.5}	0	_	_	Coefficient for the length dependence of back-bias dependence of II				
132	PWA4	$V^{-0.5}$	0	_	_	Coefficient for the width dependence of back-bias dependence of II				
133	PLWA4	$V^{-0.5}$	0	_	_	Coefficient for the length times width dependence of back-bias dependence of II				
			Gate Cu	rrent Pa	rameter	s				
134	POGCO	_	0	_	_	Coefficient for the geometry independent part of gate tunneling energy adjustment				
135	POIGINV	A	0	_	_	Coefficient for the geometry independent part of gate channel current pre-factor				
136	PLIGINV	A	0	_	_	Coefficient for the length dependence of gate channel current pre-factor				
137	PWIGINV	A	0	_	_	Coefficient for the width dependence of gate channel current pre-factor				
138	PLWIGINV	A	0	_	_	Coefficient for the length times width dependence of gate channel current prefactor				
139	POIGOV	A	0	_		Coefficient for the geometry independent part of gate overlap current pre-factor				
140	PLIGOV	A	0	_	_	Coefficient for the length dependence of gate overlap current pre-factor				
141	PWIGOV	A	0	_	_	Coefficient for the width dependence of gate overlap current pre-factor				
142	PLWIGOV	A	0	_	_	Coefficient for the length times width dependence of gate overlap current pre-factor				
143	POSTIG	-	2	_	_	Coefficient for the geometry independent part of temperature dependence of gate current				
144	POGC2	_	$3.75 \cdot 10^{-1}$	_	_	Coefficient for the geometry independent part of gate current slope factor				
145	POGC3	_	$6.3 \cdot 10^{-2}$	_	_	Coefficient for the geometry independent part of gate current curvature factor				
146	РОСНІВ	V	3.1	_	_	Coefficient for the geometry independent part of tunneling barrier height				
			nduced Drain	Leakag	e (GIDL) Parameters				
147	POAGIDL	A/V ³	0	_	_	Coefficient for the geometry independent part of GIDL pre-factor				
148	PLAGIDL	A/V ³	0	_	_	Coefficient for the length dependence of GIDL pre-factor				
149	PWAGIDL	A/V ³	0	_	_	Coefficient for the width dependence of GIDL pre-factor				
150	PLWAGIDL	A/V ³	0	_	_	Coefficient for the length times width dependence of GIDL pre-factor				

... continued from previous page

	continued from previous page							
No.	Name	Unit	Default	Min.	Max.	Description		
151	POBGIDL	V	41	_	_	Coefficient for the geometry independent part of GIDL probability factor at TR		
152	POSTBGIDL	V/K	0	_	_	Coefficient for the geometry independent part of temperature dependence of BGIDL		
153	POCGIDL		0	_	_	Coefficient for the geometry independent part of back-bias dependence of GIDL		
			Charge I	Model Pa	rametei	rs		
154	POCOX	F	10^{-14}	_	_	Coefficient for the geometry independent part of oxide capacitance for intrinsic channel		
155	PLCOX	F	0	_	_	Coefficient for the length dependence of oxide capacitance for intrinsic channel		
156	PWCOX	F	0	_	_	Coefficient for the width dependence of oxide capacitance for intrinsic channel		
157	PLWCOX	F	0	_	_	Coefficient for the length times width dependence of oxide capacitance for intrinsic channel		
158	POCGOV	F	10^{-15}	_	_	Coefficient for the geometry independent part of oxide capacitance for gatedrain/source overlap		
159	PLCGOV	F	0	_	_	Coefficient for the length dependence of oxide capacitance for gate-drain/source overlap		
160	PWCGOV	F	0	_	_	Coefficient for the width dependence of oxide capacitance for gate-drain/source overlap		
161	PLWCGOV	F	0	_	_	Coefficient for the length times width dependence of oxide capacitance for gatedrain/source overlap		
162	POCGBOV	F	0	_	_	Coefficient for the geometry independent part of oxide capacitance for gate-bulk overlap		
163	PLCGBOV	F	0	_	_	Coefficient for the length dependence of oxide capacitance for gate-bulk overlap		
164	PWCGBOV	F	0	_	_	Coefficient for the width dependence of oxide capacitance for gate-bulk overlap		
165	PLWCGBOV	F	0	_	_	Coefficient for the length times width dependence of oxide capacitance for gatebulk overlap		
166	POCFR	F	0		_	Coefficient for the geometry independent part of outer fringe capacitance		
167	PLCFR	F	0	_	_	Coefficient for the length dependence of outer fringe capacitance		
168	PWCFR	F	0	_	_	Coefficient for the width dependence of outer fringe capacitance		

... continued from previous page

No.	Name	Unit	Default	Min.	Max.	Description				
169	PLWCFR	F	0	_	_	Coefficient for the length times width dependence of outer fringe capacitance				
Noise Model Parameters										
170	POFNT	_	1	_	_	Coefficient for the geometry independent part of thermal noise coefficient				
171	PONFA	V^{-1}/m^4	$8 \cdot 10^{22}$	_	_	Coefficient for the geometry independent part of first coefficient of flicker noise				
172	PLNFA	V ⁻¹ /m ⁴	0	_	_	Coefficient for the length dependence of first coefficient of flicker noise				
173	PWNFA	V ⁻¹ /m ⁴	0	_	_	Coefficient for the width dependence of first coefficient of flicker noise				
174	PLWNFA	V^{-1}/m^4	0	_	_	Coefficient for the length times width dependence of first coefficient of flicker noise				
175	PONFB	V^{-1}/m^2	$3 \cdot 10^7$	_	_	Coefficient for the geometry independent part of second coefficient of flicker noise				
176	PLNFB	V^{-1}/m^2	0	_	_	Coefficient for the length dependence of second coefficient of flicker noise				
177	PWNFB	V^{-1}/m^2	0	_	_	Coefficient for the width dependence of second coefficient of flicker noise				
178	PLWNFB	V^{-1} /m ²	0	_	_	Coefficient for the length times width dependence of second coefficient of flicker noise				
179	PONFC	V^{-1}	0	_	_	Coefficient for the geometry independent part of third coefficient of flicker noise				
180	PLNFC	V^{-1}	0	_	_	Coefficient for the length dependence of third coefficient of flicker noise				
181	PWNFC	V^{-1}	0	_	_	Coefficient for the width dependence of third coefficient of flicker noise				
182	PLWNFC	V^{-1}	0	_	_	Coefficient for the length times width dependence of third coefficient of flicker noise				
			Othe	er Param	eters					
183	DTA	K	0	_	_	temperature offset w.r.t. ambient circuit temperature				

2.5.5 Parameters for stress model

The stress model of BSIM4.4.0 has been adopted in PSP with as little modifications as possible. Parameter names have been copied, but they have been subjected to PSP conventions by replacing every zero by an 'O'. Moreover, the parameters STK2 and LODK2 are not available in PSP. Except for these changes, stress parameters determined for BSIM can be directly applied in PSP.

The parameters in this section are part of PSP's global parameter set (both geometrical and binning).

No.	Name	Unit	Default	Min.	Max.	Description
0	SAREF	m	10^{-6}	10^{-9}	_	Reference distance between OD edge to Poly from one side
1	SBREF	m	10^{-6}	10^{-9}	_	Reference distance between OD edge to Poly from other side
2	WLOD	m	0	_	_	Width parameter
3	KUO	m	0	_	_	Mobility degrada- tion/enhancement coef- ficient
4	KVSAT	m	0	-1	1	Saturation velocity degradation/enhancement parameter
5	TKUO	-	0	_	_	Temperature coefficient of KUO
6	LKUO	m ^{LLODKUO}	0	_	_	Length dependence of KUO
7	WKUO	mWLODKUO	0	_	_	Width dependence of KUO
8	PKUO	mLLODKUO+WLODKUO	0	_	_	Cross-term dependence of KUO
9	LLODKUO	-	0	0	_	Length parameter for mobility stress effect
10	WLODKUO	-	0	0	_	Width parameter for mobility stress effect
11	KVTHO	Vm	0	_	_	Threshold shift parameter
12	LKVTHO	m ^{LLODVTH}	0	_	_	Length dependence of KVTHO
13	WKVTHO	mwlodvth	0	_	_	Width dependence of KVTHO
14	PKVTHO	mLLODVTH+WLODVTH	0	_	_	Cross-term dependence of KVTHO
15	LLODVTH	-	0	0	_	Length parameter for thres- hold voltage stress effect
16	WLODVTH	-	0	0	_	Width parameter for thres- hold voltage stress effect
17	STETAO	m	0	_	_	ETAO shift factor related to threshold voltage change

... continued from previous page

No.	Name	Unit	Default	Min.	Max.	Description
18	LODETAO	_	1	0	_	ETAO shift modification
						factor

2.5.6 Parameters for local model

The set of local parameters valid for an individual transistor with a specific channel width and length are given in the table below. Since the local parameter set is valid for one device with a specific geometry, it does not contain the channel length and width as instance parameters.

No.	Name	Unit	Default	Min.	Max.	Description	
0	LEVEL	_	102	_	_	Model selection parameter; see Sec. 6.1	
1	ТҮРЕ	_	1	-1	1	Channel type parameter; $1 \leftrightarrow NMOS, -1 \leftrightarrow PMOS^3$	
2	TR	°C	21	-273	_	Reference temperature	
Switch Parameters							
3	SWIGATE	_	0	0	1	Flag for gate current $(0 \leftrightarrow \text{``off''})$	
4	SWIMPACT	_	0	0	1	Flag for impact ionization current (0 \leftrightarrow "off")	
5	SWGIDL	-	0	0	1	Flag for GIDL/GISL current $(0 \leftrightarrow \text{``off''})$	
6	SWJUNCAP	-	0	0	3	Flag for JUNCAP (0 \leftrightarrow "off"); see Sec. 2.5.2	
7	QMC	_	1	0	_	Quantum-mechanical correction factor	
			P	rocess Pa	rametei	rs	
8	VFB	V	-1	_	_	Flat-band voltage at TR	
9	STVFB	V/K	$5 \cdot 10^{-4}$	_	_	Temperature dependence of VFB	
10	TOX	m	$2 \cdot 10^{-9}$	10^{-10}	_	Gate oxide thickness	
11	NEFF	m^{-3}	$5 \cdot 10^{23}$	10^{20}	10^{26}	Substrate doping	
12	VNSUB	V	0	_	_	Effective doping bias-dependence parameter	
13	NSLP	V	0.05	10^{-3}	_	Effective doping bias-dependence parameter	
14	DNSUB	V^{-1}	0	0	1	Effective doping bias-dependence parameter	
15	DPHIB	V	0	_	-	Offset of $arphi_{ m B}$	
16	NP	${\rm m}^{-3}$	10^{26}	0	_	Substrate doping Effective doping bias-dependence parameter Effective doping bias-dependence parameter Effective doping bias-dependence parameter Offset of $\varphi_{\rm B}$ Gate poly-silicon doping Interface states factor Overlap oxide thickness	
17	CT	_	0	0	_	Interface states factor	
18	TOXOV	m	$2 \cdot 10^{-9}$	10^{-10}	_	Overlap oxide thickness	
19	NOV	m^{-3}	$5\cdot 10^{25}$	10^{20}	10^{27}	Effective doping of overlap region	
			I	DIBL Par	rameters	S	
20	CF	V^{-1}	0	0	_	DIBL parameter	
21	CFB	V^{-1}	0	0	1	Back-bias dependence of CF	
				obility Pa	aramete	rs	
22	BETN	m ² /V/s	$7 \cdot 10^{-2}$	0	_	Product of channel aspect ratio and zero-field mobility at TR	
23	STBET	_	1	_	_	Temperature dependence of BETN	
24	MUE	m/V	0.5	0	_	Mobility reduction coefficient at TR	

continued on next page...

³Note: In the SiMKit-based and built-in version of PSP in *Spectre* one should use type=n and type=p. Similarly, in the SiMKit-based and built-in version of PSP in *ADS* one should use gender=1 and gender=-1.

... continued from previous page

continued from previous page									
No.	Name	Unit	Default	Min.	Max.	Description			
25	STMUE	_	0	_	1	Temperature dependence of MUE			
26	THEMU	_	1.5	0	ı	Mobility reduction exponent at TR			
27	STTHEMU	_	1.5	_	ı	Temperature dependence of THEMU			
28	CS	_	0	0	_	Coulomb scattering parameter at TR			
29	STCS	_	0	_	_	Temperature dependence of CS			
30	XCOR	V^{-1}	0	0	_	Non-universality parameter			
31	STXCOR	_	0	_	_	Temperature dependence of XCOR			
32	FETA	_	1	0	_	Effective field parameter			
			Series	Resistan	ce Parai	meters			
33	RS	Ω	30	0	_	Source/drain series resistance at TR			
34	STRS	-	1	_	_	Temperature dependence of RS			
35	RSB	V^{-1}	0	-0.5	1	Back-bias dependence of RS			
36	RSG	V^{-1}	0	-0.5	_	Gate-bias dependence of RS			
			Velocity	Saturat	ion Para	nmeters			
37	THESAT	V^{-1}	1	0	_	Velocity saturation parameter at TR			
38	STTHESAT	-	1	_	_	Temperature dependence of THESAT			
39	THESATB	V^{-1}	0	-0.5	1	Back-bias dependence of velocity saturation			
40	THESATG	V^{-1}	0	-0.5	_	Gate-bias dependence of velocity saturation			
			Satura	tion Volta	age Para	ameter			
41	AX	-	3	2	_	Linear/saturation transition factor			
		Chan	nel Length	Modula	tion (CI	LM) Parameters			
42	ALP	-	0.01	0	_	CLM pre-factor			
43	ALP1	V	0	0	_	CLM enhancement factor above threshold			
44	ALP2	V^{-1}	0	0	_	CLM enhancement factor below threshold			
45	VP	V	0.05	10^{-10}	_	CLM logarithmic dependence parameter			
			Impact I	onization	(II) Par	rameters			
46	A1	_	1	0	_	Impact-ionization pre-factor			
47	A2	V	10	0	_	Impact-ionization exponent at TR			
48	STA2	V	0	_	_	Temperature dependence of A2			
49	A3	_	1	0	_	Saturation-voltage dependence of II			
50	A4	$V^{-\frac{1}{2}}$	0	0	_	Back-bias dependence of II			
		ı		Current					
51	GCO	_	0	-10	10	Gate tunnelling energy adjustment			
52	IGINV	A	0	0	_	Gate channel current pre-factor			
53	IGOV	A	0	0	_	Gate overlap current pre-factor			
54	STIG	-	2	_	_	Temperature dependence of gate current			
55	GC2	_	0.375	0	10	Gate current slope factor			
56	GC3	_	0.063	-2	2	Gate current curvature factor			

 $continued \ on \ next \ page. \ . .$

... continued from previous page

No.	Name	Unit	Default	Min.	Max.	Description				
57	СНІВ	V	3.1	1	_	Tunnelling barrier height				
	Gate-Induced Drain Leakage (GIDL) Parameters									
58	58 AGIDL A/V ³ 0 0 — GIDL pre-factor									
59	BGIDL	V	41	0	_	GIDL probability factor at TR				
60	STBGIDL	V/K	0	_	_	Temperature dependence of BGIDL				
61	CGIDL	-	0	_	_	Back-bias dependence of GIDL				
	Charge Model Parameters									
62	COX	F	10^{-14}	0	_	Oxide capacitance for intrinsic channel				
63	CGOV	F	10^{-15}	0	_	Oxide capacitance for gate-drain/source				
						overlap				
64	CGBOV	F	0	0	_	Oxide capacitance for gate–bulk overlap				
65	CFR	F	0	0	_	Outer fringe capacitance				
			Nois	se Model	Parame	ters				
66	FNT	_	1.0	0	_	Thermal noise coefficient				
67	NFA	V^{-1}/m^4	$8 \cdot 10^{22}$	0	_	First coefficient of flicker noise				
68	NFB	V^{-1}/m^2	$3 \cdot 10^7$	0	_	Second coefficient of flicker noise				
69	69 NFC V^{-1} 0 0 — Third coefficient of flicker noise		Third coefficient of flicker noise							
Other Parameters										
70 DTA K 0 — Temperature offset w.r.t. ambient circ temperature										

2.5.7 Parameters for source-bulk and drain-bulk junction model

The JUNCAP2 parameters are part of both the global and the local parameter sets.

No.	Name	Unit	Default	Min.	Max.	Description					
0	TRJ	°C	21	$T_{ m min}$	_	Reference temperature					
1	IMAX	A	1000	10^{-12}	_	Maximum current up to which forward current behaves exponentially					
	Capacitance Parameters										
2	CJORBOT	F/m ²	10^{-3}	10^{-12}	_	Zero-bias capacitance per unit-of-area of bottom component					
3	CJORSTI	F/m	10^{-9}	10^{-18}	_	Zero-bias capacitance per unit-of-length of STI-edge component					
4	CJORGAT	F/m	10^{-9}	10^{-18}	_	Zero-bias capacitance per unit-of-length of gate-edge component					
5	VBIRBOT	V	1	$V_{ m bi,low}$	_	Built-in voltage at the reference temperature of bottom component					
6	VBIRSTI	V	1	$V_{ m bi,low}$	_	Built-in voltage at the reference temperature of STI-edge component					
7	VBIRGAT	V	1	$V_{ m bi,low}$	_	Built-in voltage at the reference temperature of gate-edge component					
8	PBOT	_	0.5	0.05	0.95	Grading coefficient of bottom component					
9	PSTI	_	0.5	0.05	0.95	Grading coefficient of STI-edge component					
10	PGAT	_	0.5	0.05	0.95	Grading coefficient of gate-edge component					
			Ideal-	current I	Paramet	ers					
11	PHIGBOT	V	1.16	_	_	Zero-temperature bandgap voltage of bottom component					
12	PHIGSTI	V	1.16		_	Zero-temperature bandgap voltage of STI-edge component					
13	PHIGGAT	V	1.16	_	_	Zero-temperature bandgap voltage of gate- edge component					
14	IDSATRBOT	A/m ²	10^{-12}	0	_	Saturation current density at the reference temperature of bottom component					
15	IDSATRSTI	A/m	10^{-18}	0	_	Saturation current density at the reference temperature of STI-edge component					
16	IDSATRGAT	A/m	10^{-18}	0	_	Saturation current density at the reference temperature of gate-edge component					
17	CSRHBOT	A/m ³	10^{2}	0	_	Shockley-Read-Hall prefactor of bottom component					
18	CSRHSTI	A/m ²	10^{-4}	0	_	Shockley-Read-Hall prefactor of STI-edge component					
19	CSRHGAT	A/m ²	10^{-4}	0	_	Shockley-Read-Hall prefactor of gate-edge component					
20	XJUNSTI	m	10^{-7}	10^{-9}	_	Junction depth of STI-edge component					
21	XJUNGAT	m	10^{-7}	10^{-9}	_	Junction depth of gate-edge component					

continued on next page...

... continued from previous page

No. 22	Name CTATBOT	Unit	Default	Min.	Max.	Description						
22	СТАТВОТ	r				I .						
22	СТАТВОТ	Trap-assisted Tunneling Parameters										
		A/m ³	10^{2}	0	_	Trap-assisted tunneling prefactor of bottom component						
23	CTATSTI	A/m ²	10^{-4}	0	_	Trap-assisted tunneling prefactor of STI-edge component						
24	CTATGAT	A/m ²	10^{-4}	0	_	Trap-assisted tunneling prefactor of gate- edge component						
25	MEFFTATBOT	_	0.25	.01	_	Effective mass (in units of m_0) for trapassisted tunneling of bottom component						
26	MEFFTATSTI	_	0.25	.01	_	Effective mass (in units of m_0) for trapassisted tunneling of STI-edge component						
27	MEFFTATGAT	-	0.25	.01	_	Effective mass (in units of m_0) for trapassisted tunneling of gate-edge component						
		I	Band-to-ba	nd Tunn	Leling Par	rameters						
28	СВВТВОТ	AV^{-3}	10^{-12}	0	_	Band-to-band tunneling prefactor of bot- tom component						
29	CBBTSTI	AV^{-3} m	10^{-18}	0	_	Band-to-band tunneling prefactor of STI- edge component						
30	CBBTGAT	$\mathrm{AV^{-3}m}$	10^{-18}	0	_	Band-to-band tunneling prefactor of gate edge component						
31	FBBTRBOT	Vm ⁻¹	109	_	_	Normalization field at the reference tem perature for band-to-band tunneling of bot tom component						
32	FBBTRSTI	Vm ⁻¹	109	_	_	Normalization field at the reference temperature for band-to-band tunneling of STI-edge component						
33	FBBTRGAT	Vm ⁻¹	10 ⁹	_	_	Normalization field at the reference temperature for band-to-band tunneling of gate-edge component						
34	STFBBTBOT	K^{-1}	-10^{-3}	_	_	Temperature scaling parameter for band- to-band tunneling of bottom component						
35	STFBBTSTI	K ⁻¹	-10^{-3}	_	_	Temperature scaling parameter for band- to-band tunneling of STI-edge component						
36	STFBBTGAT	K ⁻¹	-10^{-3}	-	_	Temperature scaling parameter for band- to-band tunneling of gate-edge component						
		A	valanche a	nd Break	down Pa	nrameters						
37	VBRBOT	V	10	0.1	_	Breakdown voltage of bottom component						
38	VBRSTI	V	10	0.1	_	Breakdown voltage of STI-edge component						
39	VBRGAT	V	10	0.1	_	Breakdown voltage of gate-edge component						

continued on next page...

... continued from previous page

No.	Name	Unit	Default	Min.	Max.	Description	
40	PBRBOT	V	4	0.1	_	Breakdown onset tuning parameter of bo tom component	
41	PBRSTI	V	4	0.1	_	Breakdown onset tuning parameter of STI edge component	
42	PBRGAT	V	4	0.1	_	Breakdown onset tuning parameter of gate- edge component	

Section 3

Geometry and Stress dependence

3.1 Introduction

The physical geometry scaling rules of PSP (Section 3.2) have been developed to give a good description over the whole geometry range of CMOS technologies. As an alternative, the binning-rules can be used (Section 3.3) to allow for a more phenomenological geometry dependency. (Note that the user has to choose between the two options; the geometrical scaling rules and the binning scaling rules cannot be used at the same time.) In both cases, the result is a local parameter set (for a transistor of the specified L and W), which is fed into the local model.

Use of the stress model (Section 3.4) leads to a stress-dependent modification of some of the local parameters calculated from the geometrical or binning scaling rules.

3.2 Geometrical scaling rules

The physical scaling rules to calculate the local parameters from a global parameter set are given in this section. **Note:** After calculation of the local parameters (and possible application of the stress equations in Section 3.4), clipping is applied according to Section 2.5.6.

Effective length and width

$$L_{\rm EN} = 10^{-6} \tag{3.1}$$

$$W_{\rm EN} = 10^{-6} \tag{3.2}$$

$$\Delta L_{\rm PS} = \mathbf{LVARO} \cdot \left(1 + \mathbf{LVARL} \cdot \frac{L_{\rm EN}}{L} \right) \cdot \left(1 + \mathbf{LVARW} \cdot \frac{W_{\rm EN}}{W} \right)$$
(3.3)

$$\Delta W_{\rm OD} = \mathbf{WVARO} \cdot \left(1 + \mathbf{WVARL} \cdot \frac{L_{\rm EN}}{L} \right) \cdot \left(1 + \mathbf{WVARW} \cdot \frac{W_{\rm EN}}{W} \right)$$
(3.4)

$$L_{\rm E} = L - \Delta L = L + \Delta L_{\rm PS} - 2 \cdot \text{LAP}$$
(3.5)

$$W_{\rm E} = W - \Delta W = W + \Delta W_{\rm OD} - 2 \cdot \mathbf{WOT} \tag{3.6}$$

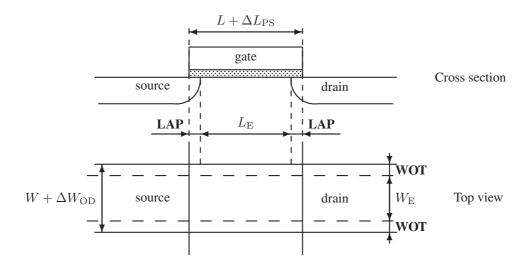


Figure 3.1: Specification of the dimensions of a MOS transistor

$$L_{\text{E.CV}} = L + \Delta L_{\text{PS}} - 2 \cdot \text{LAP} + \text{DLQ}$$
(3.7)

$$W_{\text{E,CV}} = W + \Delta W_{\text{OD}} - 2 \cdot \mathbf{WOT} + \mathbf{DWQ}$$
(3.8)

$$L_{G,CV} = L + \Delta L_{PS} + \mathbf{DLQ}$$
(3.9)

$$W_{G,CV} = W + \Delta W_{OD} + \mathbf{DWQ} \tag{3.10}$$

Note: If the calculated $L_{\rm E}$, $W_{\rm E}$, $L_{\rm E,CV}$, $W_{\rm E,CV}$, $L_{\rm G,CV}$, or $W_{\rm G,CV}$ is smaller than 1 nm (10⁻⁹ m), the value is clipped to this lower bound of 1 nm.

Process Parameters

$$\mathbf{VFB} = \mathbf{VFBO} \cdot \left(1 + \mathbf{VFBL} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}\right) \cdot \left(1 + \mathbf{VFBW} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}}\right)$$

$$\cdot \left(1 + \mathbf{VFBLW} \cdot \frac{W_{\mathrm{EN}} \cdot L_{\mathrm{EN}}}{W_{\mathrm{E}} \cdot L_{\mathrm{E}}}\right) \quad (3.11)$$

$$\mathbf{STVFB} = \mathbf{STVFBO} \cdot \left(1 + \mathbf{STVFBL} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}\right) \cdot \left(1 + \mathbf{STVFBW} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}}\right)$$

$$\cdot \left(1 + \mathbf{STVFBLW} \cdot \frac{W_{\mathrm{EN}} \cdot L_{\mathrm{EN}}}{W_{\mathrm{E}} \cdot L_{\mathrm{E}}}\right) \quad (3.12)$$

$$TOX = TOXO (3.13)$$

$$N_{\mathrm{sub0,eff}} = \mathbf{NSUBO} \cdot \mathbf{MAX} \left(\left[1 + \mathbf{NSUBW} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} \cdot \ln \left(1 + \frac{W_{\mathrm{E}}}{\mathbf{WSEG}} \right) \right], 10^{-3} \right)$$
 (3.14)

$$N_{\text{pck,eff}} = \text{NPCK} \cdot \text{MAX} \left(\left[1 + \text{NPCKW} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \cdot \ln \left(1 + \frac{W_{\text{E}}}{\text{WSEGP}} \right) \right], 10^{-3} \right)$$
(3.15)

$$L_{\text{pck,eff}} = \mathbf{LPCK} \cdot \text{MAX} \left(\left[1 + \mathbf{LPCKW} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \cdot \ln \left(1 + \frac{W_{\text{E}}}{\mathbf{WSEGP}} \right) \right], 10^{-3} \right)$$
(3.16)

$$a = 7.5 \cdot 10^{10} \tag{3.17}$$

$$b = \sqrt{N_{\text{sub0,eff}} + 0.5 \cdot N_{\text{pck,eff}}} - \sqrt{N_{\text{sub0,eff}}}$$
(3.18)

$$N_{\rm sub0,eff} + N_{\rm pck,eff} \cdot \left[2 - \frac{L_{\rm E}}{L_{\rm pck,eff}} \right] \qquad \text{for } L_{\rm E} < L_{\rm pck,eff}$$

$$N_{\rm sub0,eff} + N_{\rm pck,eff} \cdot \frac{L_{\rm pck,eff}}{L_{\rm E}} \qquad \text{for } L_{\rm pck,eff} \le L_{\rm E} \le 2 \cdot L_{\rm pck,eff}$$

$$\left[\sqrt{N_{\rm sub0,eff}} + a \cdot \ln \left(1 + 2 \cdot \frac{L_{\rm pck,eff}}{L_{\rm E}} \cdot \left[\exp \left(\frac{b}{a} \right) - 1 \right] \right) \right]^{2} \qquad \text{for } L_{\rm E} > 2 \cdot L_{\rm pck,eff}$$

$$(3.19)$$

$$\mathbf{NEFF} = N_{\text{sub}} \cdot \left(1 - \mathbf{FOL1} \cdot \frac{L_{\text{EN}}}{L_{\text{E}}} - \mathbf{FOL2} \cdot \left[\frac{L_{\text{EN}}}{L_{\text{E}}} \right]^2 \right)$$
(3.20)

$$VNSUB = VNSUBO (3.21)$$

$$NSLP = NSLPO (3.22)$$

$$DNSUB = DNSUBO (3.23)$$

$$\mathbf{DPHIB} = \left(\mathbf{DPHIBO} + \mathbf{DPHIBL} \cdot \left[rac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}
ight]^{\mathbf{DPHIBLEXP}}
ight)$$

$$\cdot \left(1 + \mathbf{DPHIBW} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}}\right) \cdot \left(1 + \mathbf{DPHIBLW} \cdot \frac{W_{\mathrm{EN}} \cdot L_{\mathrm{EN}}}{W_{\mathrm{E}} \cdot L_{\mathrm{E}}}\right) \quad (3.24)$$

$$\mathbf{NP} = \mathbf{NPO} \cdot \text{MAX} \left(10^{-6}, 1 + \mathbf{NPL} \cdot \frac{L_{\text{EN}}}{L_{\text{E}}} \right)$$
 (3.25)

$$\mathbf{CT} = \left(\mathbf{CTO} + \mathbf{CTL} \cdot \left[\frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}\right]^{\mathbf{CTLEXP}}\right) \cdot \left(1 + \mathbf{CTW} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}}\right)$$

$$\cdot \left(1 + \mathbf{CTLW} \cdot \frac{W_{\mathrm{EN}} \cdot L_{\mathrm{EN}}}{W_{\mathrm{E}} \cdot L_{\mathrm{E}}} \right) \quad (3.26)$$

$$TOXOV = TOXOVO (3.27)$$

$$NOV = NOVO (3.28)$$

DIBL Parameters

$$\mathbf{CF} = \mathbf{CFL} \cdot \left[\frac{L_{\text{EN}}}{L_{\text{E}}} \right]^{\mathbf{CFLEXP}} \cdot \left(1 + \mathbf{CFW} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \right)$$
(3.29)

$$\mathbf{CFB} = \mathbf{CFBO} \tag{3.30}$$

Mobility Parameters

$$F_{\beta 1,\text{eff}} = \mathbf{FBET1} \cdot \left(1 + \mathbf{FBET1W} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \right)$$
(3.31)

$$L_{\text{P1,eff}} = \mathbf{LP1} \cdot \text{MAX} \left(\left[1 + \mathbf{LP1W} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \right], 10^{-3} \right)$$
 (3.32)

$$G_{\mathrm{P,E}} = 1 + F_{\beta 1,\mathrm{eff}} \cdot \frac{L_{\mathrm{P1,eff}}}{L_{\mathrm{E}}} \cdot \left[1 - \exp\left(-\frac{L_{\mathrm{E}}}{L_{\mathrm{P1,eff}}}\right) \right]$$
(3.33)

$$+ \mathbf{FBET2} \cdot \frac{\mathbf{LP2}}{L_{\mathrm{E}}} \cdot \left[1 - \exp\left(-\frac{L_{\mathrm{E}}}{\mathbf{LP2}}\right)\right]$$

$$G_{\mathrm{W,E}} = 1 + \mathbf{BETW1} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{BETW2} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} \cdot \ln\left(1 + \frac{W_{\mathrm{E}}}{\mathbf{WBET}}\right)$$
(3.34)

$$\mathbf{BETN} = \frac{\mathbf{UO}}{G_{\text{P.E}}} \cdot \frac{W_{\text{E}}}{L_{\text{E}}} \cdot G_{\text{W,E}}$$
(3.35)

$$\mathbf{STBET} = \mathbf{STBETO} \cdot \left(1 + \mathbf{STBETL} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}\right) \cdot \left(1 + \mathbf{STBETW} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}}\right)$$

$$\cdot \left(1 + \textbf{STBETLW} \cdot \frac{W_{\text{EN}} \cdot L_{\text{EN}}}{W_{\text{E}} \cdot L_{\text{E}}}\right)$$

$$\mathbf{MUE} = \mathbf{MUEO} \cdot \left[1 + \mathbf{MUEW} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} \right]$$
 (3.36)

$$STMUE = STMUEO (3.37)$$

$$THEMU = THEMUO (3.38)$$

$$STTHEMU = STTHEMUO (3.39)$$

$$\mathbf{CS} = \left(\mathbf{CSO} + \mathbf{CSL} \cdot \left[\frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}\right]^{\mathbf{CSLEXP}}\right) \cdot \left(1 + \mathbf{CSW} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}}\right)$$

$$\cdot \left(1 + \mathbf{CSLW} \cdot \frac{W_{\mathrm{EN}} \cdot L_{\mathrm{EN}}}{W_{\mathrm{E}} \cdot L_{\mathrm{E}}}\right) \quad (3.40)$$

(3.41)

STCS = STCSO

$$\mathbf{XCOR} = \mathbf{XCORO} \cdot \left(1 + \mathbf{XCORL} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} \right) \cdot \left(1 + \mathbf{XCORW} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} \right)$$

$$\cdot \left(1 + \mathbf{XCORLW} \cdot \frac{W_{\text{EN}} \cdot L_{\text{EN}}}{W_{\text{E}} \cdot L_{\text{E}}}\right) \quad (3.42)$$

$$STXCOR = STXCORO (3.43)$$

$$\mathbf{FETA} = \mathbf{FETAO} \tag{3.44}$$

Series Resistance Parameters

$$\mathbf{RS} = \mathbf{RSW1} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \cdot \left[1 + \mathbf{RSW2} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \right]$$
(3.45)

$$STRS = STRSO (3.46)$$

$$RSB = RSBO (3.47)$$

$$RSG = RSGO (3.48)$$

Velocity Saturation Parameters

$$\begin{aligned} \textbf{THESAT} &= \left(\textbf{THESATO} + \textbf{THESATL} \cdot \frac{G_{\text{W,E}}}{G_{\text{P,E}}} \cdot \left[\frac{L_{\text{EN}}}{L_{\text{E}}} \right]^{\textbf{THESATLEXP}} \right) \\ & \cdot \left(1 + \textbf{THESATW} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \right) \cdot \left(1 + \textbf{THESATLW} \cdot \frac{W_{\text{EN}} \cdot L_{\text{EN}}}{W_{\text{E}} \cdot L_{\text{E}}} \right) \end{aligned} \tag{3.49}$$

 $\textbf{STTHESAT} = \textbf{STTHESATO} \cdot \left(1 + \textbf{STTHESATL} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}\right)$

$$\cdot \left(1 + \textbf{STTHESATW} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}}\right) \cdot \left(1 + \textbf{STTHESATLW} \cdot \frac{W_{\text{EN}} \cdot L_{\text{EN}}}{W_{\text{E}} \cdot L_{\text{E}}}\right) \quad (3.50)$$

$$THESATB = THESATBO (3.51)$$

$$THESATG = THESATGO (3.52)$$

Saturation Voltage Parameter

$$\mathbf{AX} = \frac{\mathbf{AXO}}{1 + \mathbf{AXL} \cdot \frac{L_{\text{EN}}}{L_{\text{E}}}}$$
(3.53)

Channel Length Modulation (CLM) Parameters

$$\mathbf{ALP} = \mathbf{ALPL} \cdot \left[\frac{L_{\text{EN}}}{L_{\text{E}}} \right]^{\mathbf{ALPLEXP}} \cdot \left(1 + \mathbf{ALPW} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \right)$$
(3.54)

$$\mathbf{ALP1} = \frac{\mathbf{ALP1L1} \cdot \left[\frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}\right]^{\mathbf{ALP1LEXP}}}{1 + \mathbf{ALP1L2} \cdot \left[\frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}\right]^{\mathbf{ALP1LEXP}+1}} \cdot \left(1 + \mathbf{ALP1W} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}}\right)$$
(3.55)

$$\mathbf{ALP2} = \frac{\mathbf{ALP2L1} \cdot \left[\frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}\right]^{\mathbf{ALP2LEXP}}}{1 + \mathbf{ALP2L2} \cdot \left[\frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}\right]^{\mathbf{ALP2LEXP}+1}} \cdot \left(1 + \mathbf{ALP2W} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}}\right)$$
(3.56)

$$\mathbf{VP} = \mathbf{VPO} \tag{3.57}$$

Impact Ionization (II) Parameters

$$\mathbf{A1} = \mathbf{A10} \cdot \left(1 + \mathbf{A1L} \cdot \frac{L_{\text{EN}}}{L_{\text{E}}} \right) \cdot \left(1 + \mathbf{A1W} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \right)$$
(3.58)

$$\mathbf{A2} = \mathbf{A20} \tag{3.59}$$

$$STA2 = STA2O (3.60)$$

$$\mathbf{A3} = \mathbf{A3O} \cdot \left(1 + \mathbf{A3L} \cdot \frac{L_{\text{EN}}}{L_{\text{E}}} \right) \cdot \left(1 + \mathbf{A3W} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \right)$$
(3.61)

$$\mathbf{A4} = \mathbf{A4O} \cdot \left(1 + \mathbf{A4L} \cdot \frac{L_{\text{EN}}}{L_{\text{E}}} \right) \cdot \left(1 + \mathbf{A4W} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} \right)$$
(3.62)

Gate Current Parameters

$$GCO = GCOO (3.63)$$

$$\mathbf{IGINV} = \mathbf{IGINVLW} \cdot \frac{W_{\text{E}} \cdot L_{\text{E}}}{W_{\text{EN}} \cdot L_{\text{EN}}}$$
(3.64)

$$\mathbf{IGOV} = \mathbf{IGOVW} \cdot \frac{W_{\text{E}} \cdot \mathbf{LOV}}{W_{\text{EN}} \cdot L_{\text{EN}}}$$
(3.65)

$$STIG = STIGO (3.66)$$

$$GC2 = GC2O (3.67)$$

$$GC3 = GC3O (3.68)$$

$$\mathbf{CHIB} = \mathbf{CHIBO} \tag{3.69}$$

Gate-Induced Drain Leakage (GIDL) Parameters

$$\mathbf{AGIDL} = \mathbf{AGIDLW} \cdot \frac{W_{\mathrm{E}} \cdot \mathbf{LOV}}{W_{\mathrm{EN}} \cdot L_{\mathrm{EN}}}$$
(3.70)

$$BGIDL = BGIDLO (3.71)$$

$$STBGIDL = STBGIDLO (3.72)$$

$$CGIDL = CGIDLO (3.73)$$

Charge Model Parameters

$$\mathbf{COX} = \epsilon_{\text{ox}} \cdot \frac{W_{\text{E,CV}} \cdot L_{\text{E,CV}}}{\mathbf{TOX}}$$
(3.74)

$$\mathbf{CGOV} = \epsilon_{ox} \cdot \frac{W_{E,CV} \cdot \mathbf{LOV}}{\mathbf{TOXOV}}$$
(3.75)

$$\mathbf{CGBOV} = \mathbf{CGBOVL} \cdot \frac{L_{G,CV}}{L_{EN}}$$
(3.76)

$$\mathbf{CFR} = \mathbf{CFRW} \cdot \frac{W_{G,CV}}{W_{EN}}$$
(3.77)

Noise Model Parameters

$$NFA = NFALW \cdot \frac{W_{EN} \cdot L_{EN}}{W_{E} \cdot L_{E}}$$
(3.78)

$$NFB = NFBLW \cdot \frac{W_{EN} \cdot L_{EN}}{W_{E} \cdot L_{E}}$$
(3.79)

$$NFC = NFCLW \cdot \frac{W_{EN} \cdot L_{EN}}{W_{E} \cdot L_{E}}$$
(3.80)

3.3 Binning equations

The binning equations are provided as a (phenomenological) alternative to the physical scaling equations for computing local parameters. The physical geometrical scaling rules have been developed to give a good description over the whole geometry range of CMOS technologies. For processes under development, however, it is sometimes useful to have more flexible scaling relations. In that case on could opt for a binning strategy, where the accuracy with geometry is mostly determined by the number of bins used. The physical scaling rules of Section 3.2 are generally not suitable for binning strategies, since they may result in discontinuities in local parameter values at the bin boundaries. Consequently, special binning geometrical scaling relations have been developed, which guarantee continuity of the resulting local model parameters at the bin boundaries.

Only four different types of binning scaling rules are used, which are based on first order developments of the geometrical scaling rules in terms of $L_{\rm E}$, $1/L_{\rm E}$, $W_{\rm E}$, and $1/W_{\rm E}$ (examples below are for a fictitious parameter YYY):

1. Type I

$$\mathbf{YYY} = \mathbf{POYYY} + \mathbf{PLYYY} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWYYY} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWYYY} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.81)

2. Type II

$$\mathbf{YYY} = \mathbf{POYYY} + \mathbf{PLYYY} \cdot \frac{L_{\mathrm{E}}}{L_{\mathrm{EN}}} + \mathbf{PWYYY} \cdot \frac{W_{\mathrm{E}}}{W_{\mathrm{EN}}} + \mathbf{PLWYYY} \cdot \frac{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}$$
(3.82)

3. Type III

$$\mathbf{YYY} = \mathbf{POYYY} + \mathbf{PLYYY} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWYYY} \cdot \frac{W_{\mathrm{E}}}{W_{\mathrm{EN}}} + \mathbf{PLWYYY} \cdot \frac{W_{\mathrm{E}} \cdot L_{\mathrm{EN}}}{W_{\mathrm{EN}} \cdot L_{\mathrm{E}}}$$
(3.83)

4. Type IV (no binning)

$$\mathbf{YYY} = \mathbf{POYYY} \tag{3.84}$$

In Table 3.1 a survey of the binning type used for each local parameter is given. In some cases where the geometrical scaling rule is constant, the binning rule is chosen to be more flexible.

When using the binning rules above, the binning parameters for one bin can be directly calculated from the local parameter sets of the four corner devices of the bin (see Sec. 7.6). This results in a *separate parameter set* for each bin. The binning scheme ensures that the local parameters are exactly reproduced at the bin corners and that no humps occur in the local parameter values across bin boundaries.

Note: After calculation of the local parameters from the binning rules (and possible application of the stress equations in Section 3.4), clipping is applied according to Section 2.5.6.

Table 3.1: Overview of local parameters and binning type. The third column indicates whether there is a physical geometrical scaling rule for the local parameters.

#	parameter	physical	binning	#	parameter	physical	binning
		scaling				scaling	
0	LEVEL	no	no	36	RSG	no	no
1	TYPE	no	no	37	THESAT	yes	type I
2	TR	no	no	38	STTHESAT	yes	type I
3	SWIGATE	no	no	39	THESATB	no	type I
4	SWIMPACT	no	no	40	THESATG	no	type I
5	SWGIDL	no	no	41	AX	yes	type I
6	SWJUNCAP	no	no	42	ALP	yes	type I
7	QMC	no	no	43	ALP1	yes	type I
8	VFB	yes	type I	44	ALP2	yes	type I
9	STVFB	yes	type I	45	VP	no	no
10	TOX	no	no	46	A1	yes	type I
11	NEFF	yes	type I	47	A2	no	no
12	VNSUB	no	no	48	STA2	no	no
13	NSLP	no	no	49	A3	yes	type I
14	DNSUB	no	no	50	A4	yes	type I
15	DPHIB	yes	type I	51	GCO	no	no
16	NP	yes	type I	52	IGINV	yes	type II
17	CT	yes	type I	53	IGOV	yes	type III
18	TOXOV	no	no	54	STIG	no	no
19	NOV	no	type I	55	GC2	no	no
20	CF	yes	type I	56	GC3	no	no
21	CFB	no	no	57	CHIB	no	no
22	BETN	yes	type III	58	AGIDL	yes	type III
23	STBET	yes	type I	59	BGIDL	no	no
24	MUE	yes	type I	60	STBGIDL	no	no
25	STMUE	no	no	61	CGIDL	no	no
26	THEMU	no	no	62	COX	yes	type II
27	STTHEMU	no	no	63	CGOV	yes	type III
28	CS	yes	type I	64	CGBOV	yes	type II
29	STCS	no	no	65	CFR	yes	type III
30	XCOR	yes	type I	66	FNT	no	no
31	STXCOR	no	no	67	NFA	yes	type I
32	FETA	no	no	68	NFB	yes	type I
33	RS	yes	type I	69	NFC	yes	type I
34	STRS	no	no	70	DTA	no	no
35	RSB	no	no				

Effective length and width

$$L_{\rm EN} = 10^{-6} \tag{3.85}$$

$$W_{\rm EN} = 10^{-6} \tag{3.86}$$

$$\Delta L_{\rm PS} = \mathbf{LVARO} \cdot \left(1 + \mathbf{LVARL} \cdot \frac{L_{\rm EN}}{L} \right)$$
 (3.87)

$$\Delta W_{\rm OD} = \mathbf{WVARO} \cdot \left(1 + \mathbf{WVARW} \cdot \frac{W_{\rm EN}}{W}\right)$$
(3.88)

$$L_{\rm E} = L - \Delta L = L + \Delta L_{\rm PS} - 2 \cdot \mathbf{LAP}$$
(3.89)

$$W_{\rm E} = W - \Delta W = W + \Delta W_{\rm OD} - 2 \cdot \text{WOT}$$
(3.90)

$$L_{E,CV} = L + \Delta L_{PS} - 2 \cdot LAP + DLQ$$
(3.91)

$$W_{E,CV} = W + \Delta W_{OD} - 2 \cdot \mathbf{WOT} + \mathbf{DWQ}$$
(3.92)

$$L_{G,CV} = L + \Delta L_{PS} + \mathbf{DLQ}$$
(3.93)

$$W_{G,GV} = W + \Delta W_{OD} + \mathbf{DWQ} \tag{3.94}$$

Note: If the calculated $L_{\rm E}$, $W_{\rm E}$, $L_{\rm E,CV}$, $W_{\rm E,CV}$, $L_{\rm G,CV}$, or $W_{\rm G,CV}$ is smaller than 1 nm (10⁻⁹ m), the value is clipped to this lower bound of 1 nm.

Process Parameters

$$\mathbf{VFB} = \mathbf{POVFB} + \mathbf{PLVFB} \cdot \frac{L_{\text{EN}}}{L_{\text{E}}} + \mathbf{PWVFB} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} + \mathbf{PLWVFB} \cdot \frac{L_{\text{EN}} \cdot W_{\text{EN}}}{L_{\text{E}} \cdot W_{\text{E}}}$$
(3.95)

$$\mathbf{STVFB} = \mathbf{POSTVFB} + \mathbf{PLSTVFB} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWSTVFB} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWSTVFB} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}} (3.96)$$

$$TOX = POTOX (3.97)$$

$$\mathbf{NEFF} = \mathbf{PONEFF} + \mathbf{PLNEFF} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWNEFF} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWNEFF} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.98)

$$VNSUB = POVNSUB$$
 (3.99)

$$NSLP = PONSLP (3.100)$$

$$DNSUB = PODNSUB (3.101)$$

$$\mathbf{DPHIB} = \mathbf{PODPHIB} + \mathbf{PLDPHIB} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWDPHIB} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWDPHIB} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}} (3.102)$$

$$\mathbf{NP} = \mathbf{PONP} + \mathbf{PLNP} \cdot \frac{L_{\text{EN}}}{L_{\text{E}}} + \mathbf{PWNP} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} + \mathbf{PLWNP} \cdot \frac{L_{\text{EN}} \cdot W_{\text{EN}}}{L_{\text{E}} \cdot W_{\text{E}}}$$
(3.103)

$$\mathbf{CT} = \mathbf{POCT} + \mathbf{PLCT} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWCT} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWCT} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.104)

$$TOXOV = POTOXOV (3.105)$$

$$\mathbf{NOV} = \mathbf{PONOV} + \mathbf{PLNOV} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWNOV} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWNOV} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.106)

DIBL Parameters

$$\mathbf{CF} = \mathbf{POCF} + \mathbf{PLCF} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWCF} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWCF} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.107)

$$\mathbf{CFB} = \mathbf{POCFB} \tag{3.108}$$

Mobility Parameters

$$\mathbf{BETN} = \mathbf{POBETN} + \mathbf{PLBETN} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWBETN} \cdot \frac{W_{\mathrm{E}}}{W_{\mathrm{EN}}} + \mathbf{PLWBETN} \cdot \frac{W_{\mathrm{E}} \cdot L_{\mathrm{EN}}}{W_{\mathrm{EN}} \cdot L_{\mathrm{E}}}$$
(3.109)

$$\mathbf{STBET} = \mathbf{POSTBET} + \mathbf{PLSTBET} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWSTBET} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWSTBET} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}} (3.110)$$

$$\mathbf{MUE} = \mathbf{POMUE} + \mathbf{PLMUE} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWMUE} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWMUE} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.111)

$$\mathbf{STMUE} = \mathbf{POSTMUE} \tag{3.112}$$

$$THEMU = POTHEMU (3.113)$$

$$STTHEMU = POSTTHEMU$$
 (3.114)

$$\mathbf{CS} = \mathbf{POCS} + \mathbf{PLCS} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWCS} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWCS} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.115)

$$STCS = POSTCS (3.116)$$

$$\mathbf{XCOR} = \mathbf{POXCOR} + \mathbf{PLXCOR} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWXCOR} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWXCOR} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}} \quad (3.117)$$

$$STXCOR = POSTXCOR (3.118)$$

$$\mathbf{FETA} = \mathbf{POFETA} \tag{3.119}$$

Series Resistance Parameters

$$\mathbf{RS} = \mathbf{PORS} + \mathbf{PLRS} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWRS} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWRS} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.120)

$$STRS = POSTRS \tag{3.121}$$

$$RSB = PORSB \tag{3.122}$$

$$RSG = PORSG \tag{3.123}$$

Velocity Saturation Parameters

 $\mathbf{THESAT} = \mathbf{POTHESAT} + \mathbf{PLTHESAT} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}$

$$+ \mathbf{PWTHESAT} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWTHESAT} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}} \quad (3.124)$$

 $\mathbf{STTHESAT} = \mathbf{POSTTHESAT} + \mathbf{PLSTTHESAT} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}$

+ PWSTTHESAT ·
$$\frac{W_{\rm EN}}{W_{\rm E}}$$
 + PLWSTTHESAT · $\frac{L_{\rm EN} \cdot W_{\rm EN}}{L_{\rm E} \cdot W_{\rm E}}$ (3.125)

 $\mathbf{THESATB} = \mathbf{POTHESATB} + \mathbf{PLTHESATB} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}$

$$+ \mathbf{PWTHESATB} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWTHESATB} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}} \quad (3.126)$$

 $\mathbf{THESATG} = \mathbf{POTHESATG} + \mathbf{PLTHESATG} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}$

+ PWTHESATG
$$\cdot \frac{W_{\text{EN}}}{W_{\text{E}}}$$
 + PLWTHESATG $\cdot \frac{L_{\text{EN}} \cdot W_{\text{EN}}}{L_{\text{E}} \cdot W_{\text{E}}}$ (3.127)

Saturation Voltage Parameters

$$\mathbf{AX} = \mathbf{POAX} + \mathbf{PLAX} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWAX} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWAX} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.128)

Channel Length Modulation (CLM) Parameters

$$\mathbf{ALP} = \mathbf{POALP} + \mathbf{PLALP} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWALP} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWALP} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.129)

$$\mathbf{ALP1} = \mathbf{POALP1} + \mathbf{PLALP1} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWALP1} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWALP1} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}} \tag{3.130}$$

$$\mathbf{ALP2} = \mathbf{POALP2} + \mathbf{PLALP2} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWALP2} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWALP2} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.131)

$$\mathbf{VP} = \mathbf{POVP} \tag{3.132}$$

Impact Ionization (II) Parameters

$$\mathbf{A1} = \mathbf{POA1} + \mathbf{PLA1} \cdot \frac{L_{\text{EN}}}{L_{\text{E}}} + \mathbf{PWA1} \cdot \frac{W_{\text{EN}}}{W_{\text{E}}} + \mathbf{PLWA1} \cdot \frac{L_{\text{EN}} \cdot W_{\text{EN}}}{L_{\text{E}} \cdot W_{\text{E}}}$$
(3.133)

$$\mathbf{A2} = \mathbf{POA2} \tag{3.134}$$

$$STA2 = POSTA2 \tag{3.135}$$

$$\mathbf{A3} = \mathbf{POA3} + \mathbf{PLA3} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWA3} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWA3} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.136)

$$\mathbf{A4} = \mathbf{POA4} + \mathbf{PLA4} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWA4} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWA4} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.137)

Gate Current Parameters

$$GCO = POGCO (3.138)$$

 $\mathbf{IGINV} = \mathbf{POIGINV} + \mathbf{PLIGINV} \cdot \frac{L_{\mathrm{E}}}{L_{\mathrm{EN}}}$

+ PWIGINV
$$\cdot \frac{W_{\rm E}}{W_{\rm EN}}$$
 + PLWIGINV $\cdot \frac{L_{\rm E} \cdot W_{\rm E}}{L_{\rm EN} \cdot W_{\rm EN}}$ (3.139)

$$\mathbf{IGOV} = \mathbf{POIGOV} + \mathbf{PLIGOV} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWIGOV} \cdot \frac{W_{\mathrm{E}}}{W_{\mathrm{EN}}} + \mathbf{PLWIGOV} \cdot \frac{W_{\mathrm{E}} \cdot L_{\mathrm{EN}}}{W_{\mathrm{EN}} \cdot L_{\mathrm{E}}}$$
(3.140)

$$STIG = POSTIG (3.141)$$

$$GC2 = POGC2 (3.142)$$

$$GC3 = POGC3 \tag{3.143}$$

$$\mathbf{CHIB} = \mathbf{POCHIB} \tag{3.144}$$

Gate-Induced Drain Leakage (GIDL) Parameters

 $\mathbf{AGIDL} = \mathbf{POAGIDL} + \mathbf{PLAGIDL} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}}$

$$+$$
 PWAGIDL $\cdot \frac{W_{\mathrm{E}}}{W_{\mathrm{EN}}}$ $+$ **PLWAGIDL** $\cdot \frac{W_{\mathrm{E}} \cdot L_{\mathrm{EN}}}{W_{\mathrm{EN}} \cdot L_{\mathrm{E}}}$ (3.145)

$$BGIDL = POBGIDL (3.146)$$

$$STBGIDL = POSTBGIDL \tag{3.147}$$

$$\mathbf{CGIDL} = \mathbf{POCGIDL} \tag{3.148}$$

Charge Model Parameters

$$\mathbf{COX} = \mathbf{POCOX} + \mathbf{PLCOX} \cdot \frac{L_{\mathrm{E,CV}}}{L_{\mathrm{EN}}} + \mathbf{PWCOX} \cdot \frac{W_{\mathrm{E,CV}}}{W_{\mathrm{EN}}} + \mathbf{PLWCOX} \cdot \frac{L_{\mathrm{E,CV}} \cdot W_{\mathrm{E,CV}}}{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}$$
(3.149)

$$\mathbf{CGOV} = \mathbf{POCGOV} + \mathbf{PLCGOV} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E,CV}}}$$

+ **PWCGOV** ·
$$\frac{W_{\text{E,CV}}}{W_{\text{EN}}}$$
 + **PLWCGOV** · $\frac{W_{\text{E,CV}} \cdot L_{\text{EN}}}{W_{\text{EN}} \cdot L_{\text{E,CV}}}$ (3.150)

$$\mathbf{CGBOV} = \mathbf{POCGBOV} + \mathbf{PLCGBOV} \cdot \frac{L_{\mathrm{G,CV}}}{L_{\mathrm{EN}}}$$

$$+ \mathbf{PWCGBOV} \cdot \frac{W_{\mathrm{G,CV}}}{W_{\mathrm{EN}}} + \mathbf{PLWCGBOV} \cdot \frac{L_{\mathrm{G,CV}} \cdot W_{\mathrm{G,CV}}}{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}} \quad (3.151)$$

$$\mathbf{CFR} = \mathbf{POCFR} + \mathbf{PLCFR} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{G,CV}}} + \mathbf{PWCFR} \cdot \frac{W_{\mathrm{G,CV}}}{W_{\mathrm{EN}}} + \mathbf{PLWCFR} \cdot \frac{W_{\mathrm{G,CV}} \cdot L_{\mathrm{EN}}}{W_{\mathrm{EN}} \cdot L_{\mathrm{G,CV}}}$$
(3.152)

Noise Model Parameters

$$\mathbf{FNT} = \mathbf{POFNT} \tag{3.153}$$

$$\mathbf{NFA} = \mathbf{PONFA} + \mathbf{PLNFA} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWNFA} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWNFA} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.154)

$$\mathbf{NFB} = \mathbf{PONFB} + \mathbf{PLNFB} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWNFB} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWNFB} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.155)

$$\mathbf{NFC} = \mathbf{PONFC} + \mathbf{PLNFC} \cdot \frac{L_{\mathrm{EN}}}{L_{\mathrm{E}}} + \mathbf{PWNFC} \cdot \frac{W_{\mathrm{EN}}}{W_{\mathrm{E}}} + \mathbf{PLWNFC} \cdot \frac{L_{\mathrm{EN}} \cdot W_{\mathrm{EN}}}{L_{\mathrm{E}} \cdot W_{\mathrm{E}}}$$
(3.156)

3.4 Parameter modification due to stress effects

The stress model of BSIM4.4.0 [2] has been adopted in PSP without any modifications, except for two changes: (1) in the original BSIM parameter names all zeros have been replaced by "O"s, in order to comply with PSP conventions and (2) the BSIM parameters *STK2* and *LODK2* are not available in PSP.

The local PSP parameters affected by the stress equations are BETN, THESAT, VFB, and CF.

Note: After modification of the local parameters by the stress equations, clipping is applied according to Section 2.5.6.

Note: If both **SA** and **SB** are set to 0, the stress-equations are *not* computed.

3.4.1 Layout effects for regular shapes

$$R_{\mathbf{A}} = \frac{1}{\mathbf{S}\mathbf{A} + 0.5 \cdot L} \tag{3.157}$$

$$R_{\rm B} = \frac{1}{\mathbf{SB} + 0.5 \cdot L} \tag{3.158}$$

$$R_{\text{A,ref}} = \frac{1}{\text{SAREF} + 0.5 \cdot L} \tag{3.159}$$

$$R_{\text{B,ref}} = \frac{1}{\text{SBREF} + 0.5 \cdot L} \tag{3.160}$$

3.4.2 Layout effects for irregular shapes

For irregular shapes the following effective values for SA and SB are to be used.

$$\frac{1}{\mathbf{S}\mathbf{A}_{\text{eff}} + 0.5 \cdot L} = \sum_{i=1}^{n} \frac{\mathbf{S}\mathbf{W}_{i}}{W} \cdot \frac{1}{\mathbf{S}\mathbf{A}_{i} + 0.5 \cdot L}$$
(3.161)

$$\frac{1}{\mathbf{SB}_{\text{eff}} + 0.5 \cdot L} = \sum_{i=1}^{n} \frac{\mathbf{SW}_i}{W} \cdot \frac{1}{\mathbf{SB}_i + 0.5 \cdot L}$$
(3.162)

Note: These values have to be supplied *manually* or by a layout extraction tool!

3.4.3 Calculation of parameter modifications

Mobility-related equations

$$\begin{split} K_{\text{u0}} &= \left(1 + \frac{\textbf{LKUO}}{\left(L + \Delta L_{\text{PS}}\right)^{\textbf{LLODKUO}}} + \frac{\textbf{WKUO}}{\left(W + \Delta W_{\text{OD}} + \textbf{WLOD}\right)^{\textbf{WLODKUO}}} \right. \\ &\quad \left. + \frac{\textbf{PKUO}}{\left(L + \Delta L_{\text{PS}}\right)^{\textbf{LLODKUO}} \cdot \left(W + \Delta W_{\text{OD}} + \textbf{WLOD}\right)^{\textbf{WLODKUO}}} \right) \\ &\quad \left. \cdot \left[1 + \textbf{TKUO} \cdot \left(\frac{T_{\text{KD}}}{T_{\text{KR}}} - 1\right)\right] \quad (3.163) \end{split}$$

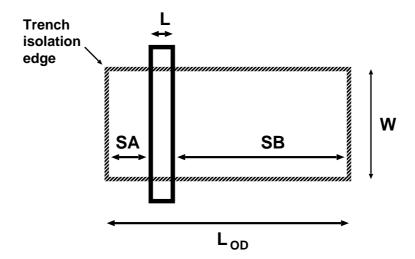


Figure 3.2: Typical layout of a MOSFET. Note that $L_{\rm OD} = {\bf SA} + {\bf SB} + L$, where OD is the active region definition.

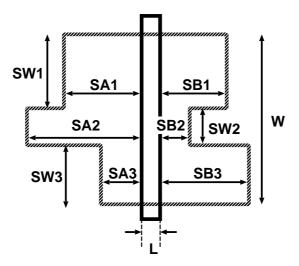


Figure 3.3: A typical layout of MOS devices with more instance parameters $(SW_i, SA_i \text{ and } SB_i)$ in addition to the traditional L and W.

$$\rho_{\beta} = \frac{\text{KUO}}{K_{\text{H0}}} \cdot (R_{\text{A}} + R_{\text{B}}) \tag{3.164}$$

$$\rho_{\beta,\text{ref}} = \frac{\text{KUO}}{K_{\text{u0}}} \cdot (R_{\text{A,ref}} + R_{\text{B,ref}}) \tag{3.165}$$

$$\mathbf{BETN} = \frac{1 + \rho_{\beta}}{1 + \rho_{\beta,\text{ref}}} \cdot \mathbf{BETN}_{\text{ref}}$$
(3.166)

$$\mathbf{THESAT} = \frac{1 + \rho_{\beta}}{1 + \rho_{\beta, ref}} \cdot \frac{1 + \mathbf{KVSAT} \cdot \rho_{\beta, ref}}{1 + \mathbf{KVSAT} \cdot \rho_{\beta}} \cdot \mathbf{THESAT}_{ref}$$
(3.167)

Threshold-voltage-related equations

$$K_{\rm vth0} = 1 + \frac{\mathbf{LKVTHO}}{\left(L + \Delta L_{\rm PS}\right)^{\mathbf{LLODVTH}}} + \frac{\mathbf{WKVTHO}}{\left(W + \Delta W_{\rm OD} + \mathbf{WLOD}\right)^{\mathbf{WLODVTH}}}$$

+
$$\frac{\mathbf{PKVTHO}}{(L + \Delta L_{PS})^{\mathbf{LLODVTH}} \cdot (W + \Delta W_{OD} + \mathbf{WLOD})^{\mathbf{WLODVTH}}}$$
 (3.168)

$$\Delta R = R_{\rm A} + R_{\rm B} - R_{\rm A,ref} - R_{\rm B,ref} \tag{3.169}$$

$$\mathbf{VFB} = \mathbf{VFB}_{ref} + \mathbf{KVTHO} \cdot \frac{\Delta R}{K_{vth0}}$$
(3.170)

$$\mathbf{CF} = \mathbf{CF}_{\text{ref}} + \mathbf{STETAO} \cdot \frac{\Delta R}{K_{\text{vth0}}^{\mathbf{LODETAO}}}$$
(3.171)

Section 4

PSP Model Equations

4.1 Internal Parameters (including Temperature Scaling)

In this section, bias-independent internal parameters will be calculated, including temperature scaling. These parameters are computed from local parameters. Local parameters are (as usual) denoted by capital characters in bold font, whereas the internal parameters are denoted by symbols in bold font.

Transistor temperature

$$T_{\rm KR} = T_0 + \mathbf{TR} \tag{4.1}$$

$$T_{\rm KD} = T_0 + T_{\rm A} + \mathbf{DTA} \tag{4.2}$$

$$\Delta T = T_{\rm KD} - T_{\rm KR} \tag{4.3}$$

$$\phi_{\mathbf{T}} = \frac{k_{\mathbf{B}} \cdot T_{\mathbf{KD}}}{q} \tag{4.4}$$

Local process parameters

$$\phi_{\mathbf{T}}^* = \phi_{\mathbf{T}} \cdot \left(1 + \mathbf{CT} \cdot \frac{T_{KR}}{T_{KD}} \right) \tag{4.5}$$

$$V_{\rm FB} = VFB + STVFB \cdot \Delta T \tag{4.6}$$

$$E_{\rm g}/q = 1.179 - 9.025 \cdot 10^{-5} \cdot T_{\rm KD} - 3.05 \cdot 10^{-7} \cdot T_{\rm KD}^{2}$$
 (4.7)

$$r_{\rm T} = (1.045 + 4.5 \cdot 10^{-4} \cdot T_{\rm KD}) \cdot (0.523 + 1.4 \cdot 10^{-3} \cdot T_{\rm KD} - 1.48 \cdot 10^{-6} \cdot T_{\rm KD}^{2})$$
(4.8)

$$n_{\rm i} = 2.5 \cdot 10^{25} \cdot r_{\rm T}^{3/4} \cdot (T_{\rm KD}/300)^{3/2} \cdot \exp\left(-\frac{E_{\rm g}/q}{2 \cdot \phi_{\rm T}}\right)$$
 (4.9)

$$\phi_{\mathrm{B}}^{\mathrm{cl}} = \mathrm{MAX}\left(\mathbf{DPHIB} + 2 \cdot \phi_{\mathbf{T}} \cdot \ln\left[\mathbf{NEFF}/n_{\mathrm{i}}\right], 0.05\right)$$
 (4.10)

$$C_{\rm ox} = \epsilon_{\rm ox}/{\rm TOX}$$
 (4.11)

$$\gamma_0 = \sqrt{2 \cdot q \cdot \epsilon_{\rm Si} \cdot \text{NEFF}} / C_{\rm ox}$$
 (4.12)

$$G_0^{\rm cl} = \gamma_0 / \sqrt{\phi_{\rm T}} \tag{4.13}$$

Polysilicon depletion parameter

$$\mathbf{k}_{\mathbf{P}} = \begin{cases} \text{if } \mathbf{NP} = 0 & \begin{cases} \mathbf{k}_{\mathbf{P}} = 0 \\ \\ \text{if } \mathbf{NP} > 0 \end{cases} & \begin{cases} \text{NP}_{1} = \text{MAX}(\mathbf{NP}, 8 \cdot 10^{7} / \mathbf{TOX}^{2}) \\ \\ \text{NP}_{2} = \text{MAX}(\text{NP}_{1}, 3 \cdot 10^{25}) \\ \\ \mathbf{k}_{\mathbf{P}} = 2 \cdot \phi_{\mathbf{T}} \cdot C_{\text{ox}}^{2} / (q \cdot \epsilon_{\text{Si}} \cdot \text{NP}_{2}) \end{cases}$$

$$(4.14)$$

Quantum-mechanical correction parameters

$$q_{\lim} = 10 \cdot \phi_{\mathrm{T}} \tag{4.15}$$

$$\boldsymbol{q}_{\mathbf{q}} = \begin{cases} 0.4 \cdot \mathbf{QMC} \cdot QM_{\mathrm{N}} \cdot C_{\mathrm{ox}}^{2/3} & \text{for NMOS} \\ \\ 0.4 \cdot \mathbf{QMC} \cdot QM_{\mathrm{P}} \cdot C_{\mathrm{ox}}^{2/3} & \text{for PMOS} \end{cases}$$

$$(4.16)$$

$$q_{\rm b0} = \gamma_0 \cdot \sqrt{\phi_{\rm B}^{\rm cl}} \tag{4.17}$$

$$\phi_{\mathbf{B}} = \phi_{\mathbf{B}}^{\text{cl}} + 0.75 \cdot q_{\mathbf{q}} \cdot q_{\mathbf{b}0}^{2/3} \tag{4.18}$$

$$G_0 = G_0^{\text{cl}} \cdot \left(1 + q_q \cdot q_{\text{b0}}^{-1/3} \right) \tag{4.19}$$

$V_{ m SB}$ -clipping parameters

$$\phi_{\mathbf{X}} = 0.95 \cdot \phi_{\mathbf{R}} \tag{4.20}$$

$$\boldsymbol{a}_{\phi} = 2.5 \cdot 10^{-3} \cdot \boldsymbol{\phi}_{\mathbf{B}}^2 \tag{4.21}$$

$$\boldsymbol{b}_{\phi} = 2.5 \cdot 10^{-3} \cdot \boldsymbol{\phi}_{\mathbf{B}}^2 \tag{4.22}$$

$$\phi_{\mathbf{X}}^{\star} = 0.5 \cdot \sqrt{b_{\phi}} \tag{4.23}$$

$$\boldsymbol{\phi}_{\mathbf{X}}^* = \text{MINA} \left(\boldsymbol{\phi}_{\mathbf{X}} - \boldsymbol{\phi}_{\mathbf{X}}^*, 0, \boldsymbol{a}_{\boldsymbol{\phi}} \right) \tag{4.24}$$

Local process parameters in gate overlap regions

$$\gamma_{\rm ov} = \sqrt{2 \cdot q \cdot \epsilon_{\rm Si} \cdot \text{NOV}} \cdot \text{TOXOV} / \epsilon_{\rm ox}$$
(4.25)

$$G_{
m ov} = \gamma_{
m ov} / \sqrt{\phi_{
m T}}$$
 (4.26)

$$\boldsymbol{\xi_{ov}} = 1 + \boldsymbol{G_{ov}} / \sqrt{2} \tag{4.27}$$

$$x_{\text{mrgov}} = 10^{-5} \cdot \xi_{\text{ov}} \tag{4.28}$$

Mobility parameters

$$\beta = \mathbf{BETN} \cdot C_{\text{ox}} \cdot (T_{\text{KR}}/T_{\text{KD}})^{\mathbf{STBET}}$$
(4.29)

$$\theta_{\mu} = \text{THEMU} \cdot (T_{\text{KR}}/T_{\text{KD}})^{\text{STTHEMU}}$$
 (4.30)

$$\mu_{\rm E} = {\rm MUE} \cdot (T_{\rm KR}/T_{\rm KD})^{\rm STMUE} \tag{4.31}$$

$$X_{cor} = XCOR \cdot (T_{KR}/T_{KD})^{STXCOR}$$
 (4.32)

$$C_{S} = CS \cdot (T_{KR}/T_{KD})^{STCS}$$
(4.33)

$$\boldsymbol{E}_{\text{eff0}} = 10^{-8} \cdot C_{\text{ox}} / \epsilon_{\text{Si}} \tag{4.34}$$

$$\eta_{\mu} = \begin{cases} 1/2 \cdot \mathbf{FETA} & \text{for NMOS} \\ \\ 1/3 \cdot \mathbf{FETA} & \text{for PMOS} \end{cases}$$
 (4.35)

Series resistance parameter

$$R_{\rm s} = \mathbf{RS} \cdot (T_{\rm KR}/T_{\rm KD})^{\rm STRS} \tag{4.36}$$

$$\theta_{\mathbf{R}} = 2 \cdot \boldsymbol{\beta} \cdot R_{\mathbf{s}} \tag{4.37}$$

Velocity saturation parameter

$$\theta_{\text{sat}} = \text{THESAT} \cdot (T_{\text{KR}}/T_{\text{KD}})^{\text{STTHESAT}}$$
 (4.38)

Impact-ionization parameter

$$a_2 = \mathbf{A2} \cdot (T_{\mathrm{KD}}/T_{\mathrm{KR}})^{\mathbf{STA2}} \tag{4.39}$$

Gate current parameters

$$I_{\text{GINV}} = \text{IGINV} \cdot (T_{\text{KD}}/T_{\text{KR}})^{\text{STIG}}$$
 (4.40)

$$I_{GOV} = IGOV \cdot (T_{KD}/T_{KR})^{STIG}$$
 (4.41)

$$\boldsymbol{B} = \frac{4}{3} \cdot \frac{\mathbf{TOX}}{\hbar} \cdot \sqrt{2 \cdot q \cdot m_0 \cdot \mathbf{CHIB}} = 6.830909 \cdot 10^9 \cdot \mathbf{TOX} \cdot \sqrt{\mathbf{CHIB}}$$
(4.42)

$$B_{ov} = B \cdot TOXOV/TOX \tag{4.43}$$

$$GC_{\mathbf{Q}} = \begin{cases} -0.99 \cdot \frac{\mathbf{GC2}}{2 \cdot \mathbf{GC3}} & \text{for } \mathbf{GC3} < 0 \\ 0 & \text{for } \mathbf{GC3} \ge 0 \end{cases}$$

$$(4.44)$$

$$\alpha_{\mathbf{b}} = \frac{E_{\mathbf{g}}/q + \phi_{\mathbf{B}}}{2} \tag{4.45}$$

$$D_{\rm ch} = GCO \cdot \phi_{\rm T}^* \tag{4.46}$$

$$D_{\text{ov}} = \text{GCO} \cdot \phi_{\text{T}} \tag{4.47}$$

Gate-induced drain leakage parameters

$$A_{GIDL} = AGIDL \cdot \left(\frac{2 \cdot 10^{-9}}{TOXOV}\right)^2 \tag{4.48}$$

$$\boldsymbol{B_{\text{GIDL}}} = \mathbf{BGIDL} \cdot \text{MAX} \left(\left[1 + \mathbf{STBGIDL} \cdot \Delta T \right], 0 \right) \cdot \left(\frac{\mathbf{TOXOV}}{2 \cdot 10^{-9}} \right)$$
(4.49)

Noise parameter

$$N_{\rm T} = FNT \cdot 4 \cdot k_{\rm B} \cdot T_{\rm KD} \tag{4.50}$$

Additional internal parameters

$$x_1 = 1.25 (4.51)$$

$$x_{g1} = x_1 + G_{ov} \cdot \sqrt{\exp(-x_1) + x_1 - 1}$$
 (4.52)

4.2 Model Equations

In this section, the model equations of the PSP-model are given. Use is made of the applied terminal bias values $V_{\rm GS}$, $V_{\rm DS}$ and $V_{\rm SB}$, the local parameters listed in Section 2.5.6 and the internal parameters introduced in Section 4.1. Local parameters are denoted by capital characters in bold font, whereas internal (bias-independent) parameters are denoted by symbols in bold font.

The definitions of the auxiliary functions MINA(.), MAXA(.), $\chi(.)$ and $\sigma_{1,2}(.)$ can be found in Appendix A.

4.2.1 Conditioning of Terminal Voltages

$$\phi_{V} = MINA (V_{SB}, V_{SB} + V_{DS}, \boldsymbol{b}_{\boldsymbol{\phi}}) + \boldsymbol{\phi}_{\mathbf{X}}$$

$$(4.53)$$

$$V_{\mathrm{SB}}^{*} = V_{\mathrm{SB}} - \mathrm{MINA}\left(\phi_{\mathrm{V}}, 0, \boldsymbol{a}_{\boldsymbol{\phi}}\right) + \boldsymbol{\phi}_{\mathbf{X}}^{*} \tag{4.54}$$

$$V_{\rm DB}^* = V_{\rm DS} + V_{\rm SB}^* \tag{4.55}$$

$$V_{\rm dsx} = \sqrt{V_{\rm DS}^2 + 0.01} - 0.1 \tag{4.56}$$

$$V_{\rm sbx} = V_{\rm SB}^* + \frac{V_{\rm DS} - V_{\rm dsx}}{2} \tag{4.57}$$

Drain-induced barrier lowering:

$$\Delta V_{\rm G} = \mathbf{CF} \cdot V_{\rm dsx} \cdot (1 + \mathbf{CFB} \cdot V_{\rm sbx}) \tag{4.58}$$

$$V_{\rm GB}^* = V_{\rm GS} + V_{\rm SB}^* + \Delta V_{\rm G} - V_{\rm FB} \tag{4.59}$$

$$x_{\rm g} = V_{\rm GB}^* / \phi_{\rm T}^* \tag{4.60}$$

4.2.2 Bias-Dependent Body Factor

$$D_{\text{nsub}} = \mathbf{DNSUB} \cdot \text{MAXA} (0, V_{\text{GS}} + V_{\text{SB}} - \mathbf{VNSUB}, \mathbf{NSLP})$$
(4.61)

$$G = G_0 \cdot \sqrt{1 + D_{\text{nsub}}} \tag{4.62}$$

4.2.3 Surface Potential at Source Side and Related Variables

$$\xi = 1 + G/\sqrt{2} \tag{4.63}$$

$$x_{\rm ns} = \frac{\phi_{\rm B} + V_{\rm SB}^*}{\phi_{\rm T}^*} \tag{4.64}$$

$$\Delta_{\rm ns} = \exp\left(-x_{\rm ns}\right) \tag{4.65}$$

$$x_{\rm mrg} = 10^{-5} \cdot \xi$$
 (4.66)

$$\begin{aligned} & y_{\rm g} = -x_{\rm g} \\ & z = 1.25 \cdot y_{\rm g}/\xi \\ & \eta = \left[z + 10 - \sqrt{(z - 6)^2 + 64}\right]/2 \\ & a = (y_{\rm g} - \eta) - G^2 \\ & \tau = -\eta + \ln{(a/G^2)} \\ & y_0 = \sigma_1(a, c, \tau, \eta) \\ & \Delta_0 = \exp{(y_0)} \\ & p = 2 \cdot (y_{\rm g} - y_0) + G^2 \cdot \left[\Delta_0 - 1 + \Delta_{\rm ns} \cdot (1 - \chi'(y_0) - 1/\Delta_0)\right] \\ & q - (y_{\rm g} - y_0)^2 + G^2 \cdot \left[y_0 - \Delta_0 + 1 + \Delta_{\rm ns} \cdot (1 + \chi(y_0) - 1/\Delta_0 - 2 \cdot y_0)\right] \\ & x_{\rm s} = -y_0 - \frac{2 \cdot \eta}{p + \sqrt{p^2 - 2 \cdot \eta} \cdot \{2 - G^2 \cdot \left[\Delta_0 + \Delta_{\rm us} \cdot (1/\Delta_0 - \chi''(y_0))\right]\}} \end{aligned}$$
 (4.68)
if $|x_{\rm g}| \le x_{\rm mag} \left\{ \begin{array}{l} x_{\rm g} = \frac{x_{\rm g}}{\xi} \cdot \left[1 + G \cdot x_{\rm g} \cdot \frac{1 - \Delta_{\rm ns}}{\xi^2 \cdot 6 \cdot \sqrt{2}}\right] \\ & \left[\frac{2 \cdot \eta}{\xi} + \frac{x_{\rm g}}{\xi} \cdot \left[1 + x_{\rm g} \cdot (\xi \cdot x_{\rm g} - x_{\rm g})/\hat{x}_{\rm g}^2\right] \\ & x_0 = x_{\rm g} + G^2/2 - G \cdot \sqrt{x_{\rm g} + G^2/4 - 1 + \exp(-\bar{x})} \\ & b_{\chi} = x_{\rm ns} + 3 \\ & \eta = {\rm MINA}(x_0, b_{\chi}, 5) - \left(b_{\chi} - \sqrt{b_{\tilde{\chi}}^2 + 5}\right)/2 \\ & a = (x_{\tilde{g}} - \eta)^2 - G^2 \cdot \left[\exp(-\eta) - \Delta_{\rm ns} \cdot (\eta + 1 + \chi(\eta))\right] \\ & b = 1 - G^2/2 \cdot \left[\exp(-\eta) - \Delta_{\rm ns} \cdot \chi''(\eta)\right] \\ & c = 2 \cdot (x_{\tilde{g}} - \eta) + G^2 \cdot \left[1 - \exp(-\eta) - \Delta_{\rm ns} \cdot (1 + \chi'(\eta))\right] \\ & \tau = x_{\rm ns} - \eta + \ln{(a/G^2)} \\ & y_0 = \sigma_2(a, b, c, \tau, \eta) \\ & \Delta_0 = \exp{(y_0)} \\ & p = 2 \cdot (x_{\tilde{g}} - \eta_0) + G^2 \cdot \left[1 - 1/\Delta_0 + \Delta_{\rm ns} \cdot (\Delta_0 - 1 - \chi'(y_0))\right] \\ & q = (x_{\tilde{g}} - y_0)^2 - G^2 \cdot \left[y_0 + 1/\Delta_0 - 1 + \Delta_{\rm ns} \cdot (\Delta_0 - y_0 - 1 - \chi(y_0))\right] \\ & x_{\tilde{g}} = y_0 + \frac{2 \cdot \eta}{p + \sqrt{p^2 - 2 \cdot \eta} \cdot \left[2 - G^2 \cdot \left[1/\Delta_0 + \Delta_{\rm ns} \cdot (\Delta_0 - \chi''(y_0))\right]\right]} \end{aligned}$ Eqs. (4.70)-(4.72) are only calculated for $x_{\tilde{g}} > 0$.

Eqs. (4.70)-(4.72) are only calculated for $x_g > 0$

$$E_{\rm s} = \exp\left(-x_{\rm s}\right) \tag{4.70}$$

$$D_{\rm s} = [1/E_{\rm s} - x_{\rm s} - 1 - \chi(x_{\rm s})] \cdot \Delta_{\rm ns}$$
(4.71)

$$P_{\rm s} = x_{\rm s} - 1 + E_{\rm s} \tag{4.72}$$

$$x_{\rm gs} = \begin{cases} x_{\rm g} - x_{\rm s} & \text{for } x_{\rm g} \le 0\\ G \cdot \sqrt{D_{\rm s} + P_{\rm s}} & \text{for } x_{\rm g} > 0 \end{cases}$$

$$(4.73)$$

$$\psi_{\rm ss} = \phi_{\rm T}^* \cdot x_{\rm s} \tag{4.74}$$

4.2.4 Drain Saturation Voltage

Eqs. (4.75)-(4.95) are only calculated for $x_{\rm g}>0$.

$$q_{\rm is} = \frac{G^2 \cdot \phi_{\rm T}^* \cdot D_{\rm s}}{x_{\rm gs} + G \cdot \sqrt{P_{\rm s}}} \tag{4.75}$$

$$\alpha_{\rm s} = 1 + \frac{G \cdot (1 - E_{\rm s})}{2 \cdot \sqrt{P_{\rm s}}} \tag{4.76}$$

$$q_{\rm bs} = \phi_{\rm T}^* \cdot G \cdot \sqrt{P_{\rm s}} \tag{4.77}$$

$$\rho_{\rm b} = \begin{cases} 1 + \mathbf{RSB} \cdot V_{\rm sbx} & \text{for } \mathbf{RSB} \ge 0 \\ \frac{1}{1 - \mathbf{RSB} \cdot V_{\rm sbx}} & \text{for } \mathbf{RSB} < 0 \end{cases}$$

$$(4.78)$$

$$\rho_{\rm g,s} = \begin{cases} \frac{1}{1 + \mathbf{RSG} \cdot q_{\rm is}} & \text{for } \mathbf{RSG} \ge 0\\ 1 - \mathbf{RSG} \cdot q_{\rm is} & \text{for } \mathbf{RSG} < 0 \end{cases}$$

$$(4.79)$$

$$\rho_{\rm s} = \boldsymbol{\theta}_{\mathbf{R}} \cdot \rho_{\rm b} \cdot \rho_{\rm g,s} \cdot q_{\rm is} \tag{4.80}$$

$$\mu_{\mathbf{x}} = \frac{1 + \mathbf{X}_{\mathbf{cor}} \cdot V_{\mathbf{sbx}}}{1 + 0.2 \cdot \mathbf{X}_{\mathbf{cor}} \cdot V_{\mathbf{sby}}} \tag{4.81}$$

$$E_{\text{eff,s}} = E_{\text{eff0}} \cdot \left(q_{\text{bs}} + \eta_{\mu} \cdot q_{\text{is}} \right) \tag{4.82}$$

$$G_{\text{mob,s}} = \frac{1 + (\boldsymbol{\mu}_{\mathbf{E}} \cdot E_{\text{eff,s}})^{\boldsymbol{\theta}_{\boldsymbol{\mu}}} + \boldsymbol{C}_{\mathbf{S}} \cdot \left(\frac{q_{\text{bs}}}{q_{\text{is}} + q_{\text{bs}}}\right)^{2} + \rho_{\text{s}}}{\mu_{\text{x}}}$$
(4.83)

$$\xi_{\rm tb} = \begin{cases} 1 + \text{THESATB} \cdot V_{\rm sbx} & \text{for THESATB} \ge 0 \\ \\ \frac{1}{1 - \text{THESATB} \cdot V_{\rm sbx}} & \text{for THESATB} < 0 \end{cases}$$

$$(4.84)$$

$$w_{\text{sat,s}} = \frac{100 \cdot q_{\text{is}} \cdot \xi_{\text{tb}}}{100 + q_{\text{is}} \cdot \xi_{\text{tb}}}$$

$$\tag{4.85}$$

$$\theta_{\text{sat,s}}^* = \begin{cases} \frac{\theta_{\text{sat}}}{G_{\text{mob,s}}} \cdot (1 + \text{THESATG} \cdot w_{\text{sat,s}}) & \text{for THESATG} \ge 0 \\ \frac{\theta_{\text{sat}}}{G_{\text{mob,s}}} \cdot \frac{1}{1 - \text{THESATG} \cdot w_{\text{sat,s}}} & \text{for THESATG} < 0 \end{cases}$$

$$(4.86)$$

$$\phi_{\infty} = q_{\rm is}/\alpha_{\rm s} + \phi_{\rm T}^* \tag{4.87}$$

$$y_{\text{sat}} = \begin{cases} \theta_{\text{sat,s}}^* \cdot \phi_{\infty} / \sqrt{2} & \text{for NMOS} \\ \frac{\theta_{\text{sat,s}}^* \cdot \phi_{\infty} / \sqrt{2}}{\sqrt{1 + \theta_{\text{sat,s}}^* \cdot \phi_{\infty} / \sqrt{2}}} & \text{for PMOS} \end{cases}$$

$$(4.88)$$

$$z_{\rm a} = \frac{2}{1 + \sqrt{1 + 4 \cdot y_{\rm sat}}} \tag{4.89}$$

$$\phi_0 = \phi_{\infty} \cdot z_{\mathbf{a}} \cdot \left[1 + 0.86 \cdot z_{\mathbf{a}} \cdot y_{\text{sat}} \cdot \frac{1 - z_{\mathbf{a}}^2 \cdot y_{\text{sat}}}{1 + 4 \cdot z_{\mathbf{a}}^3 \cdot y_{\text{sat}}^2} \right]$$
(4.90)

$$a_{\rm sat} = x_{\rm gs} + G^2/2$$
 (4.91)

$$\phi_2 = \frac{\phi_{\mathbf{T}}^* \cdot 0.98 \cdot G^2 \cdot D_{\mathbf{s}}}{a_{\text{sat}} + \sqrt{a_{\text{sat}}^2 - 0.98 \cdot G^2 \cdot D_{\mathbf{s}}}}$$
(4.92)

$$\phi_{\text{sat}} = \frac{2 \cdot \phi_0 \cdot \phi_2}{\phi_0 + \phi_2 + \sqrt{(\phi_0 + \phi_2)^2 - 3.96 \cdot \phi_0 \cdot \phi_2}}$$
(4.93)

$$V_{\text{dsat}} = \phi_{\text{sat}} - \phi_{\mathbf{T}}^* \cdot \ln \left[1 + \frac{\phi_{\text{sat}} \cdot \left(\phi_{\text{sat}} - 2 \cdot a_{\text{sat}} \cdot \phi_{\mathbf{T}}^* \right)}{G^2 \cdot D_{\text{s}} \cdot \phi_{\mathbf{T}}^{*2}} \right]$$
(4.94)

$$V_{\rm dse} = \frac{V_{\rm DS}}{\left[1 + (V_{\rm DS}/V_{\rm dsat})^{\rm AX}\right]^{1/\rm AX}}$$
(4.95)

4.2.5 Surface Potential at Drain Side and Related Variables

Eqs. (4.96)-(4.105) are only calculated for $x_{\rm g}>0$.

$$x_{\rm nd} = \frac{\phi_{\rm B} + V_{\rm SB}^* + V_{\rm dse}}{\phi_{\rm T}^*}$$
 (4.96)

$$k_{\rm ds} = \exp\left(-V_{\rm dse}/\phi_{\rm T}^*\right) \tag{4.97}$$

$$\Delta_{\rm nd} = \Delta_{\rm ns} \cdot k_{\rm ds} \tag{4.98}$$

if
$$x_{\rm g} \le x_{\rm mrg} \left\{ x_{\rm d} = \frac{x_{\rm g}}{\xi} \cdot \left[1 + G \cdot x_{\rm g} \cdot \frac{1 - \Delta_{\rm nd}}{\xi^2 \cdot 6 \cdot \sqrt{2}} \right] \right\}$$
 (4.99)

$$\begin{cases} b_{x} = x_{nd} + 3.0 \\ \eta = MINA(x_{0}, b_{x}, 5) - \left(b_{x} - \sqrt{b_{x}^{2} + 5}\right)/2 \\ a = (x_{g} - \eta)^{2} - G^{2} \cdot \left[\exp(-\eta) + \eta - 1 - \Delta_{nd} \cdot (\eta + 1 + \chi(\eta))\right] \\ b = 1 - G^{2}/2 \cdot \left[\exp(-\eta) - \Delta_{nd} \cdot \chi''(\eta)\right] \\ c = 2 \cdot (x_{g} - \eta) + G^{2} \cdot \left[1 - \exp(-\eta) - \Delta_{nd} \cdot (1 + \chi'(\eta))\right] \\ \tau = x_{nd} - \eta + \ln\left(a/G^{2}\right) \\ y_{0} = \sigma_{2}(a, b, c, \tau, \eta) \\ \Delta_{0} = \exp\left(y_{0}\right) \\ p = 2 \cdot (x_{g} - y_{0}) + G^{2} \cdot \left[1 - 1/\Delta_{0} + \Delta_{nd} \cdot (\Delta_{0} - 1 - \chi'(y_{0}))\right] \\ q = (x_{g} - y_{0})^{2} - G^{2} \cdot \left[y_{0} + 1/\Delta_{0} - 1 + \Delta_{nd} \cdot (\Delta_{0} - y_{0} - 1 - \chi(y_{0}))\right] \\ x_{d} = y_{0} + \frac{2 \cdot q}{p + \sqrt{p^{2} - 2 \cdot q} \cdot \left\{2 - G^{2} \cdot \left[1/\Delta_{0} + \Delta_{nd} \cdot (\Delta_{0} - \chi''(y_{0}))\right]\right\}} \end{cases}$$

$$(4.101)$$

$$x_{\rm ds} = x_{\rm d} - x_{\rm s} \tag{4.101}$$

$$\lim_{x_{\rm ds}} x_{\rm ds} < 10^{-10} \begin{cases} p = 2 \cdot x_{\rm gs} + G^2 \cdot [1 - E_{\rm s} + \Delta_{\rm nd} \cdot (1/E_{\rm s} - 1 - \chi'(x_{\rm s}))] \\ q = G^2 \cdot (1 - k_{\rm ds}) \cdot D_{\rm s} \\ \xi = 1 - G^2/2 \cdot [E_{\rm s} + \Delta_{\rm nd} \left(1/E_{\rm s} - \chi''(x_{\rm s})\right)] \\ x_{\rm ds} = \frac{2 \cdot q}{p + \sqrt{p^2 - 4 \cdot \xi \cdot q}} \\ x_{\rm d} = x_{\rm s} + x_{\rm ds} \end{cases} \tag{4.102}$$

$$E_{\rm d} = \exp\left(-x_{\rm d}\right) \tag{4.103}$$

$$E_{\rm d} = \exp\left(-x_{\rm d}\right) \tag{4.103}$$

$$D_{\rm d} = (1/E_{\rm d} - x_{\rm d} - 1 - \chi(x_{\rm d})) \cdot \Delta_{\rm nd}$$
(4.104)

$$E_{\rm d} = \exp(-x_{\rm d})$$

$$D_{\rm d} = (1/E_{\rm d} - x_{\rm d} - 1 - \chi(x_{\rm d})) \cdot \Delta_{\rm nd}$$

$$\Delta \psi = \phi_{\rm T}^* \cdot x_{\rm ds}$$

$$(4.105)$$

$$(4.106)$$

$$\psi_{\rm sd} = \phi_{\rm T}^* \cdot x_{\rm d} \tag{4.106}$$

4.2.6 Mid-Point Surface Potential and Related Variables

if
$$x_{\rm g} > 0$$

$$\begin{cases}
x_{\rm m} = (x_{\rm s} + x_{\rm d})/2 \\
E_{\rm m} = \sqrt{E_{\rm s} \cdot E_{\rm d}} \\
\bar{D} = (D_{\rm s} + D_{\rm d})/2 \\
D_{\rm m} = \bar{D} + x_{\rm ds}^2/8 \cdot (E_{\rm m} - 2/G^2) \\
P_{\rm m} = x_{\rm m} - 1 + E_{\rm m} \\
x_{\rm gm} = G \cdot \sqrt{D_{\rm m} + P_{\rm m}}
\end{cases}$$
(4.107)

if
$$x_{\rm g} \le 0$$

$$\begin{cases} x_{\rm m} = x_{\rm s} \\ x_{\rm gm} = x_{\rm g} - x_{\rm s} \end{cases}$$
 (4.108)

4.2.7 Polysilicon Depletion

Eqs. (4.109)-(4.123) are only calculated for $k_{
m P}>0$ and $x_{
m g}>0$ (otherwise $\eta_{
m p}=1$):

$$x_{\rm m}^{(0)} = x_{\rm m}, x_{\rm ds}^{(0)} = x_{\rm ds}, D_{\rm m}^{(0)} = D_{\rm m}, E_{\rm m}^{(0)} = E_{\rm m}, (4.109)$$

$$d_0 = 1 - E_{\rm m}^{(0)} + 2 \cdot x_{\rm gm}/G^2 \tag{4.110}$$

$$\eta_{\rm p} = 1/\sqrt{1 + \mathbf{k_P} \cdot x_{\rm gm}} \tag{4.111}$$

$$x_{\rm pm} = k_{\rm P} \cdot \left[\frac{\eta_{\rm p} \cdot x_{\rm gm}}{1 + \eta_{\rm p}} \right]^2 \cdot \frac{D_{\rm m}^{(0)}}{D_{\rm m}^{(0)} + P_{\rm m}}$$
(4.112)

$$p = 2 \cdot (x_{\rm gm} - x_{\rm pm}) + G^2 \cdot \left(1 - E_{\rm m}^{(0)} + D_{\rm m}^{(0)}\right)$$
(4.113)

$$q = x_{\text{pm}} \cdot (x_{\text{pm}} - 2 \cdot x_{\text{gm}}) \tag{4.114}$$

$$\xi_{\rm p} = 1 - G^2/2 \cdot \left(E_{\rm m}^{(0)} + D_{\rm m}^{(0)}\right) \tag{4.115}$$

$$u_{\rm p} = \frac{p \cdot q}{p^2 - \xi_{\rm p} \cdot q} \tag{4.116}$$

$$x_{\rm m} = x_{\rm m}^{(0)} + u_{\rm p}$$
 (4.117)

$$E_{\rm m} = E_{\rm m}^{(0)} \cdot \exp\left(-u_{\rm p}\right)$$
 (4.118)

$$D_{\rm m} = D_{\rm m}^{(0)} \cdot \exp\left(u_{\rm p}\right)$$
 (4.119)

$$P_{\rm m} = x_{\rm m} - 1 + E_{\rm m} \tag{4.120}$$

$$x_{\rm gm} = G \cdot \sqrt{D_{\rm m} + P_{\rm m}} \tag{4.121}$$

$$x_{\rm ds} = x_{\rm ds}^{(0)} \cdot \frac{\exp(u_{\rm p}) \cdot \left[\bar{D} + d_{0}\right]}{1 - E_{\rm m} + 2 \cdot x_{\rm gm} \cdot \eta_{\rm p} / G^{2} + \exp(u_{\rm p}) \cdot \bar{D}}$$
(4.122)

$$\Delta \psi = \phi_{\mathbf{T}}^* \cdot x_{\mathrm{ds}} \tag{4.123}$$

4.2.8 Potential Mid-Point Inversion Charge and Related Variables

Eqs. (4.124)-(4.131) are only calculated for $x_{\rm g}>0$.

$$q_{\rm im} = \frac{G^2 \cdot \phi_{\rm T}^* \cdot D_{\rm m}}{x_{\rm gm} + G \cdot \sqrt{P_{\rm m}}} \tag{4.124}$$

$$\alpha_{\rm m} = \eta_{\rm p} + \frac{G \cdot (1 - E_{\rm m})}{2 \cdot \sqrt{P_{\rm m}}} \tag{4.125}$$

$$q_{\rm im}^* = q_{\rm im} + \phi_{\rm T}^* \cdot \alpha_{\rm m} \tag{4.126}$$

$$q_{\rm bm} = \phi_{\rm T}^* \cdot G \cdot \sqrt{P_{\rm m}} \tag{4.127}$$

Series resistance:

$$\rho_{\rm g} = \begin{cases}
\frac{1}{1 + \mathbf{RSG} \cdot q_{\rm im}} & \text{for } \mathbf{RSG} \ge 0 \\
1 - \mathbf{RSG} \cdot q_{\rm im} & \text{for } \mathbf{RSG} < 0
\end{cases}$$
(4.128)

$$\rho_{\rm s} = \boldsymbol{\theta}_{\mathbf{R}} \cdot \rho_{\rm b} \cdot \rho_{\rm g} \cdot q_{\rm im} \tag{4.129}$$

Mobility reduction:

$$E_{\text{eff}} = \mathbf{E}_{\text{eff0}} \cdot (q_{\text{bm}} + \boldsymbol{\eta}_{\boldsymbol{\mu}} \cdot q_{\text{im}}) \tag{4.130}$$

$$G_{\text{mob}} = \frac{1 + (\boldsymbol{\mu}_{\mathbf{E}} \cdot E_{\text{eff}})^{\boldsymbol{\theta}_{\boldsymbol{\mu}}} + \boldsymbol{C}_{\mathbf{S}} \cdot \left(\frac{q_{\text{bm}}}{q_{\text{im}} + q_{\text{bm}}}\right)^{2} + \rho}{\mu_{x}}$$
(4.131)

4.2.9 Drain-Source Channel Current

Eqs. (4.132)-(4.143) are only calculated for $x_{\rm g}>0$:

Channel length modulation:

$$R_1 = q_{\rm im}/q_{\rm im}^*$$
 (4.132)

$$R_2 = \phi_{\mathbf{T}}^* \cdot \alpha_{\mathbf{m}} / q_{\mathbf{im}}^* \tag{4.133}$$

$$T_{1} = \ln \left(\frac{1 + \frac{V_{DS} - \Delta \psi}{\mathbf{VP}}}{1 + \frac{V_{dse} - \Delta \psi}{\mathbf{VP}}} \right)$$
(4.134)

$$T_2 = \ln\left(1 + \frac{V_{\rm dsx} - \Delta\psi}{\mathbf{VP}}\right) \tag{4.135}$$

$$\Delta L/L = \mathbf{ALP} \cdot T_1 \tag{4.136}$$

$$G_{\Delta L} = \frac{1}{1 + \Delta L/L + (\Delta L/L)^2} \tag{4.137}$$

$$\Delta L_1/L = \left[\mathbf{ALP} + \frac{\mathbf{ALP1}}{q_{\text{im}}^*} \cdot R_1 \right] \cdot T_1 + \mathbf{ALP2} \cdot q_{\text{bm}} \cdot R_2^2 \cdot T_2$$
(4.138)

$$F_{\Delta L} = \left[1 + \Delta L_1 / L + (\Delta L_1 / L)^2\right] \cdot G_{\Delta L} \tag{4.139}$$

Velocity saturation:

$$w_{\text{sat}} = \frac{100 \cdot q_{\text{im}} \cdot \xi_{\text{tb}}}{100 + q_{\text{im}} \cdot \xi_{\text{tb}}} \tag{4.140}$$

$$\theta_{\text{sat}}^* = \begin{cases} \frac{\boldsymbol{\theta}_{\text{sat}}}{G_{\text{mob,s}} \cdot G_{\Delta L}} \cdot (1 + \text{THESATG} \cdot w_{\text{sat}}) & \text{for THESATG} \ge 0 \\ \frac{\boldsymbol{\theta}_{\text{sat}}}{G_{\text{mob,s}} \cdot G_{\Delta L}} \cdot \frac{1}{1 - \text{THESATG} \cdot w_{\text{sat}}} & \text{for THESATG} < 0 \end{cases}$$

$$(4.141)$$

$$z_{\text{sat}} = \begin{cases} (\theta_{\text{sat}}^* \cdot \Delta \psi)^2 & \text{for NMOS} \\ \frac{(\theta_{\text{sat}}^* \cdot \Delta \psi)^2}{1 + \theta_{\text{ent}}^* \cdot \Delta \psi} & \text{for PMOS} \end{cases}$$
(4.142)

$$G_{\text{vsat}} = \frac{G_{\text{mob}} \cdot G_{\Delta L}}{2} \cdot \left(1 + \sqrt{1 + 2 \cdot z_{\text{sat}}}\right) \tag{4.143}$$

Drain-Source channel current:

$$I_{\rm DS} = \begin{cases} 0 & \text{for } x_{\rm g} \le 0 \\ \beta \cdot F_{\Delta L} \cdot \frac{q_{\rm im}^*}{G_{\rm treet}} \cdot \Delta \psi & \text{for } x_{\rm g} > 0 \end{cases}$$

$$(4.144)$$

4.2.10 Auxiliary Variables for Calculation of Intrinsic Charges and Gate Current

Eqs. (4.145)-(4.147) are only calculated for $x_{\rm g}>0$.

$$V_{\text{oxm}} = \phi_{\mathbf{T}}^* \cdot x_{\text{gm}} \tag{4.145}$$

$$\alpha_{\rm m}' = \alpha_{\rm m} \cdot \left[1 + \frac{z_{\rm sat}}{2} \cdot \left(\frac{G_{\rm mob} \cdot G_{\Delta L}}{G_{\rm vsat}} \right)^2 \right] \tag{4.146}$$

$$H = \frac{G_{\text{mob}} \cdot G_{\Delta L}}{G_{\text{vsat}}} \cdot \frac{q_{\text{im}}^*}{\alpha_{\text{m}}'} \tag{4.147}$$

4.2.11 Impact Ionization or Weak-Avalanche

The equations in this Section are only calculated when SWIMPACT = 1 and $x_{\rm g}>0$.

$$a_2^* = \mathbf{a_2} \cdot \left[1 + \mathbf{A4} \cdot \left(\sqrt{V_{\text{SB}}^* + \phi_{\mathbf{B}}} - \sqrt{\phi_{\mathbf{B}}} \right) \right]$$
(4.148)

$$\Delta V_{\text{sat}} = V_{\text{DS}} - \mathbf{A3} \cdot \Delta \psi \tag{4.149}$$

$$M_{\text{avl}} = \begin{cases} 0 & \text{for } \Delta V_{\text{sat}} \le 0\\ \mathbf{A1} \cdot \Delta V_{\text{sat}} \cdot \exp\left(-\frac{a_2^*}{\Delta V_{\text{sat}}}\right) & \text{for } \Delta V_{\text{sat}} > 0 \end{cases}$$

$$(4.150)$$

$$I_{\text{avl}} = M_{\text{avl}} \cdot I_{\text{DS}} \tag{4.151}$$

4.2.12 Surface Potential in Gate Overlap Regions

$$\begin{cases} y_{\rm g} = -x_{\rm g} \\ z = x_1 \cdot y_{\rm g}/\xi_{\rm ov} \\ \eta = \left[z + 10 - \sqrt{(z - 6)^2 + 64}\right]/2 \\ a = (y_{\rm g} - \eta)^2 + G_{\rm ov}^2 \cdot (\eta + 1) \\ c = 2 \cdot (y_{\rm g} - \eta) - G_{\rm ov}^2 \\ \tau = -\eta + \ln\left(a/G_{\rm ov}^2\right) \\ y_0 = \sigma_1(a, c, \tau, \eta) \\ \Delta_0 = \exp\left(y_0\right) \\ p = 2 \cdot (y_{\rm g} - y_0) + G_{\rm ov}^2 \cdot (\Delta_0 - 1) \\ q = (y_{\rm g} - y_0)^2 + G_{\rm ov}^2 \cdot (y_0 - \Delta_0 + 1) \\ x_{\rm ov} = -y_0 - \frac{2 \cdot q}{p + \sqrt{p^2 - 2 \cdot q \cdot (2 - G_{\rm ov}^2 \cdot \Delta_0)}} \end{cases}$$

$$\text{if } |x_{\rm g}| < x_{\rm mrgov} \left\{ \begin{array}{c} x_{\rm ov} = x_{\rm g}/\xi_{\rm ov} \\ x_{\rm ov} = x_{\rm g}/\xi_{\rm ov} \cdot \left[1 + x_{\rm g} \cdot (\xi_{\rm ov} \cdot x_{\rm l} - x_{\rm gl})/x_{\rm gl}^2\right] \\ \omega = 1 - \exp\left(-\bar{x}\right) \\ x_0 = x_{\rm g} + G_{\rm ov}^2/2 - G_{\rm ov} \cdot \sqrt{x_{\rm g} + G_{\rm ov}^2/4 - \omega} \\ \Delta_0 = \exp\left(-x_0\right) \\ p = 2 \cdot (x_{\rm g} - x_0) + G_{\rm ov}^2 \cdot (1 - \Delta_0) \\ q = (x_{\rm g} - x_0)^2 - G_{\rm ov}^2 \cdot (x_0 + \Delta_0 - 1) \\ x_{\rm ov} = x_0 + \frac{2 \cdot q}{p + \sqrt{p^2 - 2 \cdot q \cdot (2 - G_{\rm ov}^2 \cdot \Delta_0)}} \end{cases}$$

$$\psi_{\text{sov}} = -\phi_{\mathbf{T}} \cdot x_{\text{ov}} \left(-\frac{V_{\text{GS}}}{\phi_{\mathbf{T}}} \right) \tag{4.153}$$

$$\psi_{\text{dov}} = -\phi_{\mathbf{T}} \cdot x_{\text{ov}} \left(-\frac{V_{\text{GS}} - V_{\text{DS}}}{\phi_{\mathbf{T}}} \right) \tag{4.154}$$

$$V_{\text{ov}_0} = V_{\text{GS}} - \psi_{\text{sov}} \tag{4.155}$$

$$V_{\text{ov}_{\text{L}}} = V_{\text{GS}} - V_{\text{DS}} - \psi_{\text{dov}} \tag{4.156}$$

4.2.13 **Gate Current**

The equations in this Section are only calculated when SWIGATE = 1.

Source/Drain gate overlap current:

Source/Drain gate overlap current:
$$\begin{cases} V_{\text{ov}}^* = \sqrt{V_{\text{ov}}^2 + 10^{-6}} \\ \psi_{\text{tov}} = \text{MINA} \left(0, V_{\text{ov}} + \boldsymbol{D_{\text{ov}}}, 0.01 \right) \\ v_{\text{tov}} = V_{\text{ov}} + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} = V_{\text{ov}} + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} \\ \frac{V_{\text{ov}}^*}{V_{\text{ov}}} = V_{\text{ov}} + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} \\ V_{\text{ov}}^* = V_{\text{ov}}^* + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} \\ V_{\text{ov}}^* = V_{\text{ov}}^* + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} \\ V_{\text{ov}}^* = V_{\text{ov}}^* + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} \\ V_{\text{ov}}^* = V_{\text{ov}}^* + \frac{V_{\text{ov}}^*}{V_{\text{ov}}} + \frac{V_{\text{ov}}^*}{V_{o$$

$$I_{\text{GSov}} = I_{\text{Gov}} \left(V_{\text{GS}}, \, \psi_{\text{sov}}, \, V_{\text{ov}_0} \right) \tag{4.158}$$

$$I_{\text{GDov}} = I_{\text{Gov}} (V_{\text{GS}} - V_{\text{DS}}, \psi_{\text{dov}}, V_{\text{ov}_{\text{I}}})$$
 (4.159)

Gate-channel current:

$$V_{\rm m} = V_{\rm SB}^* + \phi_{\rm T}^* \cdot \left[\frac{x_{\rm ds}}{2} - \ln \left(\frac{1 + \exp(x_{\rm ds} - V_{\rm dse}/\phi_{\rm T}^*)}{2} \right) \right]$$
(4.160)

$$\psi_{\rm t} = {\rm MINA} (0, V_{\rm oxm} + D_{\rm ch}, 0.01)$$
 (4.161)

$$V_{\text{oxm}}^* = \sqrt{V_{\text{oxm}}^2 + 10^{-6}} \tag{4.162}$$

$$z_{\rm g} = \begin{cases} \text{MINA}\left(\frac{V_{\rm oxm}^*}{\mathbf{CHIB}}, \mathbf{GC_Q}, 10^{-6}\right) & \text{for } \mathbf{GC3} < 0\\ \frac{V_{\rm oxm}^*}{\mathbf{CHIB}} & \text{for } \mathbf{GC3} \ge 0 \end{cases}$$

$$(4.163)$$

$$\Delta_{\rm Si} = \exp\left(x_{\rm m} - \frac{\alpha_{\rm b} + V_{\rm m} - \psi_{\rm t}}{\phi_{\rm T}^*}\right) \tag{4.164}$$

$$F_{\rm S} = \ln \left[\frac{1 + \Delta_{\rm Si}}{1 + \Delta_{\rm Si} \cdot \exp\left(-\frac{V_{\rm GS} + V_{\rm SB}^* - V_{\rm m}}{\phi_{\rm T}^*}\right)} \right]$$
(4.165)

$$I_{\text{GCO}} = I_{\text{GINV}} \cdot F_{\text{S}} \cdot \exp\left(B \cdot \left[-3/2 + z_{\text{g}} \cdot (\text{GC2} + \text{GC3} \cdot z_{\text{g}})\right]\right)$$
(4.166)

$$\operatorname{if} x_{\mathrm{g}} > 0 \begin{cases} u_{0} = \operatorname{CHiB} / \left[B \cdot (\operatorname{GC2} + 2 \cdot \operatorname{GC3} \cdot z_{\mathrm{g}}) \right] \\ x = \Delta \psi / \left(2 \cdot u_{0} \right) \\ b = u_{0} / H \\ B_{\mathrm{g}} = b \cdot \left(1 - b \right) / 2 \\ A_{\mathrm{g}} = 1 / 2 - 3 \cdot B_{\mathrm{g}} \\ p_{\mathrm{gc}} = \left(1 - b \right) \cdot \frac{\sinh(x)}{x} + b \cdot \cosh(x) \\ p_{\mathrm{gd}} = \frac{p_{\mathrm{gc}}}{2} - B_{\mathrm{g}} \cdot \sinh(x) - A_{\mathrm{g}} \cdot \frac{\sinh(x)}{x} \cdot \left[\coth(x) - \frac{1}{x} \right] \end{cases}$$

$$(4.167)$$

if
$$x_{\rm g} \le 0 \begin{cases} p_{\rm gc} = 1 \\ p_{\rm gd} = 1/2 \end{cases}$$
 (4.168)

$$S_{\rm g} = \frac{1}{2} \cdot \left(1 + \frac{x_{\rm g}}{\sqrt{x_{\rm g}^2 + 10^{-6}}} \right) \tag{4.169}$$

$$I_{\rm GC} = I_{\rm GCO} \cdot p_{\rm gc} \cdot S_{\rm g} \tag{4.170}$$

$$I_{\text{GCD}} = I_{\text{GCO}} \cdot p_{\text{gd}} \cdot S_{\text{g}} \tag{4.171}$$

$$I_{GCS} = I_{GC} - I_{GCD} \tag{4.172}$$

$$I_{\rm GB} = I_{\rm GCO} \cdot p_{\rm gc} \cdot (1 - S_{\rm g}) \tag{4.173}$$

4.2.14 Gate-Induced Drain/Source Leakage Current

The equations in this section are only calculated when SWGIDL = 1.

$$I_{\text{gixl}}(V_{\text{ov}}, V) = \begin{cases} V_{\text{tov}} = \sqrt{V_{\text{ov}}^2 + \mathbf{CGIDL}^2 \cdot V^2 + 10^{-6}} \\ t = V \cdot V_{\text{tov}} \cdot V_{\text{ov}} \\ I_{\text{gixl}} = \begin{cases} -\mathbf{A}_{\text{GIDL}} \cdot t \cdot \exp\left(-\frac{\mathbf{B}_{\text{GIDL}}}{V_{\text{tov}}}\right) & \text{for } V_{\text{ov}} < 0 \\ 0 & \text{for } V_{\text{ov}} \ge 0 \end{cases}$$

$$(4.174)$$

$$I_{\text{gisl}} = I_{\text{gixl}}(V_{\text{OV}_0}, V_{\text{SB}})$$
 (4.175)

$$I_{\text{gidl}} = I_{\text{gixl}}(V_{\text{ov}_{\text{L}}}, V_{\text{DS}} + V_{\text{SB}})$$
 (4.176)

4.2.15 Total Terminal Currents

$$I_{\rm D} = I_{\rm DS} + I_{\rm avl} - I_{\rm GDov} - I_{\rm GCD} + I_{\rm gidl}$$

$$(4.177)$$

$$I_{\rm S} = -I_{\rm DS} - I_{\rm GSov} - I_{\rm GCS} + I_{\rm gisl} \tag{4.178}$$

$$I_{\rm G} = I_{\rm GC} + I_{\rm GB} + I_{\rm GDov} + I_{\rm GSov} \tag{4.179}$$

$$I_{\rm B} = -I_{\rm avl} - I_{\rm GB} - I_{\rm gidl} - I_{\rm gisl} \tag{4.180}$$

4.2.16 Quantum-Mechanical Corrections

$$q_{\text{eff}} = \begin{cases} V_{\text{oxm}} & \text{for } x_{\text{g}} \le 0 \\ q_{\text{bm}} + \eta_{\mu} \cdot q_{\text{im}} & \text{for } x_{\text{g}} > 0 \end{cases}$$

$$(4.181)$$

$$q_{\text{eff}} = \begin{cases} V_{\text{oxm}} & \text{for } x_{\text{g}} \leq 0 \\ q_{\text{bm}} + \boldsymbol{\eta}_{\boldsymbol{\mu}} \cdot q_{\text{im}} & \text{for } x_{\text{g}} > 0 \end{cases}$$

$$C_{\text{OX}}^{\text{qm}} = \begin{cases} \mathbf{COX} & \text{for } \boldsymbol{q}_{\mathbf{q}} = 0 \\ \frac{\mathbf{COX}}{1 + \boldsymbol{q}_{\mathbf{q}}/(q_{\text{eff}}^2 + \boldsymbol{q}_{\text{lim}}^2)^{1/6}} & \text{for } \boldsymbol{q}_{\mathbf{q}} > 0 \end{cases}$$

$$(4.181)$$

4.2.17 Intrinsic Charge Model

$$\begin{cases}
F_{j} = \Delta \psi / (2 \cdot H) \\
q_{\Delta L} = (1 - G_{\Delta L}) \cdot (q_{im} - \alpha_{m} \cdot \Delta \psi / 2) \\
q_{\Delta L}^{*} = q_{\Delta L} \cdot (1 + G_{\Delta L}) \\
Q_{G}^{(i)} = C_{OX}^{qm} \cdot \left[V_{oxm} + \frac{\eta_{p} \cdot \Delta \psi}{2} \cdot \left(\frac{G_{\Delta L}}{3} \cdot F_{j} + G_{\Delta L} - 1 \right) \right] \\
Q_{I}^{(i)} = -C_{OX}^{qm} \cdot \left[G_{\Delta L} \cdot \left(q_{im} + \frac{\alpha_{m} \cdot \Delta \psi}{6} \cdot F_{j} \right) + q_{\Delta L} \right] \\
Q_{D}^{(i)} = -\frac{C_{OX}^{qm}}{2} \cdot \left[G_{\Delta L}^{2} \cdot \left(q_{im} + \frac{\alpha_{m} \cdot \Delta \psi}{6} \cdot \left[\frac{F_{j}^{2}}{5} + F_{j} - 1 \right] \right) + q_{\Delta L}^{*} \right]
\end{cases}$$
(4.183)

if
$$x_{\rm g} \le 0$$

$$\begin{cases}
Q_{\rm G}^{(i)} = C_{\rm OX}^{\rm qm} \cdot V_{\rm oxm} \\
Q_{\rm I}^{(i)} = 0 \\
Q_{\rm D}^{(i)} = 0
\end{cases}$$
(4.184)

$$Q_{\rm S}^{(i)} = Q_{\rm L}^{(i)} - Q_{\rm D}^{(i)} \tag{4.185}$$

$$Q_{\rm B}^{(i)} = -Q_{\rm I}^{(i)} - Q_{\rm G}^{(i)} \tag{4.186}$$

4.2.18 Extrinsic Charge Model

The charges of the source and drain overlap regions:

$$Q_{\text{sov}} = \mathbf{CGOV} \cdot (V_{\text{GS}} - \psi_{\text{sov}}) \tag{4.187}$$

$$Q_{\text{dov}} = \mathbf{CGOV} \cdot (V_{\text{GS}} - V_{\text{DS}} - \psi_{\text{dov}}) \tag{4.188}$$

The charge of the bulk overlap region

$$Q_{\text{bov}} = \mathbf{CGBOV} \cdot (V_{\text{GS}} - V_{\text{SB}}) \tag{4.189}$$

Outer fringe charge:

$$Q_{\text{ofs}} = \mathbf{CFR} \cdot V_{\text{GS}} \tag{4.190}$$

$$Q_{\text{ofd}} = \mathbf{CFR} \cdot (V_{\text{GS}} - V_{\text{DS}}) \tag{4.191}$$

4.2.19 Total Terminal Charges

$$Q_{\rm G} = Q_{\rm G}^{(i)} + Q_{\rm sov} + Q_{\rm dov} + Q_{\rm ofs} + Q_{\rm ofd} + Q_{\rm bov}$$
(4.192)

$$Q_{\rm S} = Q_{\rm S}^{(i)} - Q_{\rm sov} - Q_{\rm ofs} \tag{4.193}$$

$$Q_{\rm D} = Q_{\rm D}^{(i)} - Q_{\rm dov} - Q_{\rm ofd} \tag{4.194}$$

$$Q_{\rm B} = Q_{\rm B}^{(i)} - Q_{\rm bov} \tag{4.195}$$

4.2.20 Noise Model

Eqs. (4.196)-(4.212) are only calculated for $x_{\rm g}>0$. In these equations $f_{\rm op}$ represents the operation frequency of the transistor and $j=\sqrt{-1}$.

$$N^* = \frac{C_{\text{ox}}}{q} \cdot \alpha_{\text{m}} \cdot \phi_{\text{T}} \tag{4.196}$$

$$N_{\rm m}^* = \frac{C_{\rm ox}}{q} \cdot q_{\rm im}^* \tag{4.197}$$

$$\Delta N = \frac{C_{\text{ox}}}{q} \cdot \alpha_{\text{m}} \cdot \Delta \psi \tag{4.198}$$

$$S_{\mathrm{fl}} = \frac{q \cdot \boldsymbol{\phi}_{\mathrm{T}}^2 \cdot \boldsymbol{\beta} \cdot I_{\mathrm{DS}}}{f_{\mathrm{op}} \cdot C_{\mathrm{ox}} \cdot G_{\mathrm{vsat}} \cdot N^*} \cdot \left[(\mathbf{NFA} - \mathbf{NFB} \cdot N^* + \mathbf{NFC} \cdot N^{*\,2}) \cdot \ln \left(\frac{N_{\mathrm{m}}^* + \Delta N/2}{N_{\mathrm{m}}^* - \Delta N/2} \right) \right]$$

+
$$\left(\mathbf{NFB} + \mathbf{NFC} \cdot [N_{\mathrm{m}}^* - 2 \cdot N^*]\right) \cdot \Delta N$$
 (4.199)

$$H_0 = \frac{q_{\rm im}^*}{\alpha_{\rm m}} \tag{4.200}$$

$$t_1 = \frac{q_{\rm im}}{q_{\rm im}^*} \tag{4.201}$$

$$t_2 = \left(\frac{\Delta\psi}{12 \cdot H_0}\right)^2 \tag{4.202}$$

$$R = \frac{H_0}{H} - 1 \tag{4.203}$$

$$l_{\rm c} = 1 - 12 \cdot t_2 \cdot R \tag{4.204}$$

$$g_{\text{ideal}} = \frac{\beta \cdot q_{\text{im}}^*}{G_{\text{vsat}}} \cdot F_{\Delta L} \tag{4.205}$$

$$C_{\text{Geff}} = \left(\frac{G_{\text{vsat}}}{G_{\text{mob}} \cdot G_{\Delta L}}\right)^2 \cdot C_{\text{OX}}^{\text{qm}} \cdot \eta_{\text{p}} \tag{4.206}$$

$$m_{\rm id} = \frac{g_{\rm ideal}}{l_{\rm c}^2} \cdot [t_1 + 12 \cdot t_2 - 24 \cdot (1 + t_1) \cdot t_2 \cdot R]$$
(4.207)

$$S_{\rm id} = N_{\rm T} \cdot m_{\rm id} \tag{4.208}$$

$$m_{ig} = \frac{1}{l_{c}^{2} \cdot g_{ideal}} \cdot \left[\frac{t_{1}}{12} - t_{2} \cdot \left(t_{1} + \frac{1}{5} - 12 \cdot t_{2} \right) - \frac{8}{5} \cdot t_{2} \cdot (t_{1} + 1 - 12 \cdot t_{2}) \cdot R \right]$$
(4.209)

$$S_{ig} = \mathbf{N}_{\mathbf{T}} \cdot \frac{(2 \cdot \pi \cdot f_{op} \cdot C_{Geff})^2 \cdot m_{ig}}{1 + (2 \cdot \pi \cdot f_{op} \cdot C_{Geff} \cdot m_{ig})^2}$$
(4.210)

$$m_{\text{igid}} = \frac{\sqrt{t_2}}{l_c^2} \cdot \left[1 - 12 \cdot t_2 - \left(t_1 + \frac{96}{5} \cdot t_2 - 12 \cdot t_1 \cdot t_2 \right) \cdot R \right]$$
(4.211)

$$S_{\text{igid}} = N_{\text{T}} \cdot \frac{2 \cdot \pi \cdot j \cdot f_{\text{op}} \cdot C_{\text{Geff}} \cdot m_{\text{igid}}}{1 + 2 \cdot \pi \cdot j \cdot f_{\text{op}} \cdot C_{\text{Geff}} \cdot m_{\text{ig}}}$$
(4.212)

Gate current shot noise:

$$S_{igs} = 2 \cdot q \cdot (I_{GCS} + I_{GSov}) \tag{4.213}$$

$$S_{\text{igd}} = 2 \cdot q \cdot (I_{\text{GCD}} + I_{\text{GDov}}) \tag{4.214}$$

Avalanche current shot noise:

$$S_{\text{avl}} = 2 \cdot q \cdot (1 + M_{\text{avl}}) \cdot I_{\text{avl}} \tag{4.215}$$

Section 5

Non-quasi-static RF model

5.1 Introduction

For high-frequency modeling and fast transient simulations, a special version of the PSP model is available, which enables the simulation of non-quasi-static (NQS) effects, and includes several parasitic resistances.

5.2 NQS-effects

In the PSP-NQS model, NQS-effects are introduced by applying the one-dimensional current continuity equation ($\partial I/\partial y \propto -\partial \rho/\partial t$) to the channel. A full numerical solution of this equation is too inefficient for compact modeling, therefore an approximate technique is used. The channel is partitioned into N+1 sections of equal length by assigning N equidistant collocation points. The charge density (per unit channel area) along the channel is then approximated by a cubic spline through these collocation points, assuring that both the charge and its first and second spatial derivatives are continuous along the channel. Within this approximation, the current continuity equation reduces to a system of N coupled first order ordinary differential equations, from which the channel charge at each collocation point can be found:

$$\begin{cases}
\frac{dQ_1}{dt} = f_1(Q_1, \dots, Q_N) \\
\vdots & \vdots \\
\frac{dQ_N}{dt} = f_N(Q_1, \dots, Q_N)
\end{cases}$$
(5.1)

Here, Q_i is the charge density at the *i*-th collocation point and f_i are functions, which contain the *complete* PSP-charge model. These equations are implemented by the definition of appropriate subcircuits (see left part of Fig. 5.1) and solved by the circuit simulator. Finally, the four terminal charges are calculated from the channel charges, using the Ward-Dutton partitioning scheme for the source and drain charges.

A full description of the PSP-NQS model is given in Section 5.5. More background information can be found in literature [3, 4].

5.3 Parasitics circuit

To facilitate RF-simulations, the PSP-NQS model contains a small network of parasitic elements: a gate resistance and four bulk resistances. Note that the junction diodes are no longer directly connected to the bulk terminal of the intrinsic MOS-transistor. The complete circuit is shown on the right side of Fig. 5.1.

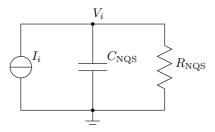
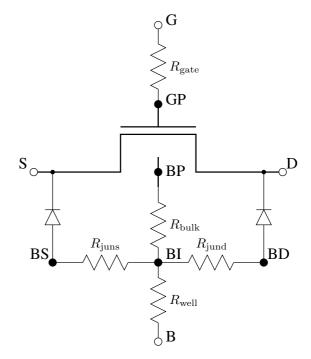


Figure 5.1: Above: The subcircuit used to solve one of the differential equations of Eq. (5.1). The current is set to $I_i = C_{\text{NQS}} \cdot f(V_1, \ldots, V_N)$, where the voltage V_i represents the charge density Q_i at the i-th collocation point and is solved by the circuit simulator. N of these circuits are defined and they are coupled through the dependence of I_i on the voltages of the other circuits. The resistance R_{NQS} has a very large value and is present only for convergence purposes. Right: The full network of parasitic elements in the PSP-NQS model. The large full dots indicate the five additional internal nodes.



The PSP-model includes the thermal (white) noise of these parasitic resistances.

$$S_{\rm R_G} = 4 \cdot k_{\rm B} \cdot T_{\rm KD} / R_{\rm gate} \tag{5.2}$$

$$S_{R_{\text{BULK}}} = 4 \cdot k_{\text{B}} \cdot T_{\text{KD}} / R_{\text{bulk}} \tag{5.3}$$

$$S_{\text{Rwell}} = 4 \cdot k_{\text{B}} \cdot T_{\text{KD}} / R_{\text{well}} \tag{5.4}$$

$$S_{\rm R_{\rm JUNS}} = 4 \cdot k_{\rm B} \cdot T_{\rm KD} / R_{\rm juns} \tag{5.5}$$

$$S_{R_{\text{JUND}}} = 4 \cdot k_{\text{B}} \cdot T_{\text{KD}} / R_{\text{jund}} \tag{5.6}$$

5.4 NQS and RF parameters

The PSP-NQS model has a few additional parameters, which are described in the tables below. The allowed values for the parameter **SWNQS** are 0, 1, 2, 3, 5, and 9. If **SWNQS** = 0, then NQS effects are switched off, i.e. the intrinsic MOS model is identical to the standard PSP-model (however, the parasitics-circuit is still in place). If **SWNQS** is nonzero, it indicates the number of collocation points to be used in the NQS-calculations. A higher value increases the accuracy, but leads to an increased computational burden.

5.4.1 Additional Parameters for global NQS model

No.	Name	Unit	Default	Min.	Max.	Description
0	SWNQS	_	0	0	9	Switch for NQS effects / number of collocation points
1	MUNQSO	_	1	_	_	Relative mobility for NQS modeling
2	RGO	Ω	10^{-3}	_	_	Gate resistance $R_{ m gate}$
3	RBULKO	Ω	10^{-3}	_	_	Bulk resistance $R_{\rm bulk}$
4	RWELLO	Ω	10^{-3}	_	_	Well resistance R_{well}
5	RJUNSO	Ω	10^{-3}	_	_	Source-side bulk resistance $R_{\rm juns}$
6	RJUNDO	Ω	10^{-3}	_	_	Drain-side bulk resistance $R_{ m jund}$

5.4.2 Additional Parameters for local NQS model

No.	Name	Unit	Default	Min.	Max.	Description
0	SWNQS	_	0	0	9	Switch for NQS effects / number of collocation points
1	MUNQS	_	1	0	_	Relative mobility for NQS modeling
2	RG	Ω	10^{-3}	10^{-6}	_	Gate resistance $R_{ m gate}$
3	RBULK	Ω	10^{-3}	10^{-6}	_	Bulk resistance R_{bulk}
4	RWELL	Ω	10^{-3}	10^{-6}	_	Well resistance $R_{\rm well}$
5	RJUNS	Ω	10^{-3}	10^{-6}	_	Source-side bulk resistance $R_{ m juns}$
6	RJUND	Ω	10^{-3}	10^{-6}	_	Drain-side bulk resistance $R_{ m jund}$

5.4.3 Geometrical Scaling Rules

Although the parasitic resistances are (in general) dependent on geometry, the actual form of this dependency will be strongly influenced by the device layout. For this reason, L and W dependence of these resistances is currently not included in PSP; the correct values must be supplied manually for each geometry.

The following (trivial) scaling-rules are included for the NQS-model.

$$MUNQS = MUNQSO$$

$$RG = RGO$$
(5.8)

$$RBULK = RBULKO (5.9)$$

$$RWELL = RWELLO (5.10)$$

$$RJUNS = RJUNSO (5.11)$$

$$RJUND = RJUNDO (5.12)$$

Note: After calculation of the local parameters, clipping is applied according to Section 5.4.2.

5.5 NQS Model Equations

In this section, several symbols and notations are used which were defined in Section 4. Moreover, y denotes the (normalized) position along the channel (y=0 is source side, y=1 is drain side), while x denotes the surface potential (normalized to ϕ_T^*) at a certain position.

5.5.1 Internal constants

Eqs. (5.13)–(5.18) are independent of bias conditions and time. Consequently, they have to be computed only once.

Note: In PSP 102.1 and before, only SWNQS = 0, 1, 2, 3, 5, 9 are allowed!

$$n = SWNQS + 1 \tag{5.13}$$

$$h = 1/n \tag{5.14}$$

The matrix A is a square $(n+1) \times (n+1)$ -matrix with elements $A_{i,j}$ $(0 \le i, j \le n)$, which are used in Eq. 5.36. They are computed using the following algorithm (adapted from [5]):

1. Initial values:

$$A_{i,j} = 0 \qquad \text{for } 0 \le i, j \le n \tag{5.15}$$

$$v_i = 0 \qquad \text{for } 0 \le i \le n \tag{5.16}$$

2. First loop:

$$p = 2 + v_{i-1}/2$$

$$v_{i} = -1/(2 \cdot p)$$

$$A_{i,i-1} = 1/h$$

$$A_{i,i} = -2/h$$

$$A_{i,i+1} = 1/h$$

$$A_{i,j} = \frac{1}{p} \cdot (3 \cdot A_{i,j}/h - A_{i-1,j}/2)$$
 for $j = 0 \dots n$ for $j = 0 \dots n$ for $j = 0 \dots n$

3. Second loop (back substitution):

$$A_{i,j} = v_i \cdot A_{i+1,j} + A_{i,j}$$
 for $j = 0 \dots n$
$$\begin{cases} \text{for } i = (n-1) \dots 0 \end{cases}$$
 (5.18)

5.5.2 Position independent quantities

The following quantities depend on the bias conditions, but are constant along the channel:

$$if x_{g} > 0 \begin{cases}
y_{m} = \frac{1}{2} \cdot \left(1 + \frac{\Delta \psi}{4 \cdot H}\right) \\
p_{d} = \frac{x_{gm}}{x_{g} - x_{m}} \\
G_{p} = G/p_{d}
\end{cases} (5.19)$$

$$if x_g \le 0 \begin{cases} y_m = 1/2 \\ p_d = 1 \\ G_p = G \end{cases}$$
 (5.20)

$$a_{\rm p} = 1 + G_{\rm p}/\sqrt{2}$$
 (5.21)

$$p_{\text{mrg}} = 10^{-5} \cdot a_{\text{p}}$$
 (5.22)

5.5.3 Position dependent surface potential and charge

Interpolated (quasi-static) surface potential along the channel:

$$\Psi(y) = x_{\rm m} + \frac{H}{\phi_{\rm T}^*} \cdot \left(1 - \sqrt{1 - \frac{2 \cdot \Delta \psi}{H} \cdot (y - y_{\rm m})}\right)$$

$$(5.23)$$

Normalized bulk-charge and its first two derivatives as functions of surface potential:

$$q_{\rm b}(x) = -\operatorname{sgn}(x) \cdot G_{\rm p} \cdot \sqrt{\exp(-x) + x - 1}$$
(5.24)

$$q_{\rm b}'(x) = \frac{G_{\rm p}^2 \cdot [1 - \exp(-x)]}{2 \cdot q_{\rm b}(x)}$$
(5.25)

$$q_{\rm b}''(x) = -q_{\rm b}'(x) - \frac{q_{\rm b}'(x)^2 - G_{\rm p}^2/2}{q_{\rm b}(x)}$$
(5.26)

Surface potential as a function of normalized inversion charge (note that these equations are identical to Eq. (4.152), despite the different notation and physical background):

$$\Pi(x_{\rm g}) = \begin{cases} y_{\rm g} = -x_{\rm g} \\ z = 1.25 \cdot y_{\rm g}/a_{\rm p} \\ \eta = \left[z + 10 - \sqrt{(z - 6)^2 + 64}\right]/2 \\ a = (y_{\rm g} - \eta)^2 + G_{\rm p}^2 \cdot (\eta + 1) \\ c = 2 \cdot (y_{\rm g} - \eta) - G_{\rm p}^2 \\ \tau = -\eta + \ln\left(a/G_{\rm p}^2\right) \\ y_0 = \sigma_1(a, c, \tau, \eta) \\ \Delta_0 = \exp(y_0) \\ \xi = 1 - G_{\rm p}^2 \cdot \Delta_0/2 \\ p = 2 \cdot (y_{\rm g} - y_0) + G_{\rm p}^2 \cdot (\Delta_0 - 1) \\ q = (y_{\rm g} - y_0)^2 + G_{\rm p}^2 \cdot (y_0 - \Delta_0 + 1) \\ \Pi = -y_0 - \frac{2 \cdot q}{p + \sqrt{p^2 - 4 \cdot q \cdot \xi}} \\ \Pi = \frac{x_{\rm g}}{a_{\rm p}} \\ \begin{cases} \hat{x}_{\rm g1} = x_1 + G \cdot \sqrt{\exp(-x_1) + x_1 - 1} \\ \bar{x} = \frac{x_{\rm g}}{a_{\rm p}} \cdot [1 + x_{\rm g} \cdot (x_1 \cdot a_{\rm p}/\hat{x}_{\rm g1} - 1)/\hat{x}_{\rm g1}] \\ x_0 = x_{\rm g} + G_{\rm p}^2/2 - G_{\rm p} \cdot \sqrt{x_{\rm g} + G_{\rm p}^2/4 - 1 + \exp(-\bar{x})} \end{cases}$$

$$\Delta_0 = \exp(-x_0)$$
if $x_{\rm g} > x_{\rm mrg}$

$$\begin{cases} \hat{x}_{\rm g} = x_{\rm g} + G_{\rm p}^2/2 - G_{\rm p} \cdot \sqrt{x_{\rm g} + G_{\rm p}^2/4 - 1 + \exp(-\bar{x})} \\ \lambda_0 = \exp(-x_0) \\ \xi = 1 - G_{\rm p}^2 \cdot \Delta_0/2 \\ p = 2 \cdot (x_{\rm g} - x_0) + G_{\rm p}^2 \cdot (1 - \Delta_0) \\ q = (x_{\rm g} - x_0)^2 - G_{\rm p}^2 \cdot (x_0 + \Delta_0 - 1) \\ \Pi = x_0 + \frac{2 \cdot q}{p + \sqrt{p^2 - 4 \cdot q \cdot \xi}} \end{cases}$$

$$X(x_{\rm g}, y_{\rm m}) = \Pi(x_{\rm g} + x_{\rm g}, y_{\rm g})$$
(5.28)

$$X(x_{\rm g}, q_{\rm inv}) = \Pi(x_{\rm g} + q_{\rm inv}/p_{\rm d})$$
 (5.28)

Auxiliary functions:

$$q(x) = -p_{d} \cdot (x_{g} - x) - q_{b}(x) \tag{5.29}$$

$$\psi(q, q_{x1}) = \frac{q}{q_{x1}} - 1 \tag{5.30}$$

$$\phi(q, q_{x1}, q_{x2}) = \left(1 - \frac{q \cdot q_{x2}}{q_{x1}^2}\right) / q_{x1} \tag{5.31}$$

Normalized right-hand-side of continuity equation:

$$f(x_{\rm g},q,q) = \frac{\partial q}{\partial x}(x_{\rm g}) = p_{\rm d} - q_{\rm b}'(x_{\rm g})$$

$$q_{x1} = \frac{\partial q}{\partial x}(x_{\rm g}) = p_{\rm d} - q_{\rm b}'(x_{\rm g})$$

$$q_{x2} = \frac{\partial^2 q}{\partial x^2}(x_{\rm g}) = q_{\rm b}''(x_{\rm g})$$

$$f_0 = \psi(q,q_{x1}) \cdot q'' + \phi(q,q_{x1},q_{x2}) \cdot q'^2$$

$$x_{y1} = \frac{\partial x_{\rm g}}{\partial y} = q'/q_{x1}$$

$$z_{\rm sat} = \begin{cases} \left(\theta_{\rm sat}^* \cdot \phi_{\rm T}^* \cdot x_{y1}\right)^2 & \text{for NMOS} \end{cases}$$

$$\frac{\left(\theta_{\rm sat}^* \cdot \phi_{\rm T}^* \cdot x_{y1}\right)^2}{1 + \theta_{\rm sat}^* \cdot \Delta \psi} & \text{for PMOS}$$

$$\zeta = \sqrt{1 + 2 \cdot z_{\rm sat}}$$

$$F_{\rm vsat} = 2/(1 + \zeta)$$

$$f = F_{\rm vsat} \cdot \left[f_0 - F_{\rm vsat} \cdot \frac{z_{\rm sat}}{\zeta} \cdot \psi(q, q_{x1}) \cdot (q'' + x_{y1}^2 \cdot q_{\rm b}''(x_{\rm g}))\right]$$

Normalization constant:

$$T_{\text{norm}} = \frac{\text{MUNQS} \cdot \phi_{\mathbf{T}}^* \cdot \beta}{C_{\text{OX}}^{\text{qm}} \cdot G_{\text{mob}} \cdot G_{\Delta L}}$$
(5.33)

5.5.4 Cubic spline interpolation

Using cubic spline interpolation, the spatial derivatives $\frac{\partial q_i}{\partial y}(t)$ and $\frac{\partial^2 q_i}{\partial y^2}(t)$ can be expressed as functions of the $q_i(t)$.

$$q_0'' = 0 (5.34)$$

$$q_n'' = 0 ag{5.35}$$

$$q_i'' = \sum_{j=0}^n A_{i,j} \cdot q_i$$
 for $1 \le i \le n-1$ (5.36)

$$q_i' = \frac{q_{i+1} - q_i}{h} - \frac{h}{6} \cdot (2 \cdot q_i'' + q_{i+1}'') \qquad \text{for } 1 \le i \le n - 1$$
(5.37)

5.5.5 Continuity equation

Initial value for the q_i ($0 \le i \le n$). These values are used for the DC operating point.

$$x_{i,0} = \Psi(i \cdot h) \tag{5.38}$$

$$q_{i,0} = q(x_{i,0}) (5.39)$$

Note: $x_{0,0} = x_s$ and $x_{n,0} = x_d$. Moreover, these values coincide with those in the quasi-static part of PSP.

The core of the NQS-model is the solution of q(y,t) from the charge continuity equation along the channel. By approximating the y-dependence by a cubic spline through a number of collocation points, the problem is reduced to solving the $q_i(t)$ from the following set of coupled differential equations.

$$\begin{cases}
\frac{\partial q_i}{\partial t}(t) + T_{\text{norm}} \cdot f\left(x_g, q_i(t), \frac{\partial q_i}{\partial y}(t), \frac{\partial^2 q_i}{\partial y^2}(t)\right) = 0 \\
q_i(0) = q_{i,0}
\end{cases}$$
for $1 \le i \le n - 1$

Note that the boundary points $q_0(t) = q(x_s) = q_{is}$ and $q_n(t) = q(x_d) = q_{id}$ remain fixed to their quasi-static values; they are not solved from the equation above.

The set of differential equations defined above is solved by the circuit simulator via the subcircuits shown in the left part of Fig. 5.1.

5.5.6 Non-quasi-static terminal charges

Once the q_i are known, the NQS terminal charges can be computed:

$$S_0 = \sum_{i=1}^{n-1} q_i \tag{5.41}$$

$$S_2 = \sum_{i=1}^{n-1} q_i'' \tag{5.42}$$

$$q_{\rm I}^{\rm NQS} = \int_0^1 q(y) \, \mathrm{d}y = h \cdot S_0 + \frac{h}{2} \cdot (u_0 + u_n) - \frac{h^3}{12} \cdot S_2$$
 (5.43)

$$U_0 = \sum_{i=1}^{n-1} i \cdot q_i \tag{5.44}$$

$$U_2 = \sum_{i=1}^{n-1} i \cdot q_i'' \tag{5.45}$$

$$q_{\rm D}^{\rm NQS} = \int_0^1 y \cdot q(y) \, \mathrm{d}y = h^2 \cdot U_0 + \frac{h^2}{6} \cdot [q_0 + (3n-1)u_n] - \frac{h^4}{12} \cdot U_2$$
 (5.46)

$$q_{\rm S}^{\rm NQS} = q_{\rm L}^{\rm NQS} - q_{\rm D}^{\rm NQS} \tag{5.47}$$

Currently, only **SWNQS** = 0, 1, 2, 3, 5, 9 are allowed. For odd values of **SWNQS** the gate charge is integrated along the channel using "Simpson's rule". If **SWNQS** = 2, "Simpson's 3/8-rule" is used.

• If **SWNQS** is odd (that is, n is even):

$$q_{G}^{NQS} = p_{d} \cdot \left[x_{g} - \frac{h}{3} \cdot \left(X(x_{g}, q_{0}) + 4 \cdot \sum_{i=1}^{n/2} X(x_{g}, q_{2i-1}) + \frac{1}{2} \cdot \sum_{i=1}^{n/2-1} X(x_{g}, q_{2i}) + X(x_{g}, q_{n}) \right) \right]$$
(5.48)

• If **SWNQS** = 2 (that is, n = 3):

$$q_{\rm G}^{\rm NQS} = p_{\rm d} \cdot \left[x_{\rm g} - \frac{3 \cdot h}{8} \cdot (X(x_{\rm g}, q_0) + 3 \cdot X(x_{\rm g}, q_1) + 3 \cdot X(x_{\rm g}, q_2) + X(x_{\rm g}, q_3)) \right]$$
(5.49)

Convert back to conventional units:

$$Q_{\rm S}^{\rm NQS} = C_{\rm OX}^{\rm qm} \cdot \phi_{\rm T}^* \cdot q_{\rm S}^{\rm NQS} \tag{5.50}$$

$$Q_{\rm D}^{\rm NQS} = C_{\rm OX}^{\rm qm} \cdot \phi_{\rm T}^* \cdot q_{\rm D}^{\rm NQS} \tag{5.51}$$

$$Q_{\rm G}^{\rm NQS} = C_{\rm OX}^{\rm qm} \cdot \phi_{\rm T}^* \cdot q_{\rm G}^{\rm NQS} \tag{5.52}$$

$$Q_{\rm B}^{\rm NQS} = -(Q_{\rm S}^{\rm NQS} + Q_{\rm D}^{\rm NQS} + Q_{\rm G}^{\rm NQS})$$
 (5.53)

Section 6

Embedding

6.1 Model selection

Circuit simulators have different ways for the user to determine which model must be used for simulation. Typically, model selection is either done by *name* or by assigning a value to the parameter **LEVEL**. The method to be used is prescribed by the circuit simulator vendor.

If selection is done by name, the value of the parameter **LEVEL** is generally ignored. When Verilog-A code is used, model selection is always done by name.

For the SiMKit and the Verilog-A code provided by the PSP model developers, the method and values to be used are given in the table below. For other implementations, the method/value provided by the circuit simulator vendor is to be used.

Simulator	Model selection by	Global (geom.)	Global (binning)	Local
Spectre	name	psp1020	psp1021	psp102e
Pstar	LEVEL	1020	1021	102
ADS	name	psp1020	psp1021	psp102e
Verilog-A	name	PSP102VA	PSP102BVA	PSP102EVA

6.2 Case of parameters

Throughout this document, all parameter names are printed in uppercase characters. Similarly, in the Verilog-A code provided by the PSP model developers, the parameters are in upper case characters. However, in other PSP implementations a different choice can be made. For example, the parameter names may be in lowercase characters (possibly first character capitalized) if this is conform the conventions of the circuit simulator.

6.3 Embedding PSP in a Circuit Simulator

In CMOS technologies both n- and p-channel MOS transistors are supported. It is convenient to use the same set of equations for both types of transistor instead of two separate models. This is accomplished by mapping a p-channel device with its bias conditions and parameter set onto an equivalent n-channel device with appropriately changed bias conditions (i.e. currents, voltages and charges) and parameters. In this way both types of transistor can be treated internally as an n-channel transistor. Nevertheless, the electrical behavior of electrons and holes is not exactly the same (e.g., the mobility and tunneling behavior), and consequently slightly different equations have to be used in case of n- or p-type transistors.

Designers are used to the standard terminology of source, drain, gate and bulk. Therefore, in the context of

a circuit simulator it is traditionally possible to address, say, the drain of MOST number 17, even if in reality the corresponding source is at a higher potential (n-channel case). More strongly, most circuit simulators provide for model evaluation values for $V_{\rm DS}$, $V_{\rm GS}$, and $V_{\rm SB}$ based on an a priori assignment of source, drain, and bulk, independent of the actual bias conditions. Since PSP assumes that saturation occurs at the drain side of the MOSFET, the basic model cannot cope with bias conditions that correspond to $V_{\rm DS} < 0$. Again a transformation of the bias conditions is necessary. In this case, the transformation corresponds to internally reassigning source and drain, applying the standard electrical model, and then reassigning the currents and charges to the original terminals. In PSP care has been taken to preserve symmetry with respect to drain and source at $V_{\rm DS} = 0$. In other words, no singularities will occur in the higher-order derivatives at $V_{\rm DS} = 0$.

In detail, for correct embedding of PSP into a circuit simulator, the following procedure—illustrated in Fig. 6.1—is followed. It is assumed that the simulator provides the nodal potentials $V_{\rm D}^e$, $V_{\rm G}^e$, $V_{\rm S}^e$ and $V_{\rm B}^e$ based on an a priori assignment of drain, gate, source and bulk.

- Step 1 The voltages $V'_{\rm DS}$, $V'_{\rm GS}$, and $V'_{\rm SB}$ are calculated from the nodal potentials provided by the circuit simulator. In the same step, the value of the parameter **TYPE** is used to deal with the polarity of the device. From here onwards, all transistors can be treated as n-channel devices.
- **Step 2** Depending on the sign of V'_{DS} , 'source-drain interchange' is performed. At this level, the voltages comply to all the requirements for input quantities of PSP.
- **Step 3** All the internal output quantities (i.e. channel current, weak-avalanche current, gate current, nodal charges, and noise-power spectral densities) are evaluated using the standard PSP equations (Section 4) and the internal voltages.
- Step 4 The internal output quantities are corrected for a possible source-drain interchange.
- **Step 5** External output are corrected for a possible *p*-channel transformation and **MULT** is applied. The quantities of the intrinsic MOSFET and the junctions are combined.

In general, separate parameter sets are used for n- and p-channel transistors, which are distinguished by the value of **TYPE**. As a consequence, the changes in the parameter values necessary for a p-channel type transistor are normally already included in the parameter sets on file. The changes should therefore not be included in the simulator.

6.4 Integration of JUNCAP2 in PSP

Introduction

The JUNCAP2 model 200.2 is an integral part of PSP 102.1. In addition, it is available as a stand-alone model. A complete description of the JUNCAP2-model (including all model equations) can be found in the documentation of JUNCAP2's stand alone version. In this section, only the integration of JUNCAP2 in PSP is described.

Topology

In a MOS transistor, there are two junctions: one between source and bulk, and one between drain and bulk. In case of an n-channel MOSFET, the junction anode corresponds to the MOSFET bulk terminal, and the junction cathodes correspond to the source and the drain. In case of a p-channel MOSFET, it is the other way around: now the junction cathode corresponds to the MOSFET bulk terminal, and the junction anodes correspond to the source and the drain. The connections are schematically given in Fig. 6.2. In PSP, this change of junction terminal connections in case of a p-MOSFET is handled automatically via the **TYPE** parameter.

In most cases, the MOSFET is operated in such a way that the junctions are either biased in the reverse mode of operation or not biased at all. In some applications, however, the source-bulk junction has a small forward bias. This is also the case in partially depleted SOI (PDSOI).

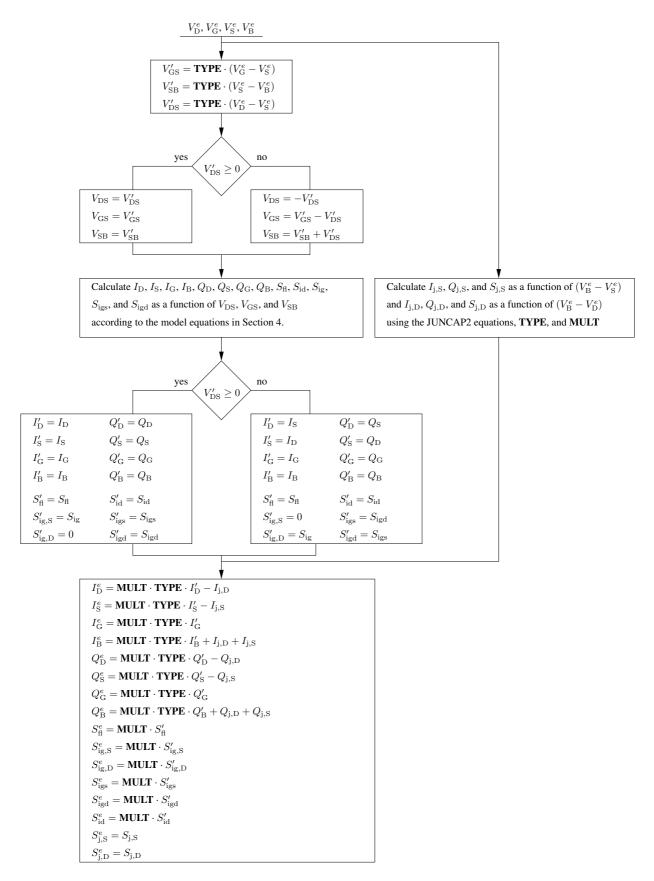


Figure 6.1: Schematic overview of source-drain interchange and handling of **TYPE** and **MULT**. Note that **TYPE** and **MULT** are included in the JUNCAP2 model equations.

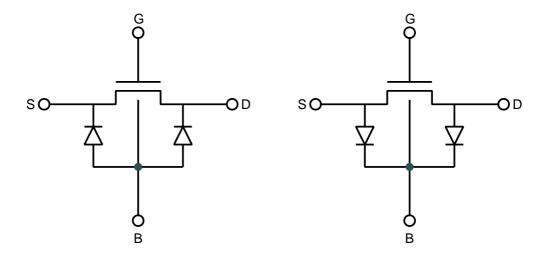


Figure 6.2: Topology of the PSP model. *Left: n*-channel MOSFET; *Right: p*-channel MOSFET. In PSP, the correct diode polarity is automatically chosen via the **TYPE**-parameter.

As indicated in Fig. 6.1, the interchange of source and drain for $V_{\rm DS} < 0$ (as explained above for the intrinsic MOS model) does *not* apply to the junctions. For example, **ABDRAIN** always refers to junction between the bulk and the terminal known as 'drain' to the simulator, independent of the sign of $V_{\rm DS}$.

Global and local model level

As explained in the introduction, the PSP model has a local and a global level. The JUNCAP2 model is a geometrically scaled model, i.e. it is valid for a range of junction geometries (as described by the geometrical parameters **AB**, **LS**, and **LG**). It has turned out that it is very unnatural to create a local parameter set for JUNCAP2, valid for one particular junction geometry: such a parameter set would have as many parameters as the global parameter set, and would be of no use. (Note that, in contrast, the local model for the intrinsic MOSFET is very useful in, e.g., parameter extraction; this is not the case for JUNCAP2.)

Therefore, the JUNCAP2 model is connected in exactly the same way to both the local and global model levels of PSP. That means that the resulting PSP local model is valid for a MOSFET with one particular channel width and length, but with arbitrary junction geometry.

Parameters

Both junctions in the MOSFET are modeled with the same set of JUNCAP2 parameters. In the PSP model, the geometrical parameters **AB**, **LS**, and **LG** need to be specified for both source and drain. They will be denoted as **ABSOURCE**, **LSSOURCE**, and **LGSOURCE** for the source junction, and **ABDRAIN**, **LSDRAIN**, and **LGDRAIN** for the drain junction. For compatibility with BSIM instance parameters, there is also an option to use **AS**, **AD**, **PS**, and **PD**. The complete list of instance parameters (PSP and JUNCAP2) can be found in Sections 2.5.1 and 2.5.2.

The parameter **MULT** is merged with the parameter **MULT** of the intrinsic MOSFET model. In other words, both intrinsic currents, charges, and noise as well as junction currents, charges and noise are multiplied by one single parameter **MULT**. Beside **MULT**, also the parameters **DTA** and **TYPE** are shared by the intrinsic MOSFET model and the junction model. For clarity, we mention here that the reference temperatures of the intrinsic MOSFET model and junction model are *not* merged; they each have their own value and name (**TR** and **TRJ**, respectively). The currents, charges and spectral noise densities of the source and drain junctions are labeled $I_{\rm j,S}$, $Q_{\rm j,S}$, $S_{\rm j,S}$, $I_{\rm j,D}$, $I_{\rm j,D}$, and $I_{\rm j,D}$ in Fig. 6.1.

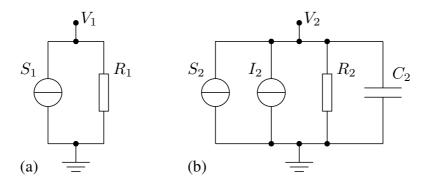


Figure 6.3: The two subcircuits used in PSP's Verilog-A implementation to model the correct frequency dependence of induced gate noise and its correlation with the channel thermal noise.

6.5 Verilog-A versus C

As mentioned in Section 1.3, two implementations of the PSP-model are distributed: in Verilog-A language and in C-language (as part of the SiMKit). The C-version is automatically generated from the Verilog-A version by a software package called ADMS [1]. This procedure guarantees that the two implementations contain identical model equations.

Nevertheless, there are a few minor differences between the two, which are due to certain limitations of either the Verilog-A language or the circuit simulators supported in the SiMKit-framework. These differences are described below.

6.5.1 Implementation of GMIN

In both implementations, there is an additional term in Eqs. (4.177) and (4.178), resulting in

$$I_{\rm D} = I_{\rm DS} + I_{\rm avl} - I_{\rm GDov} - I_{\rm GCD} + I_{\rm gidl} + G_{\rm min} \cdot V_{\rm DS}$$

$$(6.1)$$

and

$$I_{\rm S} = -I_{\rm DS} - I_{\rm GSov} - I_{\rm GCS} + I_{\rm gisl} - G_{\rm min} \cdot V_{\rm DS}. \tag{6.2}$$

In the SiMKit, G_{\min} is a variable which is accessible by the circuit simulator. This allows the circuit simulator to improve the convergence properties of a circuit by making use of so-called ' G_{\min} -stepping'.

In the Verilog-A version of PSP, G_{\min} is set to a fixed value $G_{\min} = 1 \cdot 10^{-15} \; \mathrm{S}^{1}$

6.5.2 Implementation of the noise-equations

First, the Verilog-A implementation of the noise equations is described in this section. Then, the C-implementation is derived from this by a sequence of approximations.

Verilog-A

In Verilog-A, the possibilities to directly model the frequency-dependence of noise spectral density are limited. Moreover, the only way to include correlation between noise sources is by using (extra) internal nodes. Consequently, the calculation for the description of thermal noise in the channel, induced gate noise, and their correlation is implemented using the subcircuits depicted in Fig. 6.3. The first subcircuit (a) contains a parallel

 $^{^{1}}$ If supported by the circuit simulator, Verilog-A version 2.2 allows the value of G_{\min} to be accessed by the circuit simulator. Once this feature is generally available in Verilog-A compilers, it will be included in PSP as well.

connection of a white noise current source S_1 and a resistor R_1 . The voltage over the elements is denoted by V_1 . The second subcircuit (b) contains a parallel connection of a voltage-controlled current source I_2 , a white-noise current source S_2 , a resistor S_2 , and a capacitor S_2 . The nodal voltage is S_2 . The parameters of these components are given in the table below.

Name	Component	Quantity	Value
R_1	Resistor	Resistance	1 Ω
R_2	Resistor	Resistance	1 Ω
S_1	White noise source	Noise current spectral density	$C_{ m igid}$
S_2	White noise source	Noise current spectral density	$S_{\mathrm{ig}}^{0} \cdot (1 - C_{\mathrm{igid}})$
C_2	Capacitor	Capacitance	$m_{ m ig} \cdot C_{ m Geff}$
I_2	Voltage-controlled current source	Current	$-\sqrt{S_{\mathrm{ig}}^0} \cdot V_1$

The values of $m_{\rm ig}$ and $C_{\rm Geff}$ are given by Eqs. (4.206) and (4.209), respectively. Furthermore,

$$S_{\rm ig}^0 = \frac{N_{\rm T}}{m_{\rm ig}} \tag{6.3}$$

and

$$C_{\text{igid}} = \frac{m_{\text{igid}}}{\sqrt{m_{\text{ig}} \cdot m_{\text{id}}}},\tag{6.4}$$

where $m_{\rm id}$ and $m_{\rm igid}$ are given by Eqs. (4.207) and (4.211).

Subcircuit (a) contains a single white noise source, from which the correlated parts of the channel noise and induced gate noise are derived. Now, the thermal noise in the channel is modeled by two contributions:

- 1. An uncorrelated white noise source with current spectral density $S_{\rm id} \cdot (1 C_{\rm igid})$.
- 2. A white noise source with spectral power density $S_{id} \cdot C_{igid}$ which is fully correlated with S_1 .

Subcircuit (b) contains a current noise source S_2 and a voltage controlled current source I_2 , the current of which is controlled by V_1 . The result is that I_2 acts as white noise source which is fully correlated with S_1 (and thus with the second component of the channel noise above). Summarizing, the induced gate noise is modeled by two contributions:

- 1. An uncorrelated white noise source with current spectral density $S_{ig}^0 \cdot (1 C_{igid})$.
- 2. A white noise source with current spectral density $S_{ig}^0 \cdot C_{igid}$, which is fully correlated with S_1 .

These two noise sources in subcircuit (b) are in series with a parallel combination of a resistor and a capacitor. The noise in the current through C_2 has the correct frequency dependence and is used to describe the induced gate noise in the MOSFET.

The total noise current spectral density of the two noise sources S_2 and I_2 is equal to $S_{ig}^0 \cdot (1 - C_{igid}) + S_{ig}^0 \cdot C_{igid} = S_{ig}^0$. Therefore, the total noise spectral density of the current through the capacitor C_2 is given by

$$S_{ig} = \left| \frac{j \cdot \omega \cdot C_2 \cdot R_2}{1 + j \cdot \omega \cdot C_2 \cdot R_2} \right|^2 \cdot S_{ig}^0, \tag{6.5}$$

(where $\omega=2\cdot\pi\cdot f_{\mathrm{op}}$ and $j=\sqrt{-1}$) which is indeed exactly equivalent to Eq. (4.210).

Similarly, the cross-correlation noise spectrum of (i) the current through C_2 induced by noise source I_2 and (ii) the correlated part of the channel noise is given by

$$S_{\text{igid}} = \left(\frac{j \cdot \omega \cdot C_2 \cdot R_2}{1 + j \cdot \omega \cdot C_2 \cdot R_2} \cdot \sqrt{S_{\text{ig}}^0} \cdot C_{\text{igid}}\right) \cdot \left(\sqrt{S_{\text{id}}} \cdot C_{\text{igid}}\right), \tag{6.6}$$

which is, in turn, equivalent to Eq. (4.212).

This shows that the implementation of PSP's noise model in Verilog-A naturally yields the desired correlations and frequency dependence. However, it is at the cost of two additional internal nodes.

Note once more that the equations in Section 4.2.20 exactly reflect the results of the Verilog-A implementation described above.

SiMKit C-code

Contrary to the limitation of Verilog-A language, most circuit simulators are able to directly deal with correlated and frequency dependent noise—without the use of additional internal nodes. In order to minimize the simulation time of the model, C-implementations should therefore avoid the use of such internal nodes whenever possible.

In the frequency dependence of S_{ig} and S_{igid} one can roughly distinguish two regions: a frequency dependent part at low frequencies and a constant part at high frequencies. The transition between the two regions occurs at

$$f_{\text{cross}} = \frac{1}{2 \cdot \pi \cdot C_{\text{Geff}} \cdot m_{\text{ig}}}.$$
(6.7)

Eqs. (4.210) and (4.212) ensure a smooth transition between the two regions.

As mentioned before, circuit simulators are typically able to deal with correlated noise without using additional internal nodes. However, to achieve this, two approximations are made:

- 1. The frequency dependence is split in a frequency dependent (power law; $\propto f_{\rm op}^2$ for $S_{\rm ig}$ and $\propto f_{\rm op}$ for $S_{\rm igid}$) and a frequency independent part.
- 2. Only the imaginary part of $S_{\rm igid}$ is considered.

Applying these approximations, it is found from Eq. (4.210) that

$$S_{ig} = \begin{cases} \frac{N_{T}}{m_{ig}} \cdot \left(\frac{f_{op}}{f_{cross}}\right)^{2} & \text{for } f_{op} \leq f_{cross} \\ \frac{N_{T}}{m_{ig}} & \text{for } f_{op} > f_{cross} \end{cases}$$

$$(6.8)$$

Similarly, the imaginary part of Eq. (4.212) is approximated as

$$\operatorname{Im}(S_{\text{igid}}) = \begin{cases} \frac{N_{\text{T}}}{m_{\text{ig}}} \cdot m_{\text{igid}} \cdot \frac{f_{\text{op}}}{f_{\text{cross}}} & \text{for } f_{\text{op}} \leq f_{\text{cross}} \\ \frac{N_{\text{T}}}{m_{\text{ig}}} \cdot m_{\text{igid}} & \text{for } f_{\text{op}} > f_{\text{cross}} \end{cases}$$

$$(6.9)$$

while $Re(S_{igid})$ is set to zero for all frequencies.

In the SiMKit-implementation of PSP, the values above are passed to the circuit simulator to be used in noise calculations.

Section 7

Parameter extraction

The parameter extraction strategy for PSP consists of four main steps:

- 1. Measurements
- 2. Extraction of local parameters at room temperature
- 3. Extraction of temperature scaling parameters
- 4. Extraction of geometry scaling (global) parameters

The above steps will be briefly described in the following sections. Note that the description of the extraction procedure is not 'complete' in the sense that only the most important parameters are discussed and in cases at hand it may be advantageous (or even necessary) to use an adapted procedure.

Throughout this section, bias and current conditions are given for an n-channel transistor only; for a p-channel transistor, all voltages and currents should be multiplied by -1.

As explained in the introduction, the hierarchical setup of PSP (local and global level) allows for the two-step parameter extraction procedure described in this section; this is the recommended method of operation. Nevertheless, it is possible to skip the first steps and start extracting global parameters directly. This procedure is not described here, but the directions below may still be useful.

7.1 Measurements

The parameter extraction routine consists of six different DC-measurements (two of which are optional) and two capacitance measurements.¹ Measurement V and VI are only used for extraction of gate-current, avalanche, and GIDL/GISL parameters.

```
• Measurement I ("idvg"): I_{\rm D} vs. V_{\rm GS} V_{\rm GS}=0\ldots V_{\rm sup} (with steps of maximum 50 mV). V_{\rm DS}=25 or 50 mV V_{\rm BS}=0\ldots -V_{\rm sup} (3 or more values)
```

```
• Measurement II ("idvgh"): I_{\rm D} vs. V_{\rm GS} V_{\rm GS}=0\ldots V_{\rm sup} (with steps of maximum 50 mV). V_{\rm DS}=V_{\rm sup} V_{\rm BS}=0\ldots -V_{\rm sup} (3 or more values)
```

 $^{^1}$ The bias conditions to be used for the measurements are dependent on the supply voltage of the process. Of course it is advisable to restrict the range of voltages to this supply voltage $V_{\rm sup}$. Otherwise physical effects atypical for normal transistor operation—and therefore less well described by PSP—may dominate the characteristics.

```
• Measurement III ("idvd"): I_{\rm D} vs. V_{\rm DS} V_{\rm GS}=0\ldots V_{\rm sup} (3 or more values) V_{\rm DS}=0\ldots V_{\rm sup} (with steps of maximum 50 mV). V_{\rm BS}=0 V
```

• Measurement IV ("idvdh", optional): $I_{\rm D}$ vs. $V_{\rm DS}$ $V_{\rm GS}=0\ldots V_{\rm sup}$ (3 or more values) $V_{\rm DS}=0\ldots V_{\rm sup}$ (with steps of maximum 50 mV). $V_{\rm BS}=-V_{\rm sup}$

```
• Measurement V ("igvg"): I_{\rm G} and I_{\rm B} vs. V_{\rm GS} V_{\rm GS}=-V_{\rm sup}\dots V_{\rm sup} (with steps of maximum 50 mV). V_{\rm DS}=0\dots V_{\rm sup} (3 or more values) V_{\rm BS}=0 V
```

• Measurement VI ("igvgh", optional): $I_{\rm G}$ and $I_{\rm B}$ vs. $V_{\rm GS}$ $V_{\rm GS} = -V_{\rm sup} \dots V_{\rm sup}$ (with steps of maximum 50 mV). $V_{\rm DS} = 0 \dots V_{\rm sup}$ (3 or more values) $V_{\rm BS} = -V_{\rm sup}$

```
• Measurement VII ("cggvg"): C_{\rm GG} vs. V_{\rm GS} V_{\rm GS}=-V_{\rm sup}\dots V_{\rm sup} (with steps of maximum 50 mV). V_{\rm DS}=0 V V_{\rm BS}=0 V
```

```
• Measurement VIII ("ccgvg"): C_{\rm CG} vs. V_{\rm GS} V_{\rm GS}=-V_{\rm sup}\dots V_{\rm sup} (with steps of maximum 50 mV). V_{\rm DS}=0 V V_{\rm BS}=0 V
```

For the extraction procedure, the transconductance $g_{\rm m}$ (for Measurement I and II) and the output conductance $g_{\rm DS}$ (for Measurement III and IV) are obtained by numerical differentiation of the measured I-V-curves. Furthermore, $I_{\rm min}$ is the smallest current which can reliably measured by the system (noise limit) and $I_{\rm T}$ is defined as 10% of the largest measured value of $|I_{\rm D}|$ in Measurement I. The latter will be used to make a rough distinction between the subthreshold and superthreshold region.

The channel-to-gate capacitance $C_{\rm CG}$ in Measurement VIII is the summation of the drain-to-gate capacitance $C_{\rm DG}$ and the source-to-gate capacitance $C_{\rm SG}$ (i.e., source and drain are short-circuited); it is needed to extract overlap capacitance parameters.

The local parameter extraction measurements I through VI have to be performed at room temperature for every device. In addition, capacitance measurements VII and VIII need to be performed for at least a long/wide and a short/wide (i.e., $L=L_{\rm min}$) transistor (at room temperature). Furthermore, for the extraction of temperature scaling parameters measurements I, III, and V have to be performed at different temperatures (at least two extra, typically $-40\,^{\circ}{\rm C}$ and $125\,^{\circ}{\rm C}$) for at least a long wide and a short wide transistor.

7.2 Extraction of local parameters at room temperature

General remarks

The simultaneous determination of *all* local parameters for a specific device is not advisable, because the value of some parameters can be wrong due to correlation and suboptimization. Therefore it is more practical to

split the parameters into several small groups, where each parameter group can be determined using specific measurements. In this section, such a procedure will be outlined.

The extraction of local parameters is performed for every device. In order to ensure that the temperature scaling relations do not affect the behavior at room temperature, the reference temperature **TR** should be set equal to room temperature.

Before starting the parameter extraction procedure, one should make sure that **SWIGATE**, **SWIMPACT**, **SWGIDL**, **SWJUNCAP**, and **TYPE** are set to the desired value. Moreover, **QMC** should be set to 1, in order to include quantum mechanical corrections in the simulations.

It is not the case that all local parameters are extracted for every device. Several parameters are only extracted for one or a few devices, while they are kept fixed for all other devices. Moreover, a number of parameters can generally be kept fixed at their default values and need only occasionally be used for fine-tuning in the optimization procedure. Details are given later in this section.

As a special case, it is generally not necessary to extract values for \mathbf{AX} . In stead, they can be calculated from Eq. (3.53), using $\mathbf{AXO} \sim 18$ and $\mathbf{AXL} \sim 0.25$. It may be necessary to tune the latter value such that the value of \mathbf{AX} is between 2 and 3 for the shortest channel in the technology under study.

It is recommended to start the extraction procedure with the long(est) wide(st) device, then the shortest device with the same width, followed by all remaining devices of the same width in order of decreasing length. Then the next widest-channel devices are extracted, where the various lengths are handled in the same order. In this way, one works ones way down to the narrowest channel devices.

AC-parameters

Some parameters (such as **TOX** and **NP**) that do affect the DC-behavior of a MOSFET can only be extracted accurately from C-V-measurements.² This should be done before the actual parameter extraction from DC-measurements is started. In Tables 7.1 and 7.2 the extraction procedure for the AC-parameters is given.

Table 7.1: AC-parameter extraction procedure for a long channel MOSFET.

Step	Optimized parameters	Fitted on	Abs./Rel.	Conditions
1	VFB,NEFF, DPHIB, NP, COX	VII: $C_{\rm GG}$	Relative	_
2	Repeat Step 1			

Table 7.2: AC-parameter extraction procedure for a short channel MOSFET. The values of **VFB** and **NP** are taken from the long-channel case.

Step	Optimized parameters	Fitted on	Abs./Rel.	Conditions
1	NEFF, DPHIB, COX	VII: C_{GG}	Relative	_
2	CGOV, NOV	VIII: $C_{\rm CG}$	Relative	$V_{\rm GS} < 0$
3	Repeat Steps 1 and 2			

Starting from the default parameter set and setting **TOX** to a reasonable value (as known from technology), **VFB**, **NEFF**, **DPHIB**, **COX**, and **NP** can be extracted from $C_{\rm GG}$ in Measurement VII for a long, wide device.

Next, **NOV** and **CGOV** can be extracted from C_{CG} in Measurement VIII for a short, wide device (see also Table 7.1), where **VFB** and **NP** are taken from the long channel case. In general, one can assume **TOXOV** = **TOX**.

The value of **TOX** can be determined from $\mathbf{COX} = \epsilon_{ox} \cdot L \cdot W/\mathbf{TOX}$. If the device is sufficiently long and wide, drawn length and width can be used in this formula. Even better, if Measurement VII is available for a

²Although parameter **NOV** can be determined from overlap gate current, it is nonetheless more accurately determined from Measurement VIII.

Table 7.3: Initial values for local parameter extraction for a *long*-channel device. For parameters which are not listed in this table, the default value (as given in Section 2.5.6) can be used as initial value.

Parameter	Initial value
BETN	$0.03 \cdot W/L$
RS	0
THESAT	0.1
AX	12
A1	0

few short/wide devices of different lengths, one can extract **TOX** and ΔL from a series of extracted values of **COX** vs. $L_{\rm draw}$.

Some remarks:

- If C-V-measurements are not available, one could revert to values known from the fabrication process. Note that **TOX** and **TOXOV** are *physical* oxide thicknesses; poly-depletion and quantum-mechanical effects are taken care of by the model. If the gate dielectric is not pure SiO₂, one should manually compensate for the deviating dielectric constant.
- In general, **VFB** and **NP** can be assumed independent of channel length and width (so, the long/wide-channel values can be used for all other devices as well). Only if no satisfactory fits are obtained, one could allow for a length dependence (for **NP**) or length *and* width dependence (for **VFB**). Then, one should proceed by extracting **VFB** and/or **NP** from capacitance measurements for various channel geometries, fit Eq. (3.11) / Eq. (3.25) to the result and use interpolated values in the DC parameter extraction procedure.
- The value of parameter **TOX** profoundly influences both the DC- and AC-behavior of the PSP-model and thus the values of many other parameters. It is therefore very important that this parameter is determined (as described above) and *fixed* before the rest of the extraction procedure is started.

If desired (e.g., for RF-characterization), parameters for several parasitic capacitances (gate-bulk overlap, fringe capacitance, etc.) can be extracted as well (**CGBOV** and **CFR**). However, this requires additional capacitance measurements.

The obtained values of VFB, TOX, TOXOV, NP, and NOV can now be used in the DC-parameter extraction procedure. The above values of NEFF and DPHIB can be disregarded; they will be determined more accurately from the DC-measurements.

DC-parameters

Before the optimization is started a reasonably good starting value has to be determined, both for the parameters to be extracted and for the parameters which remain constant. For most parameters to be extracted for a *long* channel device, the default values from Section 2.5.6 can be taken as initial values. Exceptions are given in Table 7.3. Starting from these values, the optimization procedure following the scheme below is performed. This method yields a proper set of parameters after the repetition indicated as the final step in the scheme. Experiments with transistors of several processes show that repeating those steps more than once is generally not necessary.

For an accurate extraction of parameter values, the parameter set for a long-channel transistor has to be determined first. In the long-channel case most of the mobility related parameters (i.e. MUE and THEMU) and the gate tunneling parameters (GCO, GC2, and GC3) are determined and subsequently fixed for the shorter-channel devices.

Table 7.4: DC-parameter extraction procedure for a long-channel MOSFET. The parameters VFB, TOX, TOXOV, NP, and NOV must be taken from *C-V*-measurements. The optimization is either performed on the absolute or relative deviation between model and measurements, as shown in the table.

Step	Optimized parameters	Fitted on	Abs./Rel.	Conditions
1	NEFF, BETN, MUE, THEMU ^a	I: I_{D}	Absolute	_
2	NEFF, DPHIB, CT	I: I_{D}	Relative	$I_{ m min} < I_{ m D} < I_{ m T}$
3	MUE , $THEMU^a$, CS , $XCOR$, $BETN$	I: $I_{\mathrm{D}}, g_{\mathrm{m}}$	Absolute	_
4	THESAT	III: $I_{ m D}$	Absolute	_
5	ALP, ALP1, ALP2, VP ^a , (AX)	III: g_{DS}	Relative	_
6	THESAT	II: I_{D}	Absolute	_
7	IGINV, GC2 ^a , GC3 ^a	V: <i>I</i> _G	Relative	$I_{ m G} > I_{ m min}$
8	$IGOV, (GCO^a)$	V: <i>I</i> _G	Relative	$V_{ m GS} < 0 \ m V, I_{ m G} < -I_{ m min}$
9	$A1, A2^a, A3$	V: <i>I</i> _B	Relative	$V_{ m GS} > 0$ V, $I_{ m B} < -I_{ m min}$
10	A4	$ ext{VI:} I_{ ext{B}}$	Relative	$V_{ m GS} > 0$ V, $I_{ m B} < -I_{ m min}$
11	AGIDL, BGIDL ^a	V: <i>I</i> _B	Relative	$V_{ m GS} < 0$ V, $I_{ m B} < -I_{ m min}$
12	CGIDL ^a	$VI:I_{ m B}$	Relative	$V_{ m GS} < 0$ V, $I_{ m B} < -I_{ m min}$
13	Repeat Steps 2 – 12			

^aOnly extracted for the widest long channel device and fixed for all other geometries.

In Table 7.4 the complete DC extraction procedure for long-channel transistors is given. The magnitude of the simulated $I_{\rm D}$ and the overall shape of the simulated $I_{\rm D}$ - $V_{\rm GS}$ -curve is roughly set in Step 1. Next the parameters NEFF, DPHIB, and CT—which are important for the subthreshold behavior—are optimized in Step 2, neglecting short-channel effects such as drain-induced barrier-lowering (DIBL). After that, the mobility parameters are optimized in Step 3, neglecting the influence of series-resistance. In Step 4 a preliminary value of the velocity saturation parameter is obtained, and subsequently the conductance parameters ALP, ALP1, ALP2, and VP are determined in Step 5. A more accurate value of THESAT can now be obtained using Step 6. The gate current parameters are determined in Steps 7 and 8, where it should be noted that GCO should only be extracted if the influence of gate-to-bulk tunneling is visible in the measurements. This is usually the case if $V_{\rm sup} \gtrsim |{\rm VFB}|$. This is followed by the weak-avalanche parameters in Step 9 and (optionally) 10, and finally, the gate-induced leakage current parameters are optimized in Step 11 and (optionally) 12.

For short-channel devices, the extracted values of the next-longer device can be used as initial values. This includes the carrier mobility parameters and the gate tunneling probability factors of the long-channel device, which are subsequently kept fixed. Next, the extraction procedure as given in Table 7.5 is executed, which applies to all devices that are not 'long'.

Note that—once the value of **THESATG** and **THESATB** have been determined from the shortest widest channel device—steps 4, 5, and 6 of the long-channel extraction procedure (Table 7.4) must be repeated to obtain updated values for **THESAT**, **ALP1**, and **ALP2**.

7.3 Extraction of Temperature Scaling Parameters

For a specific device, the temperature scaling parameters can be extracted after determination of the local parameters at room temperature. In order to do so, measurements I, II and IV need to be performed at various temperature values (at least two values different from room temperature, typically $-40\,^{\circ}\text{C}$ and $125\,^{\circ}\text{C}$), at least for a long wide device and a short wide device. If the reference temperature TR has been chosen equal to room temperature (as recommended in Section 7.2), the modeled behavior at room temperature is insensitive to the value of the temperature scaling parameters. As a first-order estimate of the temperature scaling parameter values, the default values as given in Section 2.5.6 can be used. Again the parameter extraction scheme is

Table 7.5: DC-parameter extraction procedure for a short-channel MOSFET. Parameters MUE, THEMU, VP, GCO, GC2, GC3, A2, A4, BGIDL, and CGIDL are taken from the corresponding long-channel case. The optimization is either performed on the absolute or relative deviation between model and measurements, as indicated in the table.

Step	Optimized parameters	Fitted on	Abs./Rel.	Conditions
1	NEFF, DPHIB, BETN, RS ^a	I: I_{D}	Absolute	_
2	NEFF, DPHIB, CT	I: I_{D}	Relative	$I_{ m min} < I_{ m D} < I_{ m T}$
3	BETN, RS ^a , XCOR	I: $I_{\rm D}, g_{\rm m}$	Absolute	_
4	THESAT	III: $I_{ m D}$	Absolute	_
5	ALP, ALP1, ALP2, CF, (AX)	III: g_{DS}	Relative	_
6	\mathbf{CFB}^b	IV: g_{DS}	Relative	_
7	THESAT, THESATG b , THESATB b	II: $I_{\rm D}$, $g_{\rm m}$	Absolute	_
8	IGINV, IGOV	V: <i>I</i> _G	Relative	$ I_{ m G} > I_{ m min}$
9	A1, A3	$V:I_{ m B}$	Relative	$V_{ m GS} > 0$ V, $I_{ m B} < -I_{ m min}$
10	AGIDL	V: <i>I</i> _B	Relative	$V_{ m GS} < 0$ V, $I_{ m B} < -I_{ m min}$
11	Repeat Steps 2 – 10			

^aOnly extracted for the *shortest* channel of each width and fixed for all other geometries.

Table 7.6: Temperature scaling parameter extraction procedure for a long wide channel MOSFET. This scheme only makes sense if measurements have been performed at one or (preferably) more temperatures which differ from room temperature.

Step	Optimized parameters	Fitted on	Abs./Rel.	Conditions
1	STVFB ^a	$I:I_{\mathrm{D}}$	Relative	$I_{ m D} < I_{ m T}$
2	STBETN ^a , STMUE, STTHEMU,	I: I_{D}	Absolute	_
	STCS, STXCOR			
3	$STTHESAT^a$	II: I_{D}	Absolute	_
4	STIG	V: <i>I</i> _G	Relative	$ I_{ m G} > I_{ m min}$
5	STA2	$V:I_{\mathrm{B}}$	Relative	$V_{ m GS} > 0$ V, $I_{ m B} < -I_{ m min}$
6	STBGIDL	V: <i>I</i> _B	Relative	$V_{ m GS} < 0$ V, $I_{ m B} < -I_{ m min}$

^aAlso extracted for one or more long *narrow* devices.

slightly different for the long-channel and for the short-channel case.

For an accurate extraction, the temperature scaling parameters for a long-wide-channel device have to be determined first. In the long-wide-channel case the carrier mobility parameters can be determined, and they are subsequently fixed for all other devices. In Table 7.6 the appropriate extraction procedure is given. In Step 1 the subthreshold temperature dependence is optimized, followed by the optimization of mobility reduction parameters in Step 2. Next the temperature dependence of velocity saturation is optimized in Step 3. In the subsequent steps, parameters for the temperature dependence of the gate current, the impact ionization current and gate-induced drain leakage are determined. The determined values of the mobility reduction temperature scaling parameters (i.e., STMUE, STTHEMU, STCS, and STXCOR) are copied to all other devices and kept fixed during the remainder of the temperature-scaling parameter extraction procedure. Step 1 and 2 could then be performed on one or more long narrow devices as well (for STVFB, STBETN, and STTHESAT only).

Next the extraction procedure as given in Table 7.7 is carried out for several short devices of different widths.

^bOnly extracted for the *shortest widest* device and fixed for all other geometries.

Table 7.7: Temperature scaling parameter extraction procedure for short-channel MOSFETs (both wide and narrow). This scheme only makes sense if measurements have been performed at one or (preferably) more temperatures which differ from room temperature.

Step	Optimized parameters	Fitted on	Abs./Rel.	Conditions
1	STVFB	I: I_{D}	Relative	$V_{\rm GS} < V_{ m T}$
2	STBETN, STRS ^a	I: I_{D}	Absolute	$V_{\rm GS} > V_{ m T}$
3	STTHESAT	II: I_{D}	Absolute	_

^aOnly extracted for a short *narrow* device and fixed for all other geometries.

Preferably, the extraction is done first for a short narrow device, such that the determined value of **STRS** can be used during the extraction of the wider devices.

7.4 Extraction of Geometry Scaling Parameters

The aim of the complete extraction procedure is the determination of the geometry scaling parameters (global parameters), i.e., a single set of parameters (see Section 2.5.3) which gives a good description of the MOSFET-behavior over the full geometry range of a CMOS technology.

Determination of ΔL and ΔW

An extremely important part of the geometry scaling extraction scheme is an accurate determination of ΔL and ΔW , see Eqs. (3.5) and (3.6).³ Since it affects the DC-, the AC- as well as the noise model and, moreover, it can heavily influence the quality of the resulting global parameter set, it is very important that this step is carried out with care.

Traditionally, ΔW can be determined from the extrapolated zero-crossing in **BETN** versus mask width W. In a similar way ΔL can be determined from 1/BETN versus mask length L. For modern MOS devices with pocket implants, however, it has been found that the above ΔL extraction method is no longer valid [6, 7]. Another, more accurate method is to measure the gate-to-bulk capacitance C_{GB} in accumulation for different channel lengths [7, 8]. In this case the extrapolated zero-crossing in the C_{GB} versus mask length L curve will give ΔL . Similarly, the extracted values for **COX** (from the procedure in Table 7.1 and 7.2) vs. mask length L may be used for this purpose. Unfortunately for CMOS technologies in which gate current is non-negligible, capacitance measurements may be hampered by gate current [9]. In this case gate current parameter **IGINV** plotted as a function of channel length L may be used to extract ΔL [9]. If possible, ΔL extraction from C-V-measurements is the preferred method.

Finally, LOV can be obtained from (a series of) extracted values of CGOV from one or more short devices.

From local to global

First of all, the global parameters **TYPE**, **QMC**, and the 'switch'-parameters should be set to the appropriate value. Next, parameters for which no geometrical scaling rules exist must be taken directly from the local set (this applies to **TR**, **TOXO**, **VNSUBO**, **NSLPO**, **DNSUBO**, **TOXOVO**, **NOVO**, **CFBO**, **STMUEO**, **THE-MUO**, **STTHEMUO**, **STCSO**, **STXCORO**, **FETAO**, **STRSO**, **RSBO**, **RSGO**, **THESATBO**, **THESATGO**, **VPO**, **A2O**, **STA2O**, **GCOO**, **STIGO**, **GC2O**, **GC3O**, **CHIBO**, **BGIDLO**, **STBGIDLO**, **CGIDLO**, and **DTA**). Generally, these parameters have been left at their default values or they have been extracted for one device only and subsequently fixed for all other devices. The parameters **LVARO**, **LVARL**, **LVARW**, **WVARO**, **WVARL**, and **WVARW** should be known from technology.

 $^{^3}$ Note that ΔL_{PS} and ΔW_{OD} are expected to be known from the fabrication process. So, in fact, only **LAP** and **WOT** are extracted from the electrical measurements.

Once the values of ΔL and ΔW are firmly established (as described above), **LAP** and **WOT** can be set and the actual extraction procedure of the geometry scaling parameters can be started. It consists of several *independent* sub-steps (which can be carried out in random order), one for each geometry dependent local parameter.

To illustrate such a sub-step, the local parameter \mathbf{CT} is taken as an example. The relevant geometry scaling equation from Section 3.2 is Eq. (3.26), from which it can be seen that \mathbf{CTO} , \mathbf{CTL} , \mathbf{CTLEXP} , and \mathbf{CTW} are the global parameters which determine the value of \mathbf{CT} as a function of L and W. First, the extracted \mathbf{CT} of each device in a length-series of measured (preferably wide) devices are considered as a function of L. In this context \mathbf{CTO} , \mathbf{CTL} , and \mathbf{CTLEXP} are optimized such that the fit of Eq. (3.26) to the extracted \mathbf{CT} -values is as good as possible, while keeping \mathbf{CTW} fixed at 0. Then \mathbf{CTW} is determined by considering the extracted \mathbf{CT} -values from a length-series of measured narrow devices. Finally, the four global parameters may be fine-tuned by optimizing all four parameters to all extracted \mathbf{CT} -values simultaneously. The default values given in Section 2.5.3 are good initial values for the optimization procedure.

All other parameters can be extracted in a similar manner. The local parameters **BETN** and **NEFF** have quite complicated scaling rules, particularly due to the non-uniform doping profiles employed in modern CMOS technologies. Therefore, a few additional guidelines are in place.

- The optimization procedure for **BETN** is facilitated if not **BETN**, but **BETN**_{sq} $\stackrel{\text{def}}{=}$ **BETN** $\cdot L_{\text{E}}/W_{\text{E}}$ is considered.
- Starting from the default values, first UO, FBET1, LP1, FBET2, and LP2 should be determined from a
 length-series of wide devices. Then BETW1, BETW2, and WBET should be determined from a widthseries of long devices. Finally, FBET1W and LP1W can be found by considering some short narrow
 devices.
- Starting from the default values, first extract FOL1, FOL2, NSUBO, NPCK, and LPCK from a length-series of wide devices. Here, NSUBO determines the long-channel value of NEFF. Moreover, NPCK and LPCK determine the increase of NEFF for shorter channels (short channel effect), while FOL1 and FOL2 are used to describe the decrease of NEFF for very short channels (reverse short channel effect).
- Then **NSUBW** and **WSEG** can be determined form a width-series of long devices. Finally, **NPCKW**, **LPCKW** and **WEGP** are determined from a width-series of short devices.
- Especially for **BETN** and **NEFF** it is advisable—after completing the procedure described above—to fine tune the global parameters found by considering all extracted values of **BETN** (or **NEFF**) simultaneously.

Note that in many cases it may not be necessary to use the full flexibility of PSP's parameter scaling, e.g., for many technologies **NP** and **VFB** may be considered as independent of geometry. If such a geometry-independence is anticipated, the corresponding local parameter should be fixed during local parameter extraction. Only if the resulting global parameter set is not satisfactory, the parameter should be allowed to vary during a subsequent optimization round.

Fine tuning

Once the complete set of global parameters is found, the global model should give an accurate description of the measured I-V-curves and capacitance measurements. Either for fine tuning or to facilitate the extraction of global parameters for which the geometry scaling of the corresponding extracted local parameters is not well-behaved, there are two more things that can be done.

- Local parameters for which the fitting of global parameters was completed satisfactorily could be replaced by the values calculated from the geometrical scaling rules and fixed. Then one could redo (parts of) the local parameter extraction procedure for the remaining local parameters, making them less sensitive for cross-correlations.
- Small groups of global parameters may be fitted directly to the measurements of a well-chosen series of devices, using the global model.

7.5 Summary – Geometrical scaling

Summarizing, for the determination of a full parameter set, the following procedure is recommended.

- 1. Determine local parameter sets (VFB, NEFF, ...) for all measured devices, as explained in Section 7.2 and 7.3.
- 2. Find ΔL and ΔW .
- 3. Determine the global parameters by fitting the appropriate geometry scaling rules to the extracted local parameters.
- 4. Finally, the resulting global can be fine-tuned, by fitting the result of the scaling rules and current equations to the measured currents of all devices simultaneously.

7.6 Extraction of Binning Parameters

In this section, expressions will be given for the parameters in the binning scaling rules, **POYYY**, **PLYYY**, **PWYYY**, and **PLWYYY**, as given in Section 3.3. These coefficients will be expressed in terms of parameter values at the corners of bin (see Fig. 7.1). These expressions can be easily found by substituting the parameter values at the bin corners into the binning scaling rules and inverting the resulting four equations. Note once

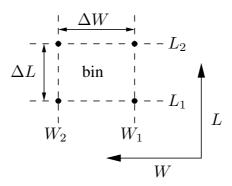


Figure 7.1: Schematic view of a bin, showing the coordinates of the four corners. Note that L_1 , L_2 , W_1 , and W_2 denote the *effective* length and width (L_E and W_E) at the bin corners.

more that this results in a separate parameter set for each bin.

In the expression below, the value of parameter YYY at bin corner (L_i, W_j) is denoted by Y_{ij} (i=1,2, j=1,2). Moreover, $\Delta L = L_2 - L_1$, $\Delta W = W_2 - W_1$, $A = 1/(\Delta L \cdot \Delta W)$.

1. Coefficients for type I scaling

$$\mathbf{POYYY} = A \cdot (L_1 \cdot W_1 \cdot Y_{11} - L_1 \cdot W_2 \cdot Y_{12} - L_2 \cdot W_1 \cdot Y_{21} + L_2 \cdot W_2 \cdot Y_{22})$$
(7.1)

$$\mathbf{PLYYY} = A \cdot \frac{L_1 \cdot L_2}{L_{\text{EN}}} \cdot (-W_1 \cdot Y_{11} + W_2 \cdot Y_{12} + W_1 \cdot Y_{21} - W_2 \cdot Y_{22})$$
 (7.2)

$$\mathbf{PWYYY} = A \cdot \frac{W_1 \cdot W_2}{W_{\text{EN}}} \cdot \left(-L_1 \cdot Y_{11} + L_1 \cdot Y_{12} - L_2 \cdot Y_{21} - L_2 \cdot Y_{22} \right)$$
(7.3)

$$\mathbf{PLWYYY} = A \cdot \frac{L_1 \cdot L_2 \cdot W_1 \cdot W_2}{L_{\text{EN}} \cdot W_{\text{EN}}} \cdot (Y_{11} - Y_{12} - Y_{21} + Y_{22})$$
 (7.4)

2. Coefficients for type II scaling

$$\mathbf{POYYY} = A \cdot (L_2 \cdot W_2 \cdot Y_{11} - L_2 \cdot W_1 \cdot Y_{12} - L_1 \cdot W_2 \cdot Y_{21} + L_1 \cdot W_1 \cdot Y_{22}) \tag{7.5}$$

$$\mathbf{PLYYY} = A \cdot L_{\text{EN}} \cdot (-W_2 \cdot Y_{11} + W_1 \cdot Y_{12} + W_2 \cdot Y_{21} - W_1 \cdot Y_{22}) \tag{7.6}$$

$$\mathbf{PWYYY} = A \cdot W_{\text{EN}} \cdot (-L_2 \cdot Y_{11} + L_2 \cdot Y_{12} - L_1 \cdot Y_{21} - L_1 \cdot Y_{22}) \tag{7.7}$$

$$PLWYYY = A \cdot L_{EN} \cdot W_{EN} \cdot (Y_{11} - Y_{12} - Y_{21} + Y_{22})$$
(7.8)

3. Coefficients for type III scaling

$$\mathbf{POYYY} = A \cdot (-L_1 \cdot W_2 \cdot Y_{11} + L_1 \cdot W_1 \cdot Y_{12} + L_2 \cdot W_2 \cdot Y_{21} - L_2 \cdot W_1 \cdot Y_{22})$$
(7.9)

$$\mathbf{PLYYY} = A \cdot \frac{L_1 \cdot L_2}{L_{\text{EN}}} \cdot (W_2 \cdot Y_{11} - W_1 \cdot Y_{12} - W_2 \cdot Y_{21} + W_1 \cdot Y_{22})$$
 (7.10)

$$\mathbf{PWYYY} = A \cdot W_{\text{EN}} \cdot (L_1 \cdot Y_{11} - L_1 \cdot Y_{12} - L_2 \cdot Y_{21} + L_2 \cdot Y_{22})$$
 (7.11)

$$\mathbf{PLWYYY} = A \cdot \frac{L_1 \cdot L_2 \cdot W_{\text{EN}}}{L_{\text{EN}}} \cdot (-Y_{11} + Y_{12} + Y_{21} - Y_{22})$$
 (7.12)

Note: For L_1 , L_2 , W_1 , and W_2 in the formulas above one must take the *effective* length and width (L_E and W_E) as defined in Section 3.2.

Section 8

DC Operating Point Output

The DC operating point output facility gives information on the state of a device at its operation point. Beside terminal currents and voltages, the magnitudes of linearized internal elements are given. In some cases meaningful quantities can be derived which are then also given (e.g., $f_{\rm T}$). The objective of the DC operating point facility is twofold:

- Calculate small-signal equivalent circuit element values
- Open a window on the internal bias conditions of the device and its basic capabilities.

All accessible quantities are described in the table below. The symbols in the 'value' column are defined in Section 4. Besides, the following notation is used: $P_D = 1 + k_p \cdot G/4$, where k_p is defined in Eq. (4.14).

Important note: For *all* operating point output the signs are such as if the device is an NMOS. Moreover, whenever there is a reference to the 'drain', this is always the terminal which is acting as drain for the actual bias conditions. This is even true for variables such as **vds** (which is therefore always nonnegative) and the junction-related variables. The output variable **sdint** shows whether or not this 'drain' is the same as the terminal which was named 'drain' in the simulator.

No.	Name	Unit	Value	Description
0	ctype	_	1 for NMOS, −1 for PMOS	Flag for channel-type
1	sdint	_	1 if $V'_{\rm DS} \ge 0$, -1 otherwise	Flag for source-drain interchange
			Current components	
2	ise	A	$I_{ m S}-I_{ m JS}$	Total source current
3	ige	A	$I_{ m G}$	Total gate current
4	ide	A	$I_{ m D}-I_{ m JD}$	Total drain current
5	ibe	A	$I_{ m B}+I_{ m JS}+I_{ m JD}$	Total bulk current
6	ids	A	$I_{ m DS}$	Drain current, excl. avalanche and tunnel currents
7	idb	A	$I_{ m avl} + I_{ m gidl} - I_{ m JD}$	Drain-to-bulk current
8	isb	A	$I_{ m gisl}-I_{ m JS}$	Source-to-bulk current
9	igs	A	$I_{ m GCS} + I_{ m GSov}$	Gate-source tunneling current
10	igd	A	$I_{ m GCD} + I_{ m GDov}$	Gate-drain tunneling current
11	igb	A	$I_{ m GB}$	Gate-bulk tunneling current

continued on next page...

.. continued from previous page

continued from previous page						
No.	Name	Unit	Value	Description		
12	igcs	A	$I_{ m GCS}$	Gate-channel tunneling current (source component)		
13	igcd	A	$I_{ m GCD}$	Gate-channel tunneling current (drain component)		
14	iavl	A	$I_{ m avl}$	Substrate current due to weak-avalanche		
15	igisl	A	$I_{ m gisl}$	Gate-induced source leakage current		
16	igidl	A	$I_{ m gidl}$	Gate-induced drain leakage current		
	T	T	Junction currents			
17	ijs	A	$I_{ m JS}$	Total source junction current		
18	ijsbot	A	$I_{ m JS, bot}$	Source junction current, bottom component		
19	ijsgat	A	$I_{ m JS,gat}$	Source junction current, gate-edge component		
20	ijssti	A	$I_{ m JS,sti}$	Source junction current, STI-edge component		
21	ijd	A	$I_{ m JD}$	Total drain junction current		
22	ijdbot	A	$I_{ m JD,bot}$	Drain junction current, bottom component		
23	ijdgat	A	$I_{ m JD,gat}$	Drain junction current, gate-edge component		
24	ijdsti	A	$I_{ m JD,sti}$	Drain junction current, STI-edge component		
			Voltages			
25	vds	V	$V_{ m DS}$	Drain-source voltage		
26	vgs	V	$V_{ m GS}$	Gate-source voltage		
27	vsb	V	$V_{ m SB}$	Source-bulk voltage		
28	vto	V	$ \mathbf{VFB} + P_{\mathbf{D}} \cdot (\boldsymbol{\phi_{\mathbf{B}}} + 2 \cdot \boldsymbol{\phi_{\mathbf{T}}^*}) + G \cdot \sqrt{\boldsymbol{\phi_{\mathbf{T}}^*} \cdot (\boldsymbol{\phi_{\mathbf{B}}} + 2 \cdot \boldsymbol{\phi_{\mathbf{T}}^*})} $	Zero-bias threshold voltage		
29	vts	V	$ \begin{aligned} \mathbf{VFB} + P_{\mathrm{D}} \cdot (V_{\mathrm{SB}}^* + \phi_{\mathbf{B}} + 2 \cdot \phi_{\mathbf{T}}^*) - V_{\mathrm{SB}}^* + \\ G \cdot \sqrt{\phi_{\mathbf{T}}^* \cdot (V_{\mathrm{SB}}^* + \phi_{\mathbf{B}} + 2 \cdot \phi_{\mathbf{T}}^*)} \end{aligned} $	Threshold voltage including backbias effects		
30	vth	V	$ ext{vts} - \Delta V_{ ext{G}}$	Threshold voltage including backbias and drain-bias effects		
31	vgt	V	vgs – vth	Effective gate drive voltage including drain- and back-bias effects		
32	vdss	V	$V_{ m dsat}$	Drain saturation voltage at actual bias		
33	vsat	V	$V_{ m DS} - V_{ m dsat}$	Saturation limit		
(Trans-)conductances						
34	gm	A/V	$\partial {f ide}/\partial V_{ m GS}$	Transconductance		
35	gmb	A/V	$-\partial {f ide}/\partial V_{ m SB}$	Substrate-transconductance		

continued on next page...

... continued from previous page

continued from previous page						
No.	Name	Unit	Value	Description		
36	gds	A/V	$\partial {f ide}/\partial V_{ m DS}$	Output conductance		
37	gjs	A/V	$-\partial \mathbf{ijs}/\partial V_{\mathrm{SB}}$	Source junction conductance		
38	gjd	A/V	$-(\partial \mathbf{ijd}/\partial V_{\mathrm{DS}} + \partial \mathbf{ijd}/\partial V_{\mathrm{SB}})$	Drain junction conductance		
Capacitances						
39	cdd	F	$\partial Q_{ m D}^{(i)}/\partial V_{ m DS}$	Drain capacitance		
40	cdg	F	$-\partial Q_{ m D}^{(i)}/\partial V_{ m GS}$	Drain-gate capacitance		
41	cds	F	cdd – cdg – cdb	Drain-source capacitance		
42	cdb	F	$\partial Q_{ m D}^{(i)}/\partial V_{ m SB}$	Drain-bulk capacitance		
43	cgd	F	$-\partial Q_{ m G}^{(i)}/\partial V_{ m DS}$	Gate-drain capacitance		
44	cgg	F	$\partial Q_{ m G}^{(i)}/\partial V_{ m GS}$	Gate capacitance		
45	cgs	F	cgg - cgd - cgb	Gate-source capacitance		
46	cgb	F	$\partial Q_{ m G}^{(i)}/\partial V_{ m SB}$	Gate-bulk capacitance		
47	csd	F	$-\partial Q_{ m S}^{(i)}/\partial V_{ m DS}$	Source-drain capacitance		
48	csg	F	$-\partial Q_{ m S}^{(i)}/\partial V_{ m GS}$	Source-gate capacitance		
49	css	F	csg + csd + csb	Source capacitance		
50	csb	F	$\partial Q_{ m S}^{(i)}/\partial V_{ m SB}$	Source-bulk capacitance		
51	cbd	F	$-\partial Q_{ m B}^{(i)}/\partial V_{ m DS}$	Bulk-drain capacitance		
52	cbg	F	$-\partial Q_{ m B}^{(i)}/\partial V_{ m GS}$	Bulk-gate capacitance		
53	cbs	F	cbb - cbd - cbg	Bulk-source capacitance		
54	cbb	F	$-\partial Q_{ m B}^{(i)}/\partial V_{ m SB}$	Bulk capacitance		
55	cgsol	F	$\partial (Q_{\rm sov} + Q_{\rm ofs})/\partial V_{\rm GS}$	Total gate-source overlap capacitance		
56	cgdol	F	$\partial (Q_{ m dov} + Q_{ m ofd})/\partial V_{ m DS}$	Total gate-drain overlap capacitance		
Junction capacitances						
57	cjs	F	$C_{ m JS}$	Total source junction capacitance		
58	cjsbot	F	$C_{ m JS, bot}$	Source junction capacitance, bottom component		
59	cjsgat	F	$C_{ m JS,gat}$	Source junction capacitance, gate- edge component		
60	cjssti	F	$C_{ m JS,sti}$	Source junction capacitance, STI-edge component		
61	cjd	F	$C_{ m JD}$	Total drain junction capacitance		
62	cjdbot	F	$C_{ m JD,bot}$	Drain junction capacitance, bottom component		
63	cjdgat	F	$C_{ m JD,gat}$	Drain junction capacitance, gate- edge component		
64	cjdsti	F	$C_{ m JD,sti}$	Drain junction capacitance, STI-edge component		

continued on next page...

... continued from previous page

No.	Name	Unit	Value	Description
			Miscellaneous	·
65	weff	m	$W_{ m E}$	Effective channel width for geometrical models
66	leff	m	$L_{ m E}$	Effective channel length for geometrical models
67	u	-	gm/gds	Transistor gain
68	rout	Ω	1/ gds	Small-signal output resistance
69	vearly	V	ide /gds	Equivalent Early voltage
70	beff	A/V ²	$2 \cdot \mathbf{ide} /\mathbf{vgt}^2$	Gain factor
71	fug	Hz	$\boxed{\mathbf{gm}/[2 \cdot \pi \cdot (\mathbf{cgg} + \mathbf{cgsol} + \mathbf{cgdol})]}$	Unity gain frequency at actual bias
			Noise	
72	sqrtsff	V/√Hz	$\sqrt{S_{ m fl}(1~{ m kHz})}/{ m gm}$	Input-referred RMS white noise voltage density at 1 kHz
73	sqrtsfw	V/√Hz	$\sqrt{S_{ m id}}/{ m gm}$	Input-referred RMS white noise voltage density
74	sid	A^2/Hz	$S_{ m id}$	Channel thermal noise current density
75	sig	A^2/Hz	$S_{ m ig}(1~{ m kHz})$	Induced gate noise current density at 1 kHz
76	cigid	_	$\frac{m_{\mathrm{igid}}}{\sqrt{m_{\mathrm{ig}} \cdot m_{\mathrm{id}}}}$	Imaginary part of correlation coefficient between S_{ig} and S_{id}
77	fknee	Hz	$1 ext{Hz} \cdot S_{ ext{fl}}(1 ext{Hz})/S_{ ext{id}}$	Cross-over frequency above which white noise is dominant
78	sigs	A^2/Hz	$S_{ m igs}$	Gate-source current noise spectral density
79	sigd	A^2/Hz	$S_{ m igd}$	Gate-drain current noise spectral density
80	siavl	A^2/Hz	$S_{ m avl}$	Impact ionization current noise spectral density
81	ssi	A^2/Hz	$S_{ m S,I}$	Total source junction current noise spectral density
82	sdi	A^2/Hz	$S_{ m D,I}$	Total drain junction current noise spectral density

References

- [1] L. Lemaitre, C. C. McAndrew, and S. Hamm, "ADMS Automatic Device Model Synthesize", *Proc. IEEE CICC*, 2002. See also http://mot-adms.sourceforge.net/
- [2] X. Xi et al., BSIM4.4.0 MOSFET Model, User's Manual, 2004, available for download at http://www-device.eecs.berkeley.edu/~bsim3/BSIM4/BSIM440/
- [3] H. Wang, T.-L. Chen, and G. Gildenblat, "Quasi-static and Nonquasi-static Compact MOSFET Models Based on Symmetric Linearization of the Bulk and Inversion Charges," *IEEE trans. Electron Dev.* **50**(11), pp. 2262-2272, 2003.
- [4] H. Wang *et al.*, "Unified Non-Quasi-Static MOSFET Model for Large-Signal and Small-Signal Simulations," *CICC* 2005.
- [5] W. H. Press *et al.*, "Numerical recipes in C", 2nd edition, Cambridge University Press (1993), available for download at http://www.library.cornell.edu/nr/bookcpdf.html
- [6] M. Minondo, G. Gouget, and A. Juge, "New Length Scaling of Current Gain Factor and Characterization Method for Pocket Implanted MOSFET's," *Proc. ICMTS* 2001, pp. 263-267, 2001.
- [7] A.J. Scholten, R. Duffy, R. van Langevelde, and D.B.M. Klaassen, "Compact Modelling of Pocket-Implanted MOSFETs," *Proc. ESSDERC* 2001, pp. 311-314, 2001.
- [8] T.S. Hsieh, Y.W. Chang, W.J. Tsai, and T.C. Lu, "A New Leff Extraction Approach for Devices with Pocket Implants," *Proc. ICMTS* 2001, pp. 15-18, 2001.
- [9] R. van Langevelde *et al.*, "Gate Current: modelling, ΔL Extraction and Impact on RF Performance," *IEDM* 2001 Tech. Digest, pp. 289-292, 2001.

Appendix A

Auxiliary Equations

In this Appendix, some auxiliary functions which are used in the model equations are defined.

The MINA-smoothing function:

MINA
$$(x, y, a) = \frac{1}{2} \cdot \left[x + y - \sqrt{(x - y)^2 + a} \right]$$
 (A.1)

The MAXA-smoothing function:

MAXA
$$(x, y, a) = \frac{1}{2} \cdot \left[x + y + \sqrt{(x - y)^2 + a} \right]$$
 (A.2)

The functions $\chi(y)$, its derivatives, σ_1 , and σ_2 , which are used in the explicit approximation of surface potential:

$$\chi(y) = \frac{y^2}{2 + y^2} \tag{A.3}$$

$$\chi'(y) = \frac{4y}{(2+y^2)^2} \tag{A.4}$$

$$\chi''(y) = \frac{8 - 12y^2}{(2 + y^2)^3} \tag{A.5}$$

$$\nu = a + c \tag{A.6}$$

$$\mu_1 = \frac{v^2}{\tau} + \frac{c^2}{2} - a \tag{A.7}$$

$$\sigma_1(a, c, \tau, \eta) = \frac{a \cdot \nu}{\mu_1 + (c^2/3 - a) \cdot c \cdot \nu/\mu_1} + \eta$$
(A.8)

$$\mu_2 = \frac{v^2}{\tau} + \frac{c^2}{2} - a \cdot b \tag{A.9}$$

$$\sigma_2(a, b, c, \tau, \eta) = \frac{a \cdot \nu}{\mu_2 + (c^2/3 - a \cdot b) \cdot c \cdot \nu/\mu_2} + \eta \tag{A.10}$$